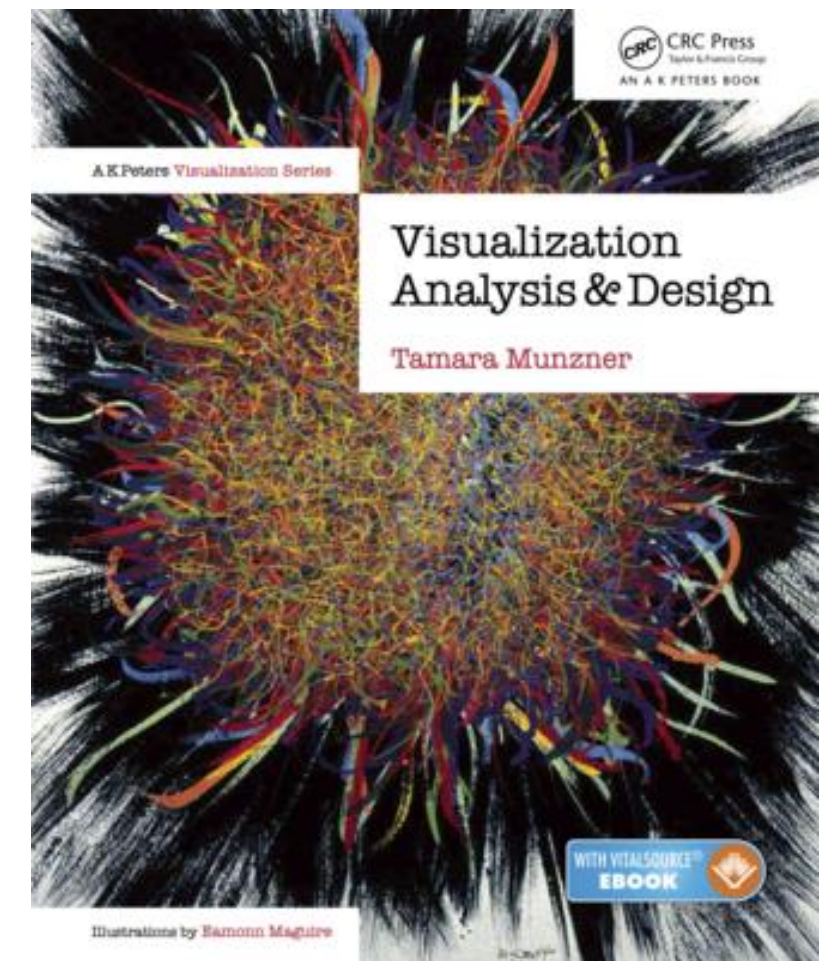


Information Visualization

Spatial Layout

- Slides refer to <https://www.cs.ubc.ca/~tmm/>



Spatial Layout

- Arrange Tables
- Arrange Spatial Data
- Arrange Networks and Trees

How?

Encode

⊕ Arrange

→ Express



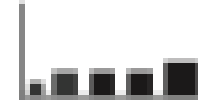
→ Separate



→ Order



→ Align



→ Use



⊕ Map

from **categorical** and **ordered** attributes

→ Color

→ Hue



→ Saturation



→ Luminance



→ Size, Angle, Curvature, ...



→ Shape



→ Motion

Direction, Rate, Frequency, ...

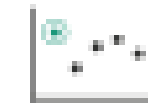


Manipulate

⊕ Change



⊕ Select



⊕ Navigate

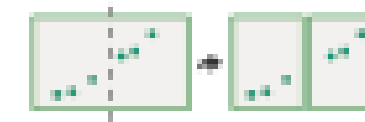


Facet

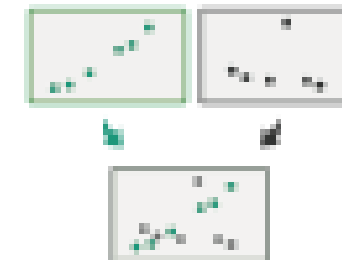
⊕ Juxtapose



⊕ Partition

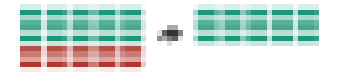


⊕ Superimpose

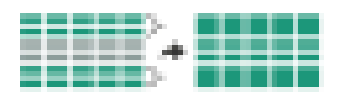


Reduce

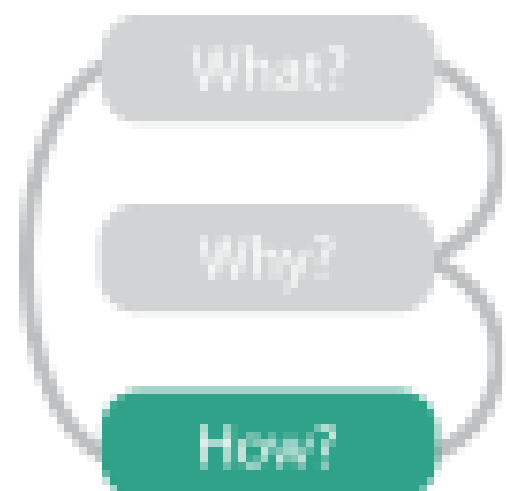
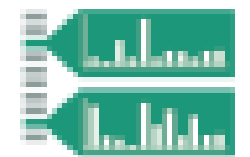
⊕ Filter



⊕ Aggregate



⊕ Embed



Encode tables: Arrange space

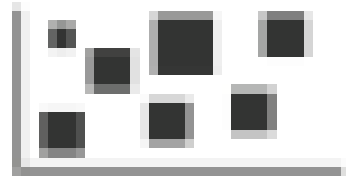
Encode

⊕ Arrange

→ Express



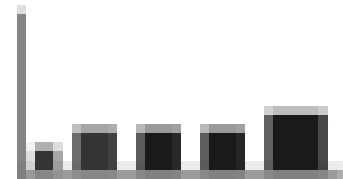
→ Separate



→ Order



→ Align



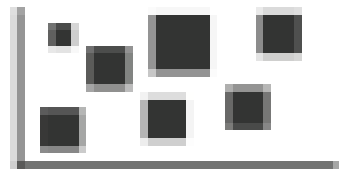
Arrange tables

⊕ Express Values

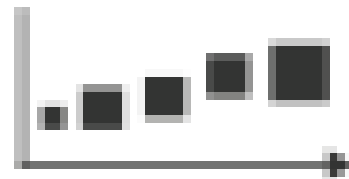


⊕ Separate, Order, Align Regions

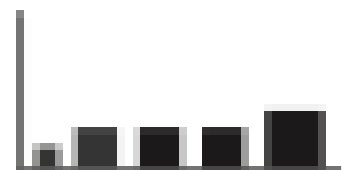
→ Separate



→ Order



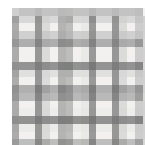
→ Align



→ 1 Key *List*



→ 2 Keys *Matrix*



→ 3 Keys *Volume*

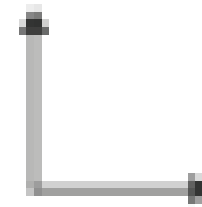


→ Many Keys *Recursive Subdivision*



⊕ Axis Orientation

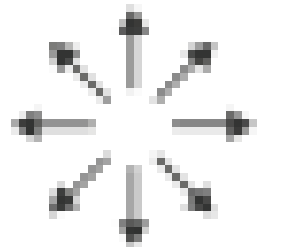
→ Rectilinear



→ Parallel

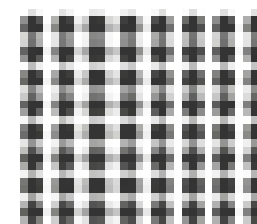


→ Radial

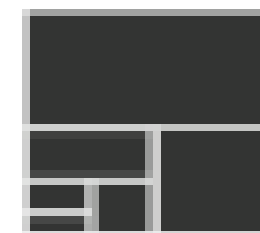


⊕ Layout Density

→ Dense



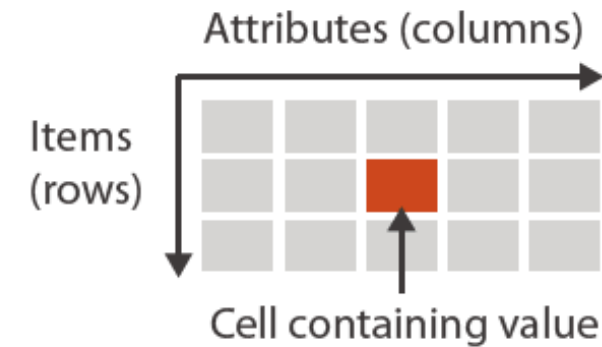
→ Space-Filling



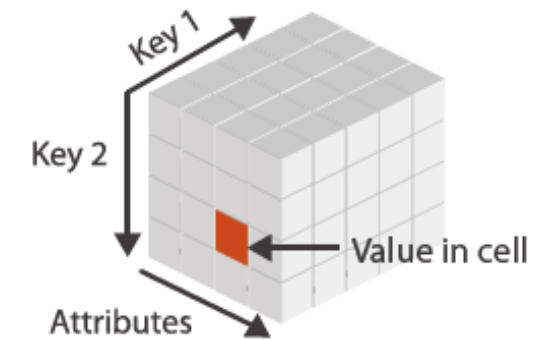
Keys and values

- key
 - independent attribute
 - used as unique index to look up items
 - simple tables: 1 key
 - multidimensional tables: multiple keys
- value
 - dependent attribute, value of cell
- classify arrangements by key count
 - 0, 1, 2, many...

→ Tables



→ Multidimensional Table



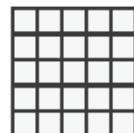
⊕ Express Values



→ 1 Key *List*



→ 2 Keys *Matrix*



→ 3 Keys *Volume*



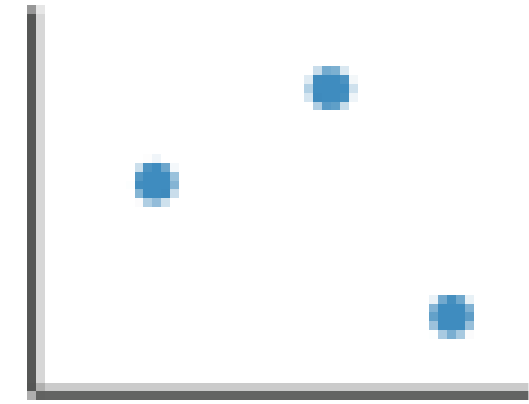
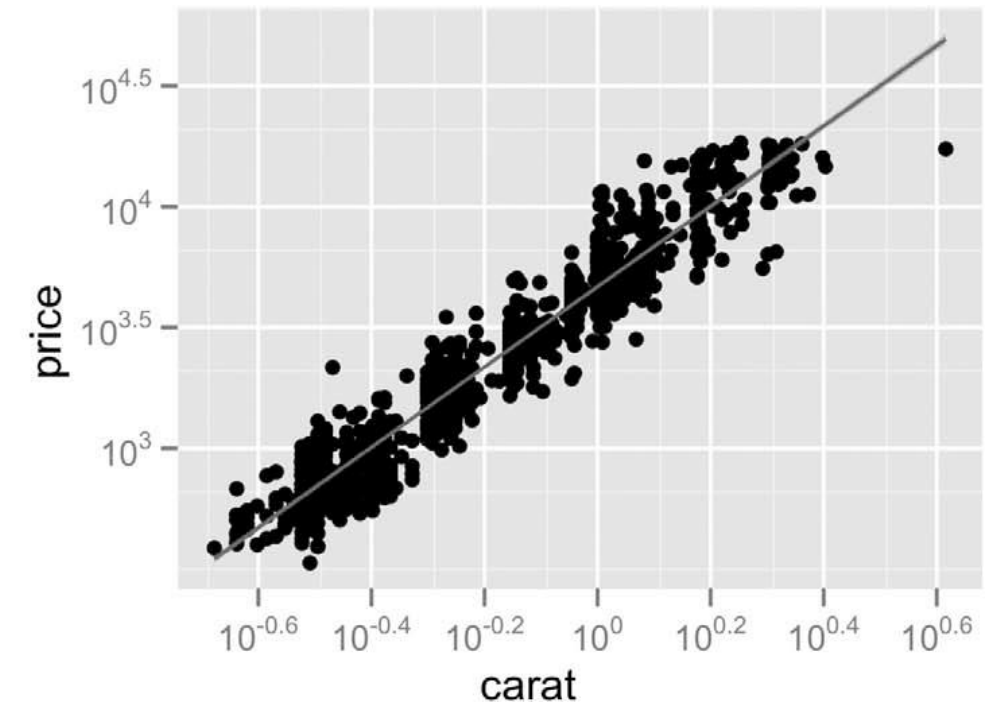
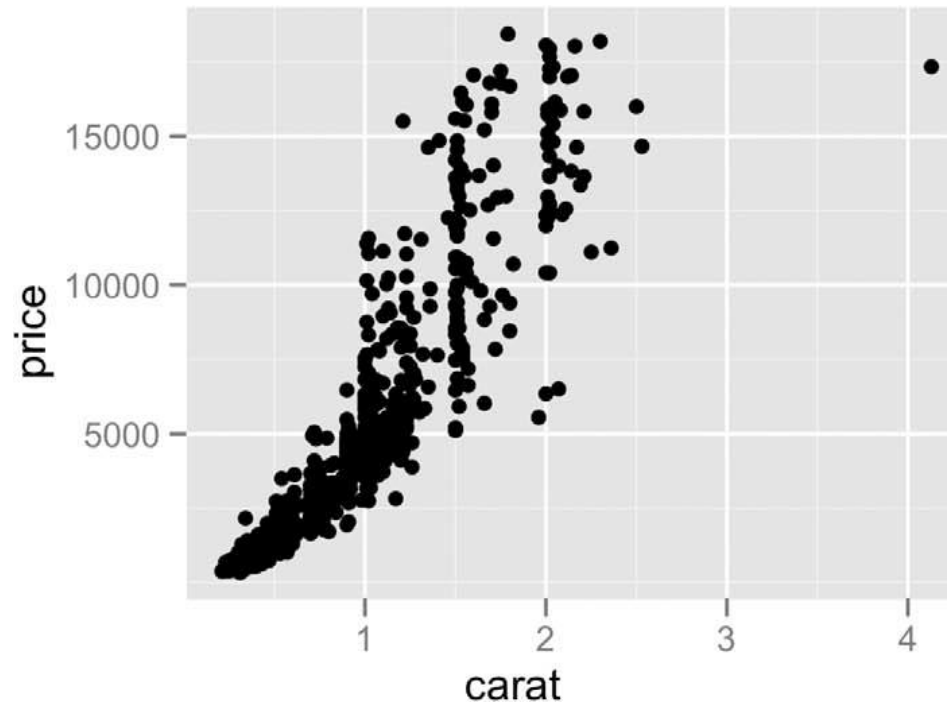
→ Many Keys *Recursive Subdivision*



Idiom: **scatterplot**

- *express* values
 - quantitative attributes
- no keys, only values
 - data
 - 2 quant attribs
 - mark: points
 - channels
 - horiz + vert position
 - tasks
 - find trends, outliers, distribution, correlation, clusters
 - scalability
 - hundreds of items

⊕ Express Values



Some keys: Categorical regions

→ Separate



→ Order



→ Align

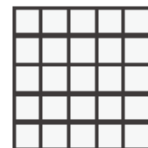


- regions: contiguous bounded areas distinct from each other
 - using space to *separate* (proximity)
 - following expressiveness principle for categorical attributes
- use ordered attribute to *order* and *align* regions

→ 1 Key
List



→ 2 Keys
Matrix



→ 3 Keys
Volume

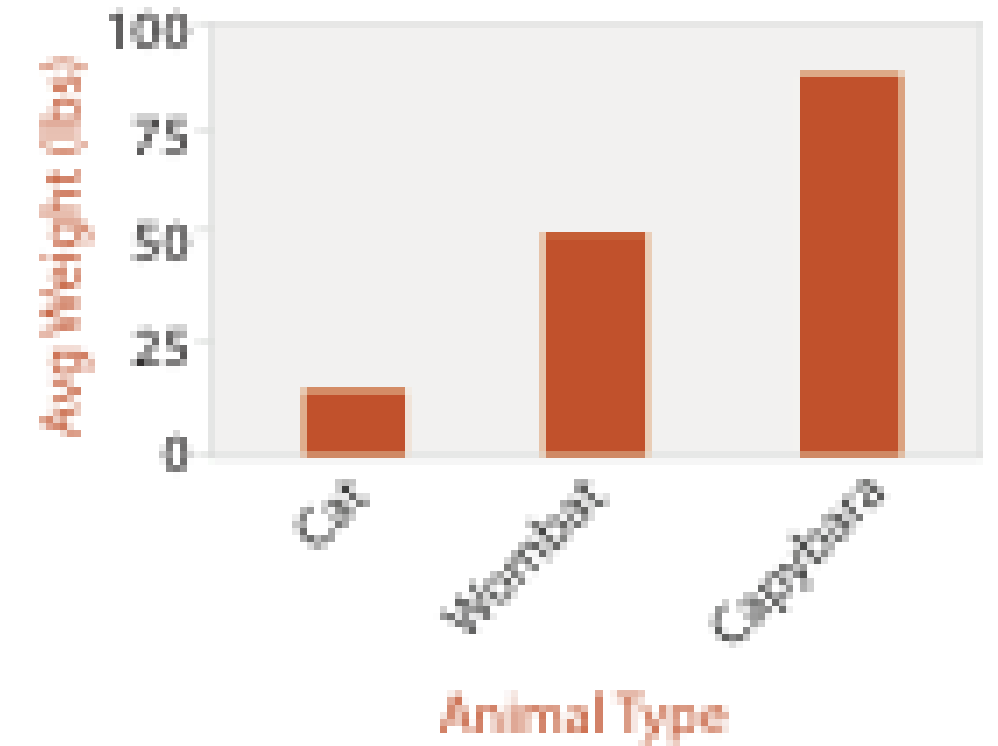
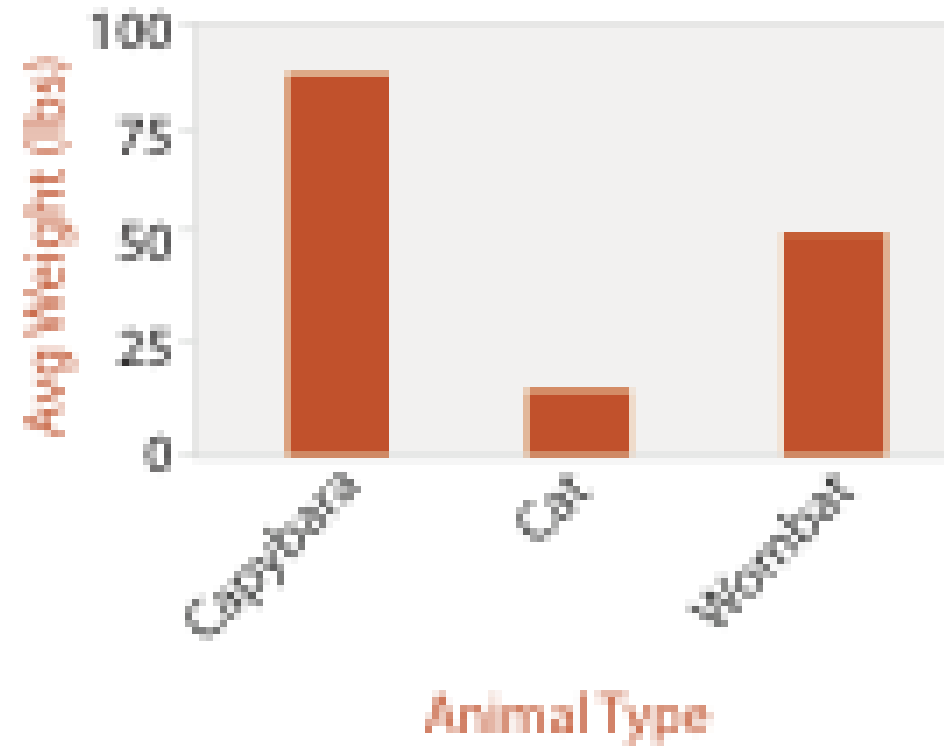


→ Many Keys
Recursive Subdivision



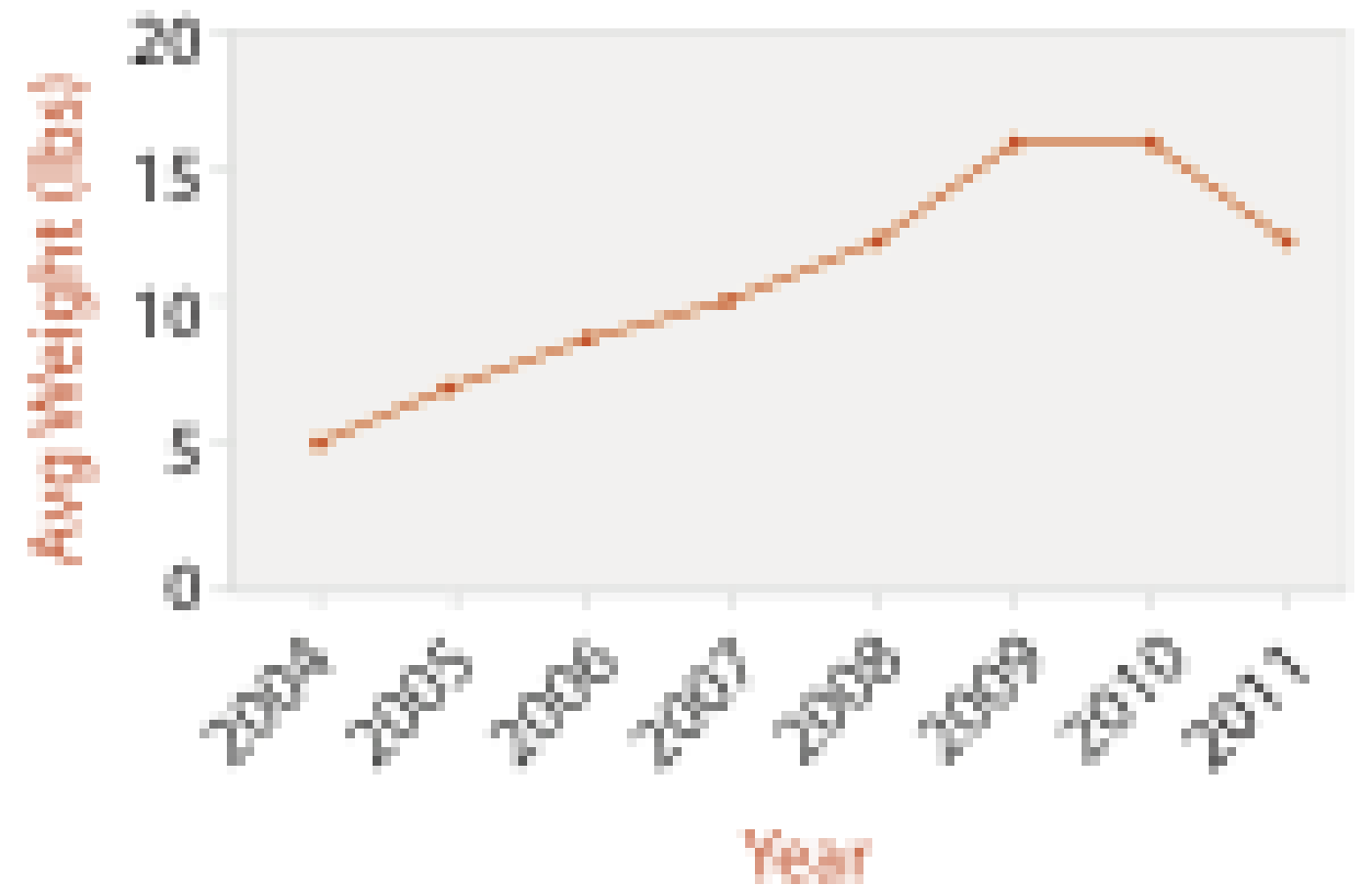
Idiom: **bar chart**

- one key, one value
 - data
 - 1 categ attrib, 1 quant attrib
 - mark: lines
 - channels
 - length to express quant value
 - spatial regions: one per mark
 - separated horizontally, aligned vertically
 - ordered by quant attrib
 - » by label (alphabetical), by length attrib (data-driven)
 - task
 - compare, lookup values
 - scalability
 - dozens to hundreds of levels for key attrib



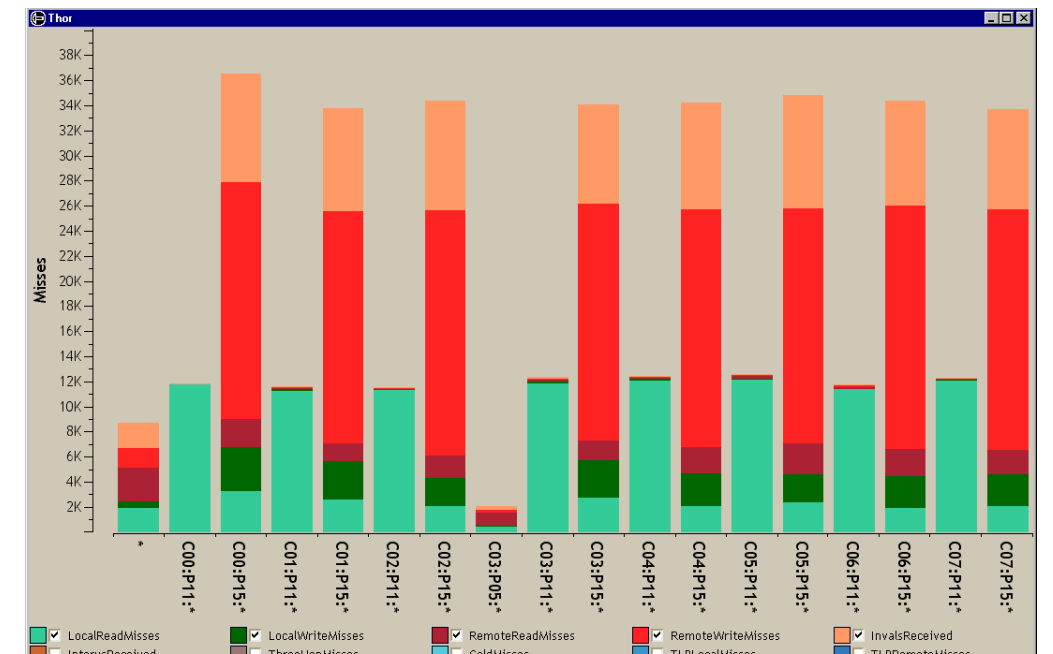
Idiom: **line chart**

- one key, one value
 - data
 - 2 quant attribs
 - mark: points
 - line connection marks between them
 - channels
 - aligned lengths to express quant value
 - separated and ordered by key attrib into horizontal regions
 - task
 - find trend
 - connection marks emphasize ordering of items along key axis by explicitly showing relationship between one item and the next



Idiom: **stacked bar chart**

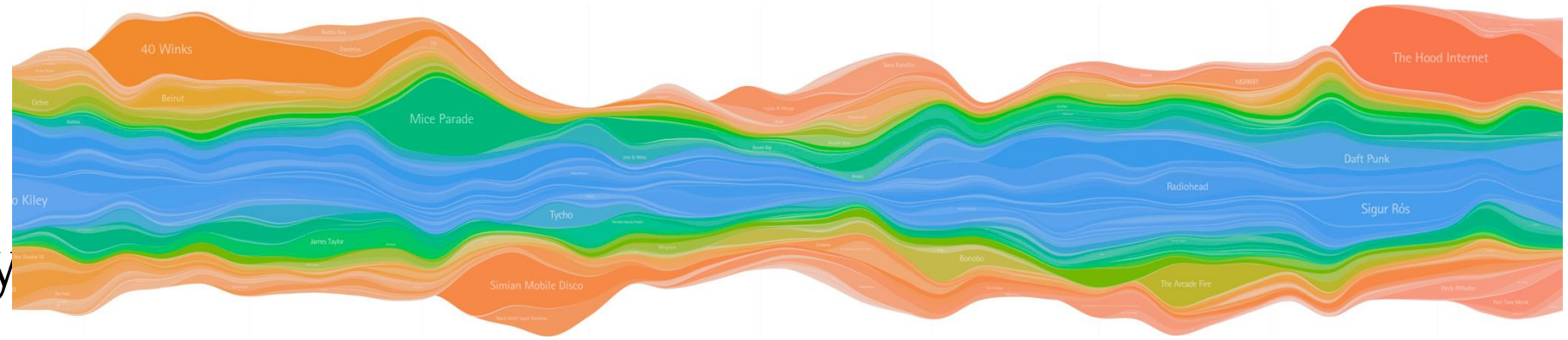
- one more key
 - data
 - 2 categ attrib, 1 quant attrib
 - mark: vertical stack of line marks
 - glyph: composite object, internal structure from multiple marks
 - channels
 - length and color hue
 - spatial regions: one per glyph
 - aligned: full glyph, lowest bar component
 - unaligned: other bar components
 - task
 - part-to-whole relationship
 - scalability
 - several to one dozen levels for stacked attrib



[Using Visualization to Understand the Behavior of Computer Systems. Bosch. Ph.D. thesis, Stanford Computer Science, 2001.]

Idiom: **streamgraph**

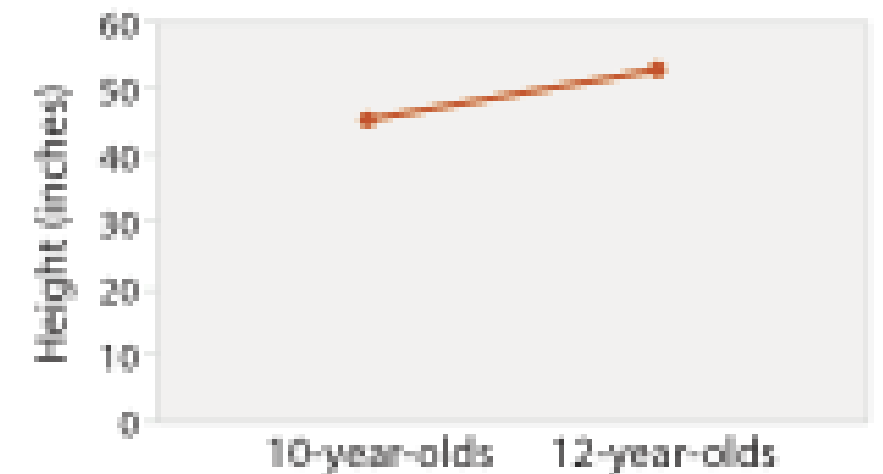
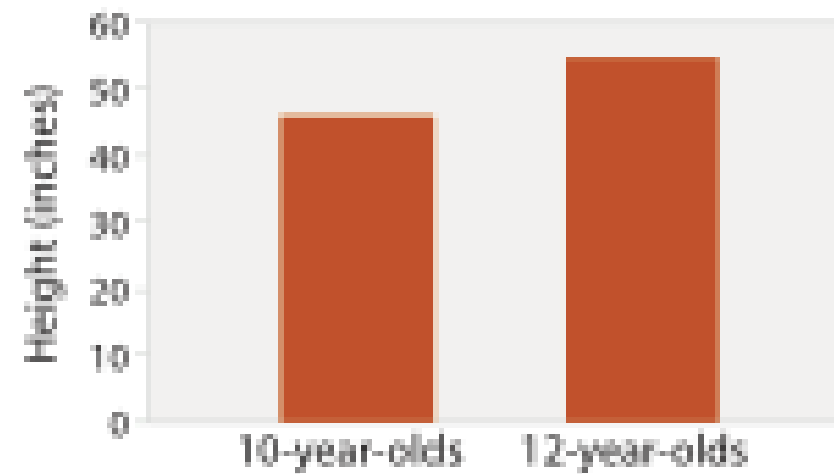
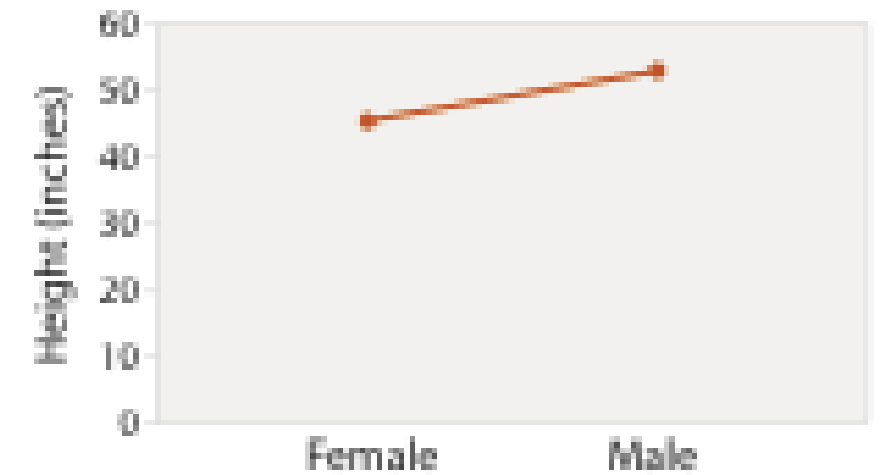
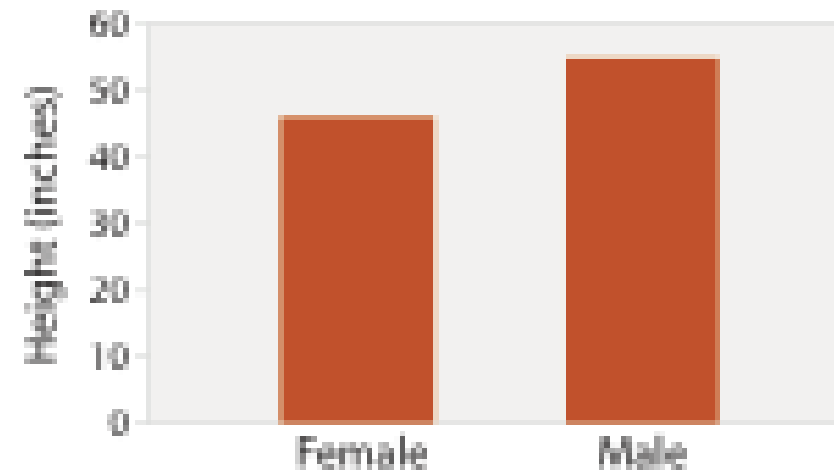
- generalized stacked graph
 - emphasizing horizontal continuity
 - vs vertical items
 - data
 - 1 categ key attrib (artist)
 - 1 ordered key attrib (time)
 - 1 quant value attrib (counts)
 - derived data
 - geometry: layers, where height encodes counts
 - 1 quant attrib (layer ordering)
 - scalability
 - hundreds of time keys
 - dozens to hundreds of artist keys
 - more than stacked bars, since most layers don't extend across whole chart



[Stacked Graphs Geometry & Aesthetics. Byron and Wattenberg. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis 2008) 14(6): 1245 – 1252, (2008).]

Choosing bar vs line charts

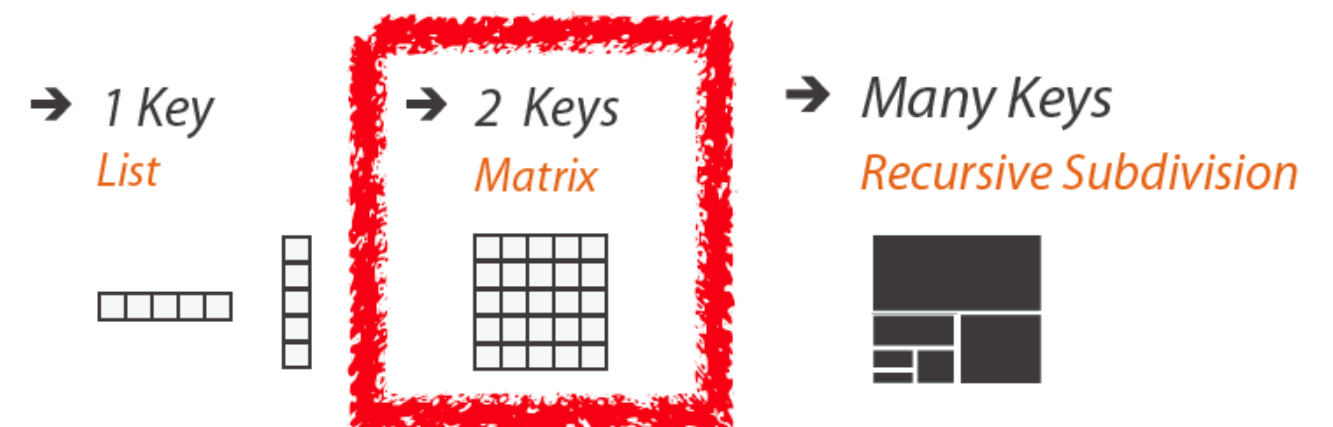
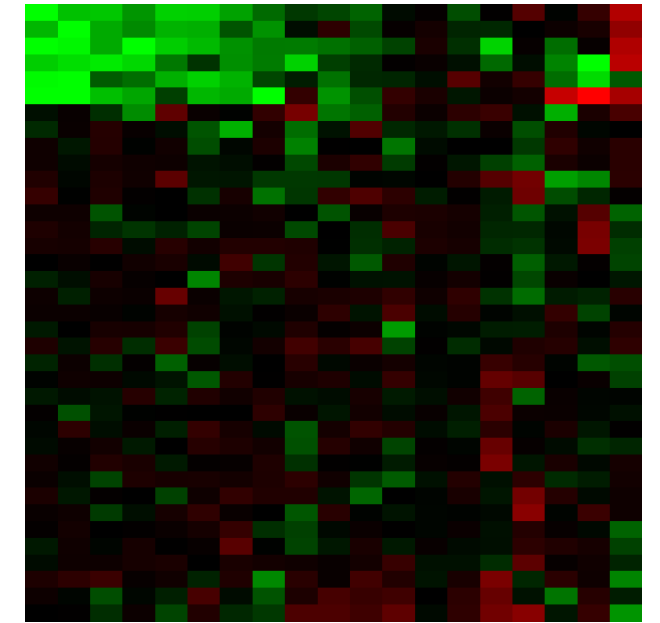
- depends on type of key attrib
 - bar charts if categorical
 - line charts if ordered
- do not use line charts for categorical key attribs
 - violates expressiveness principle
 - implication of trend so strong that it overrides semantics!
 - “The more male a person is, the taller he/she is”



after [Bars and Lines: A Study of Graphic Communication. Zacks and Tversky. Memory and Cognition 27:6 (1999), 1073 – 1079.]

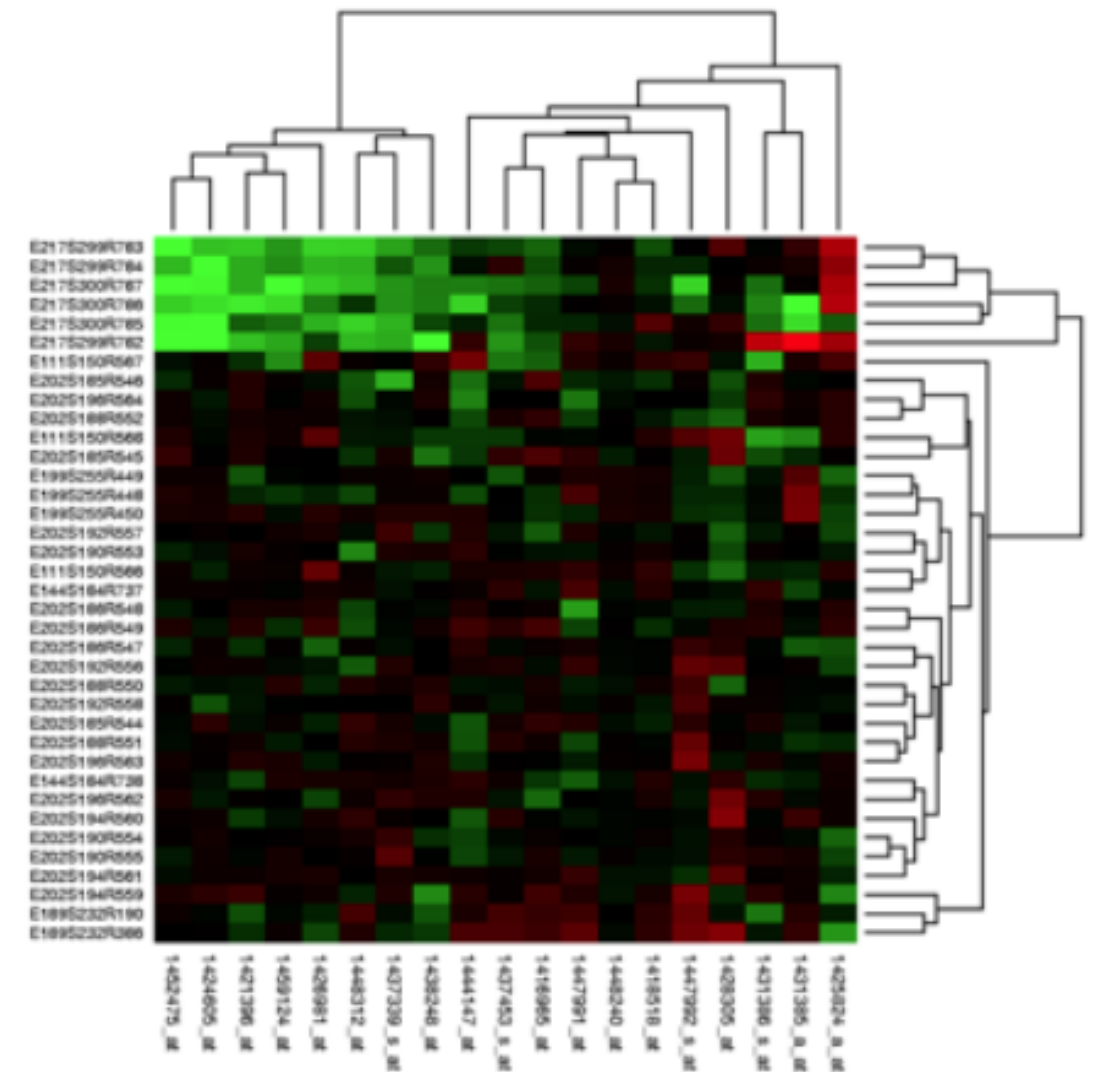
Idiom: **heatmap**

- two keys, one value
 - data
 - 2 categ attribs (gene, experimental condition)
 - 1 quant attrib (expression levels)
 - marks: area
 - separate and align in 2D matrix
 - indexed by 2 categorical attributes
 - channels
 - color by quant attrib
 - (ordered diverging colormap)
 - task
 - find clusters, outliers
 - scalability
 - 1M items, 100s of categ levels, ~10 quant attrib levels



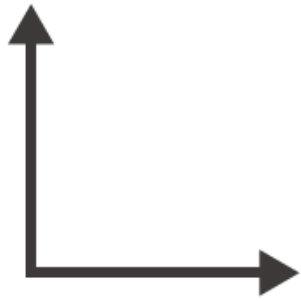
Idiom: **cluster heatmap**

- in addition
 - derived data
 - 2 cluster hierarchies
 - dendrogram
 - Parent-child relationships in tree with connection line mar
 - Leaces aligned so interior branch heights easy to compare
 - heatmap
 - Marks (re-)ordered by cluster hierarchy traversed

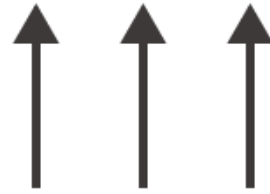


➔ **Axis Orientation**

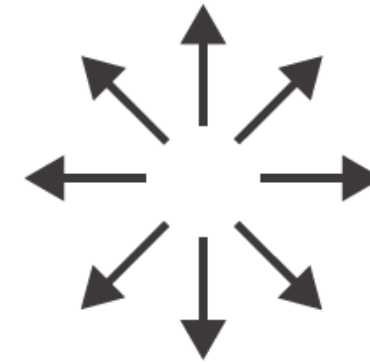
➔ Rectilinear



➔ Parallel

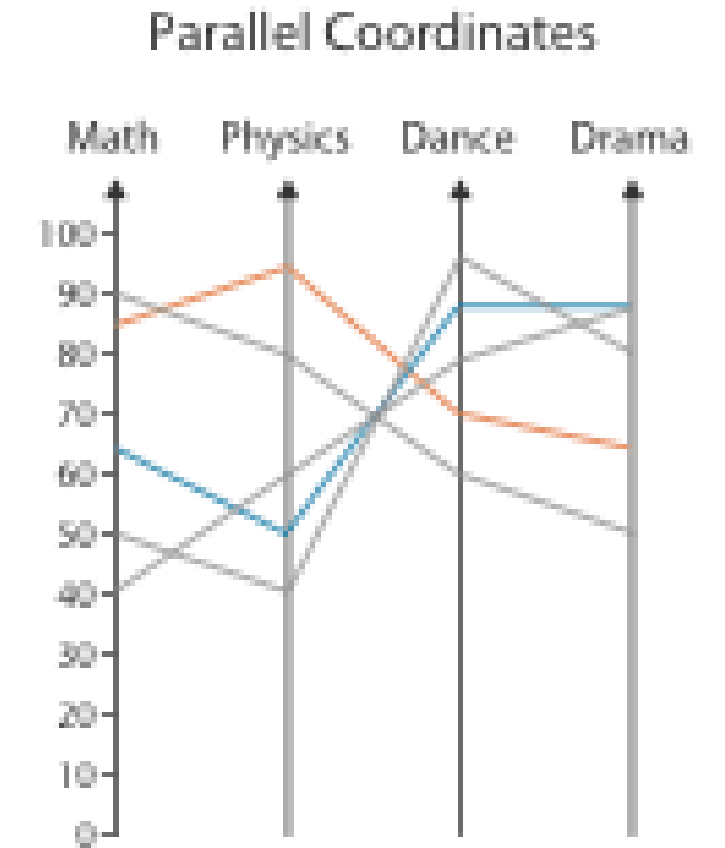
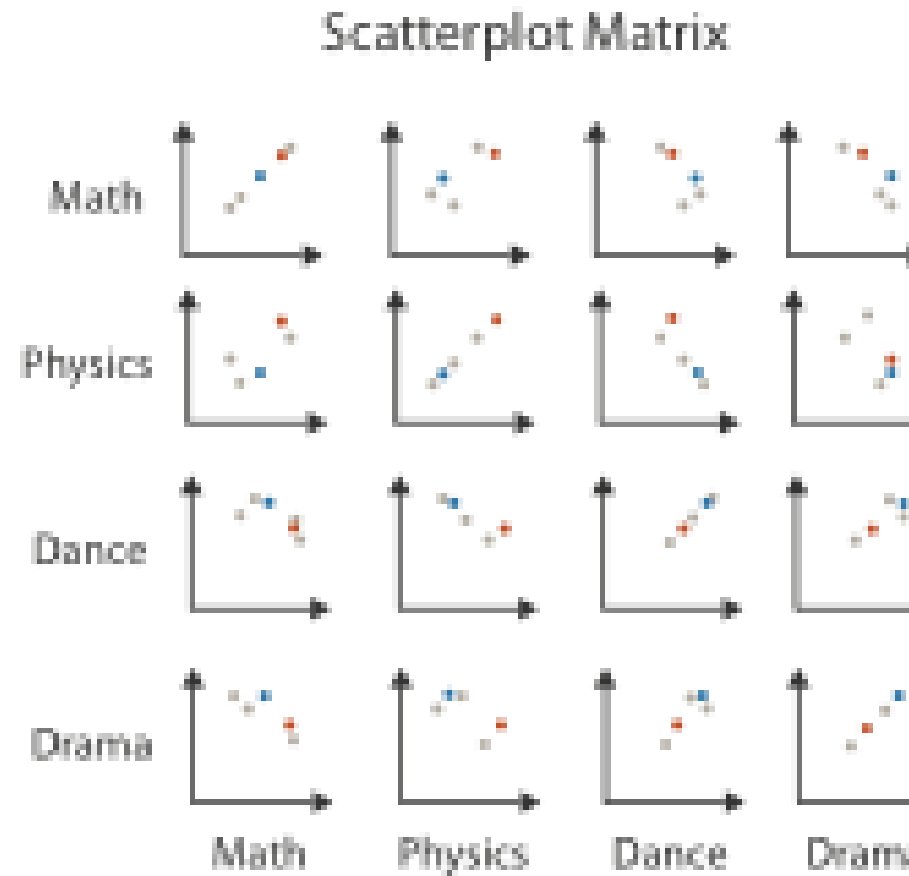


➔ Radial



Idioms: **scatterplot matrix**, **parallel coordinates**

- scatterplot matrix (SPLOM)
 - rectilinear axes, point mark
 - all possible pairs of axes
 - scalability
 - one dozen attribs
 - dozens to hundreds of items
- parallel coordinates
 - parallel axes, jagged line representing item
 - rectilinear axes, item as point
 - axis ordering is major challenge
 - scalability
 - dozens of attribs
 - hundreds of items

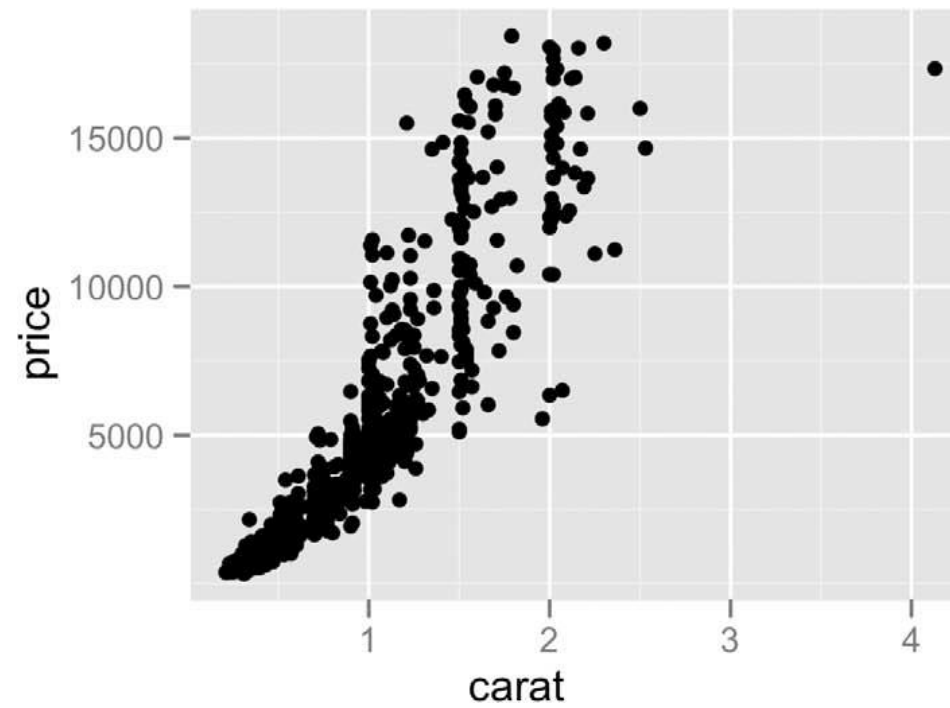


Table

| Math | Physics | Dance | Drama |
|------|---------|-------|-------|
| 85 | 95 | 70 | 65 |
| 90 | 80 | 60 | 50 |
| 65 | 50 | 90 | 90 |
| 50 | 40 | 95 | 80 |
| 40 | 60 | 80 | 90 |

Task: Correlation

- scatterplot matrix
 - positive correlation
 - diagonal low-to-high
 - negative correlation
 - diagonal high-to-low
 - uncorrelated
- parallel coordinates
 - positive correlation
 - parallel line segments
 - negative correlation
 - all segments cross at halfway point
 - uncorrelated
 - scattered crossings



[A layered grammar of graphics. Wickham. Journ. Computational and Graphical Statistics 19:1 (2010), 3 – 28.]

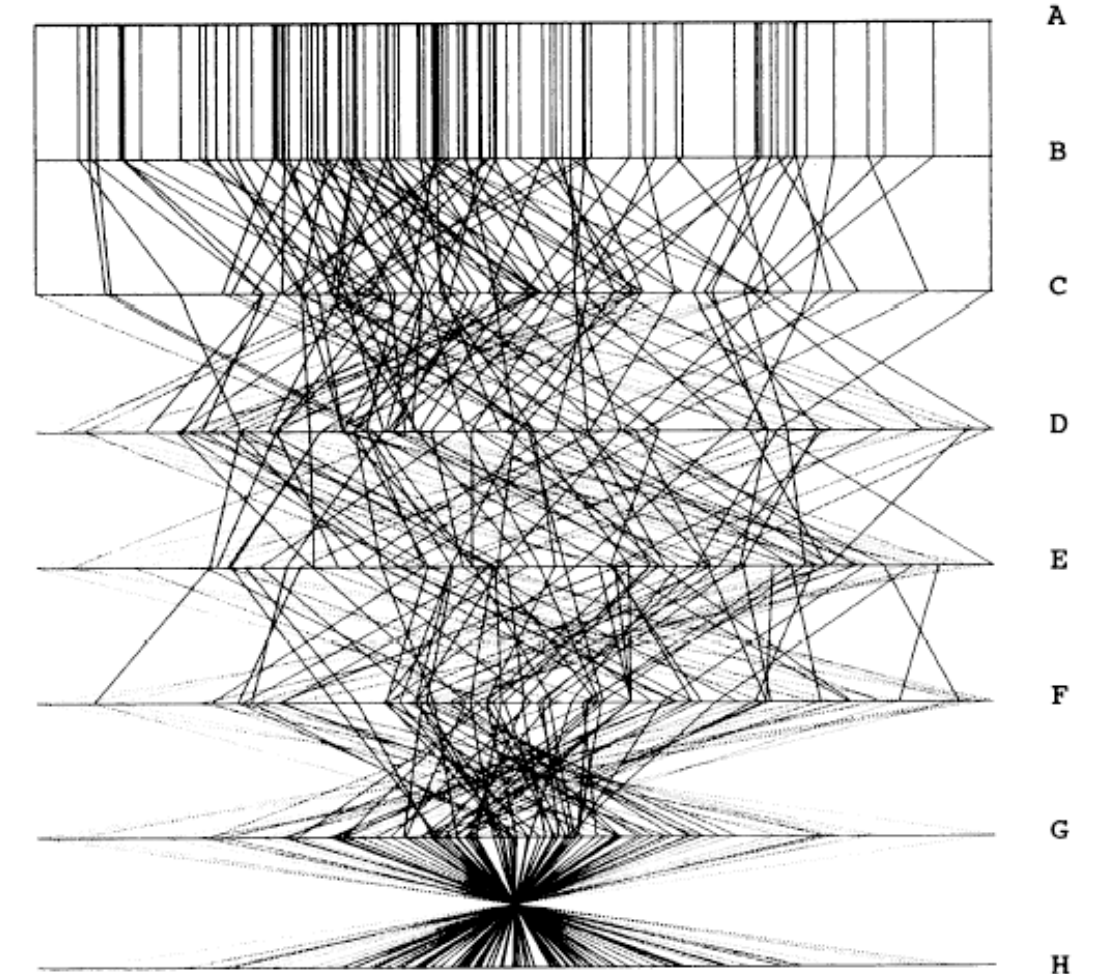
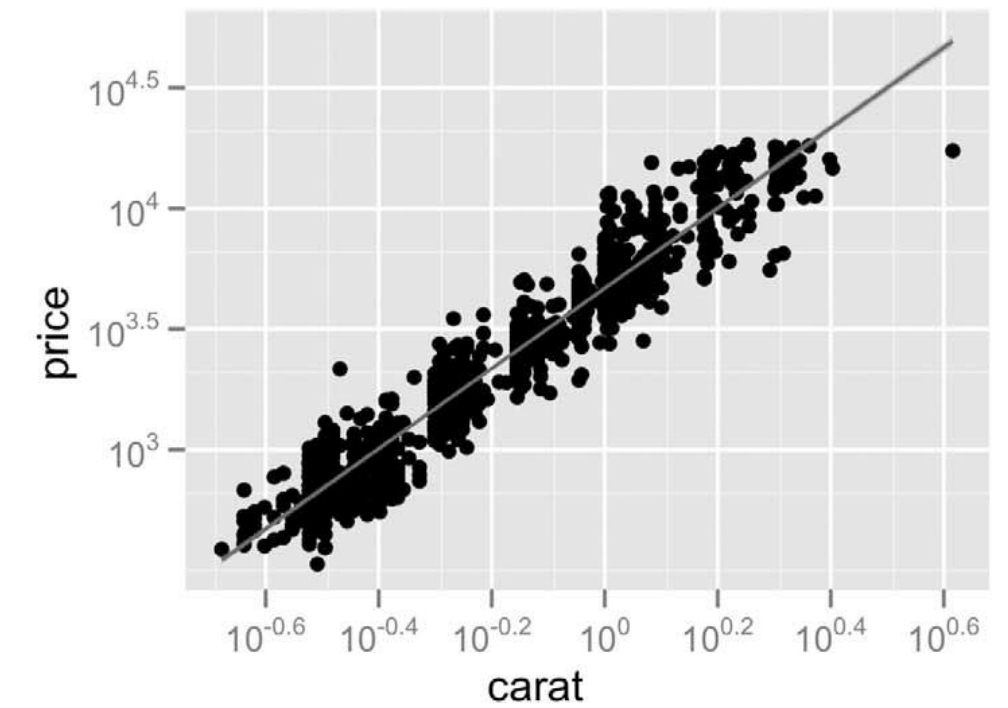
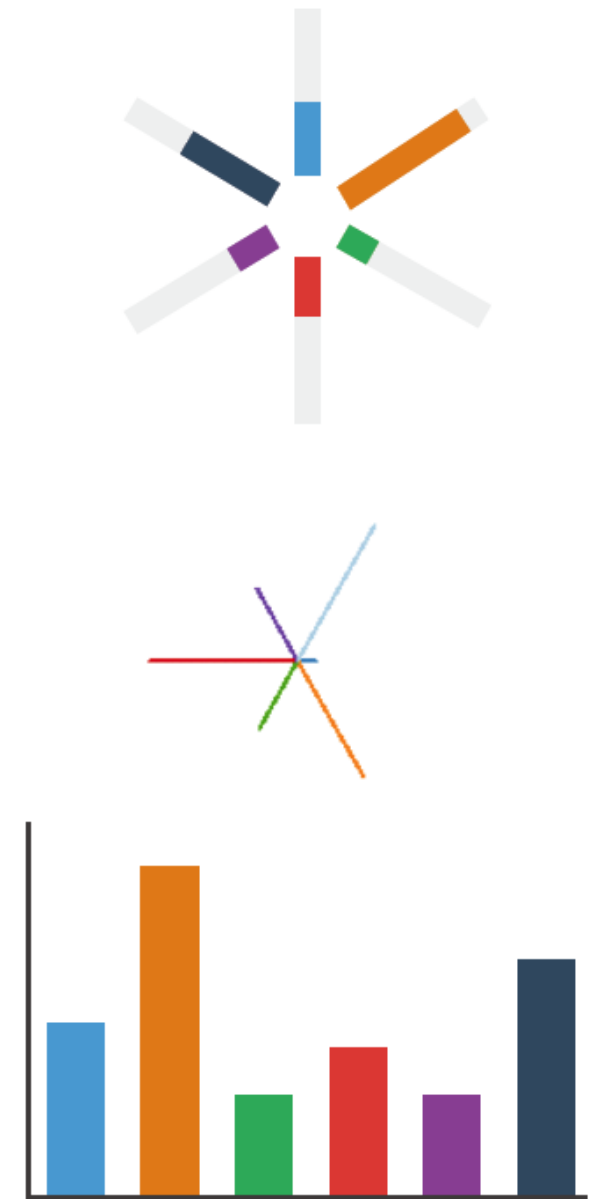


Figure 3. Parallel Coordinate Plot of Six-Dimensional Data Illustrating Correlations of $\rho = 1, .8, .2, 0, -.2, -.8$, and -1 .

[Hyperdimensional Data Analysis Using Parallel Coordinates. Wegman. Journ. American Statistical Association 85:411 (1990), 664 – 675.]

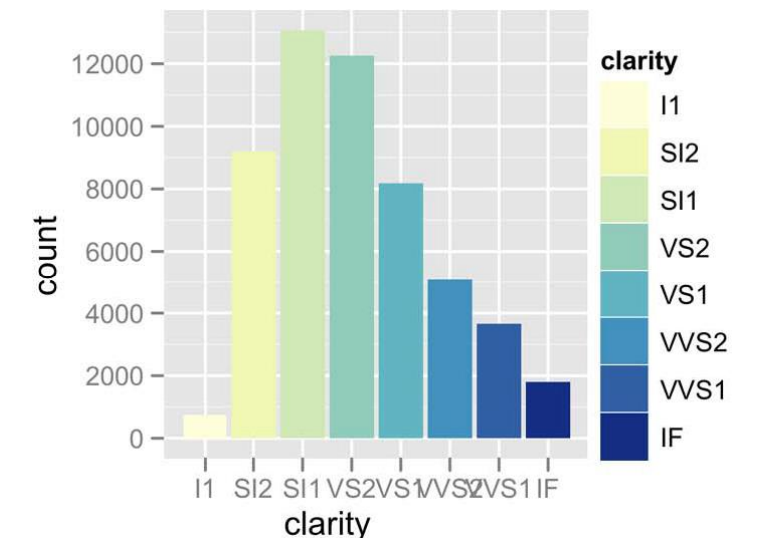
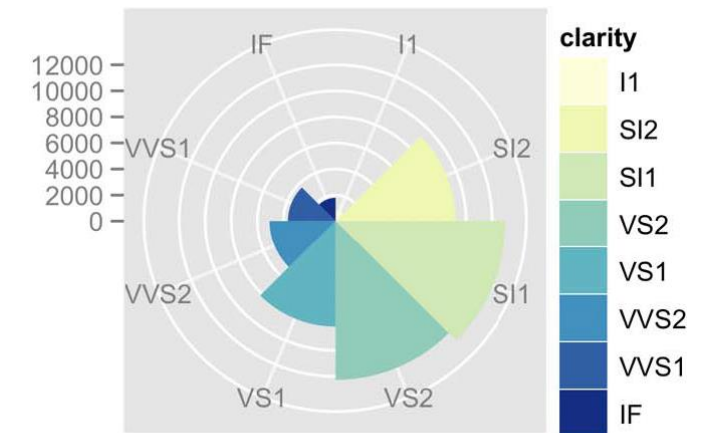
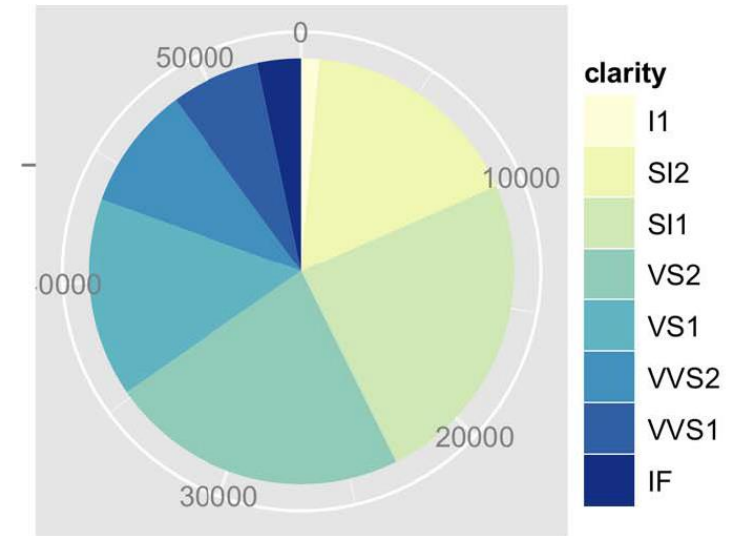
Idioms: **radial bar chart**, **star plot**

- radial bar chart
 - radial axes meet at central ring, line mark
- star plot
 - radial axes, meet at central point, line mark
- bar chart
 - rectilinear axes, aligned vertically
 - less accurate than aligned with radial



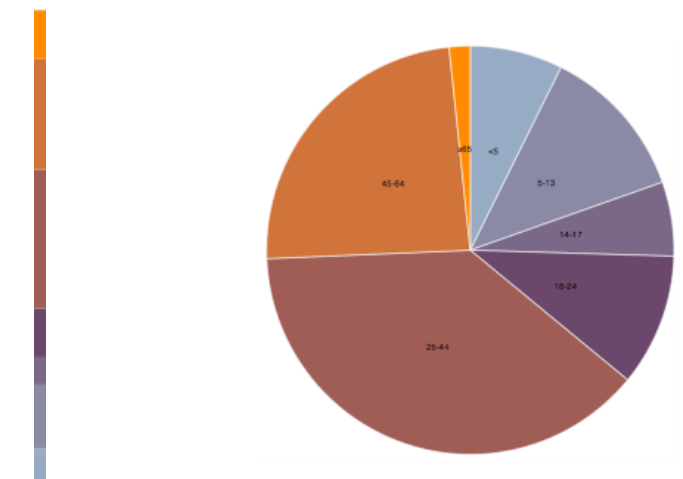
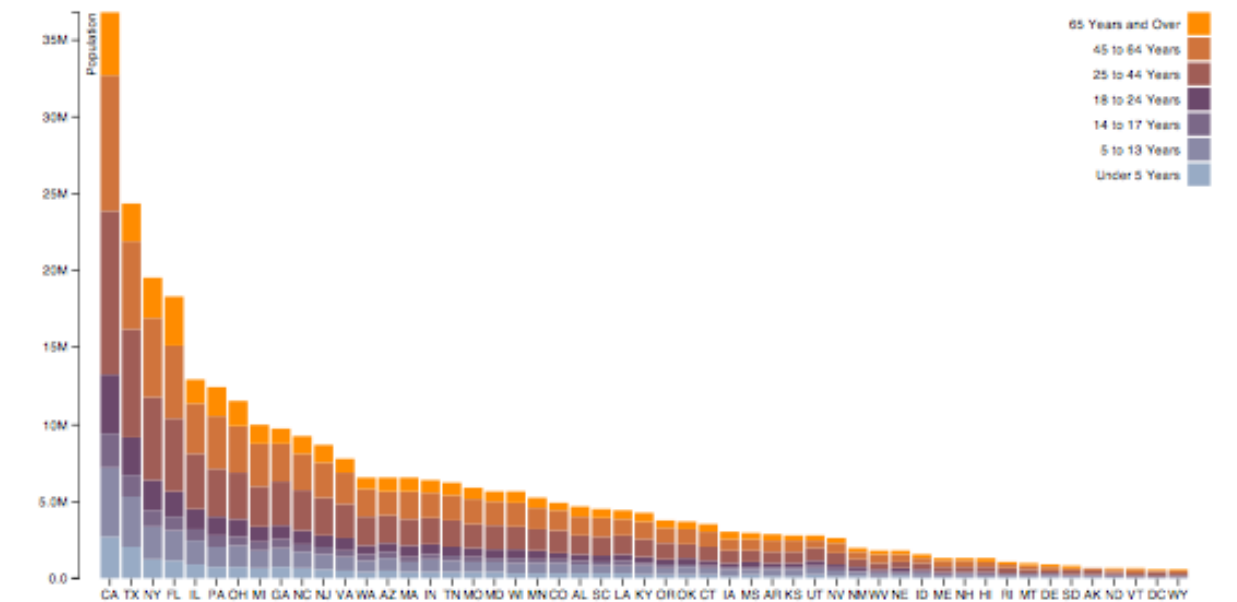
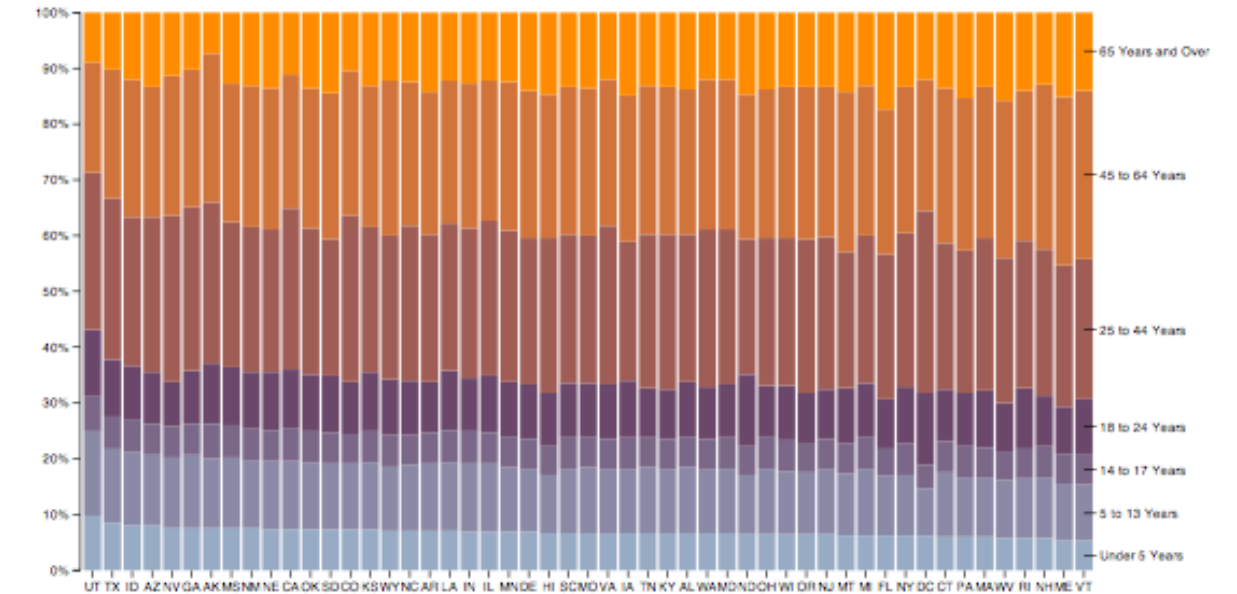
Idioms: **pie chart**, **polar area chart**

- pie chart
 - area marks with angle channel
 - accuracy: angle/area less accurate than line length
 - arclength also less accurate than line length
- polar area chart
 - area marks with length channel
 - more direct analog to bar charts
- data
 - 1 categ key attrib, 1 quant value attrib
- task
 - part-to-whole judgements



Idioms: **normalized stacked bar chart**

- task
 - part-to-whole judgements
- normalized stacked bar chart
 - stacked bar chart, normalized to full vert height
 - single stacked bar equivalent to full pie
 - high information density: requires narrow rectangle
- pie chart
 - information density: requires large circle



<http://bl.ocks.org/mbostock/3887235>,

<http://bl.ocks.org/mbostock/3886208>,

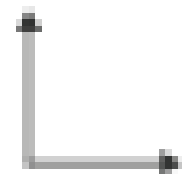
<http://bl.ocks.org/mbostock/3886394>.

Idiom: **glyphmaps**

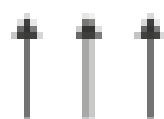
- rectilinear good for linear vs nonlinear trends
- radial good for cyclic patterns

⊕ Axis Orientation

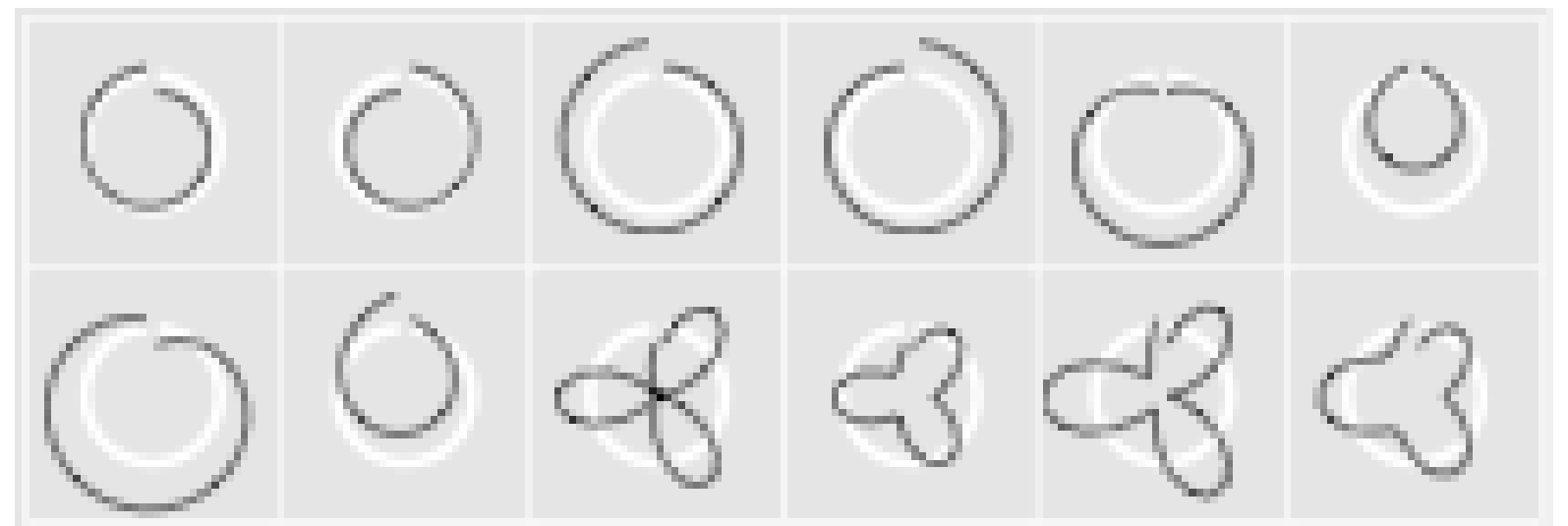
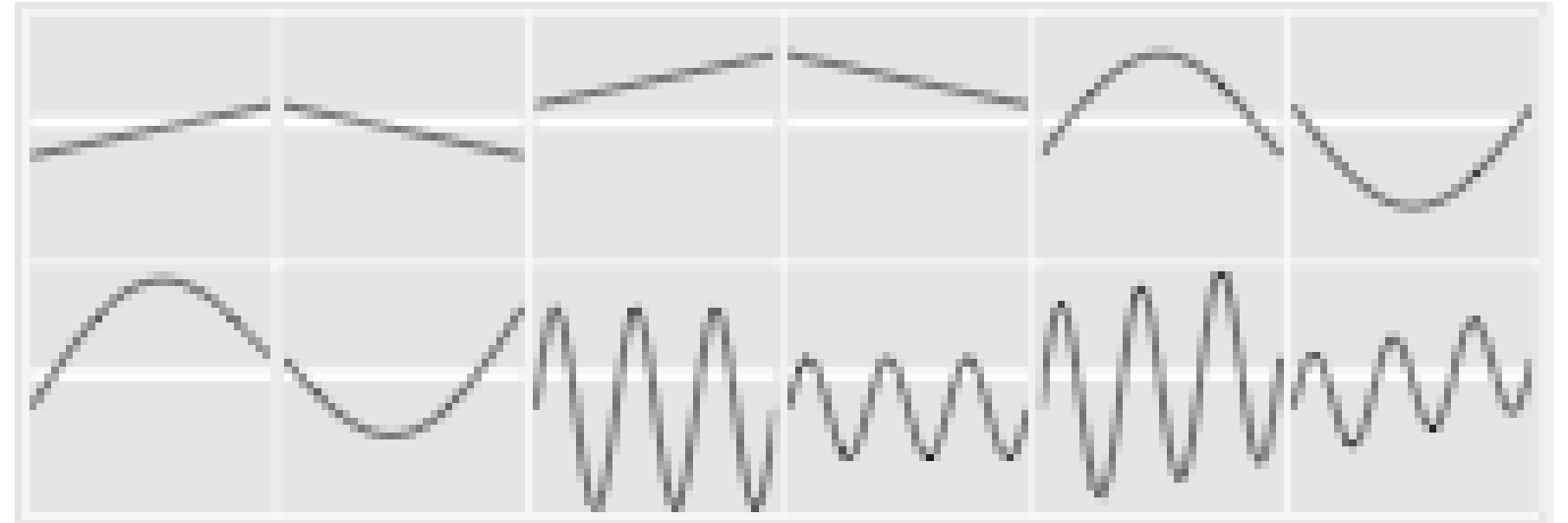
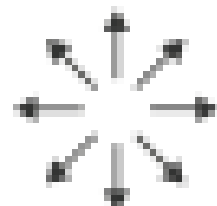
→ Rectilinear



→ Parallel



→ Radial



[Glyph-maps for Visually Exploring Temporal Patterns in Climate Data and Models. Wickham, Hofmann, Wickham, and Cook. Environmetrics 23:5 (2012), 382 – 393.]

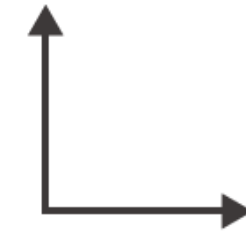
Orientation limitations

- rectilinear: scalability wrt #axes
 - 2 axes best
 - 3 problematic
 - more in afternoon
 - 4+ impossible
- parallel: unfamiliarity, training time
- radial: perceptual limits
 - angles lower precision than lengths
 - asymmetry between angle and length
 - can be exploited!

*[Uncovering Strengths and Weaknesses of Radial Visualizations
- an Empirical Approach. Diehl, Beck and Burch. IEEE TVCG
(Proc. InfoVis) 16(6):935--942, 2010.]*

➔ Axis Orientation

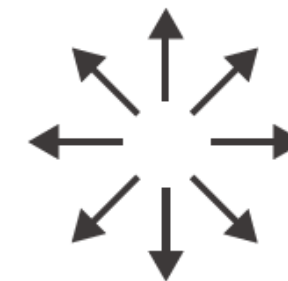
➔ Rectilinear



➔ Parallel

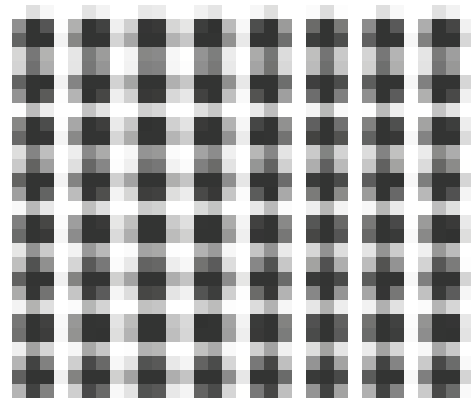


➔ Radial

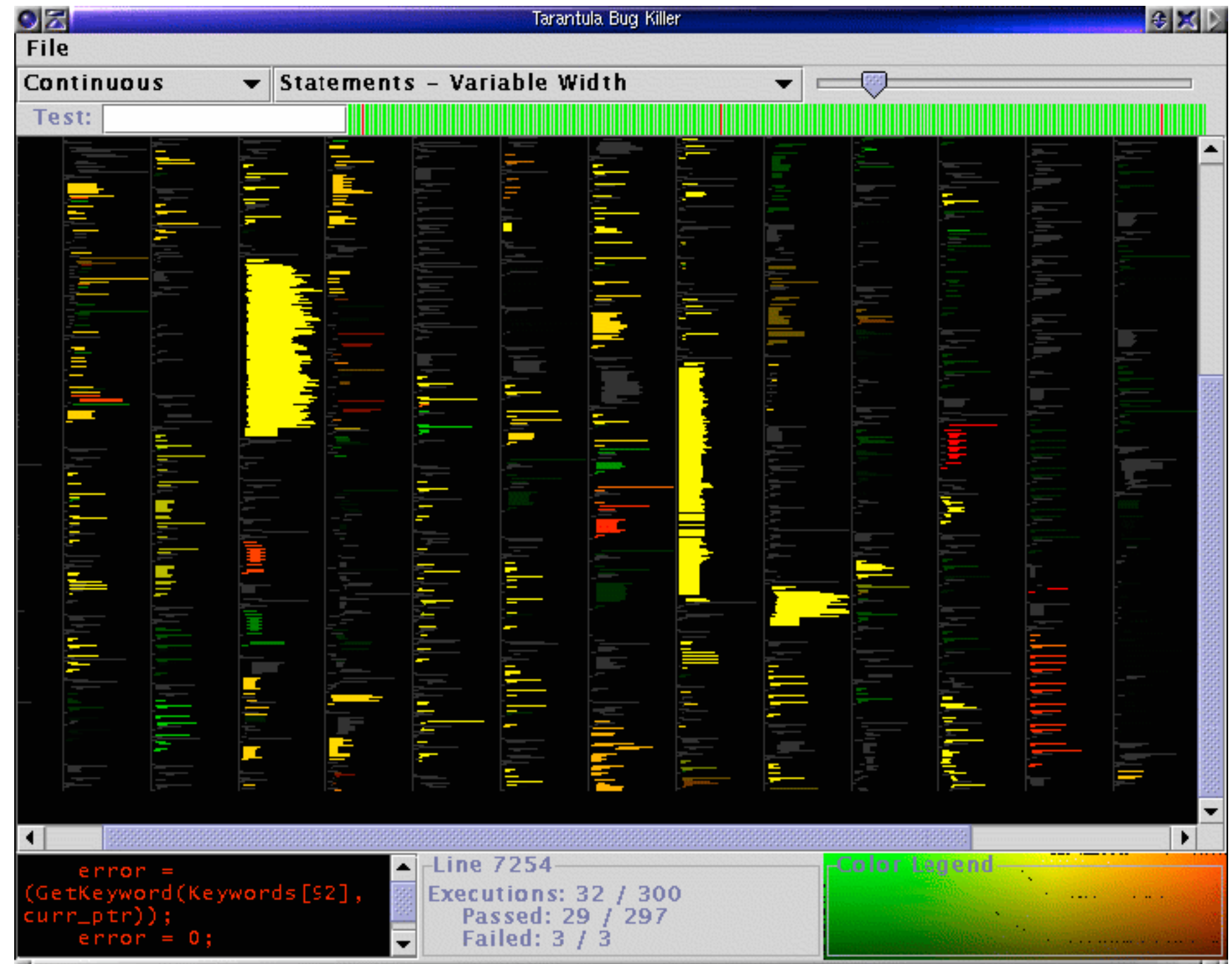


Layout Density

→ Dense



dense software overviews



Further reading

- Visualization Analysis and Design. Munzner. AK Peters Visualization Series, CRC Press, 2014.
 - *Chap 7: Arrange Tables*
- Visualizing Data. Cleveland. Hobart Press, 1993.
- *A Brief History of Data Visualization*. Friendly. 2008.
<http://www.datavis.ca/milestones>

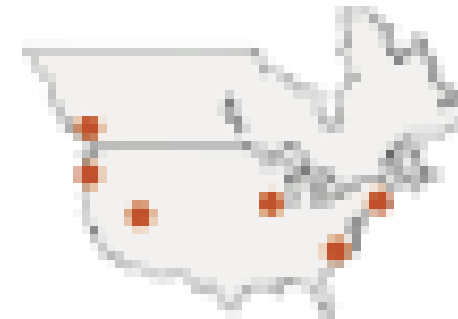
Arrange Spatial Data

Arrange spatial data

⊕ Use Given

→ Geometry

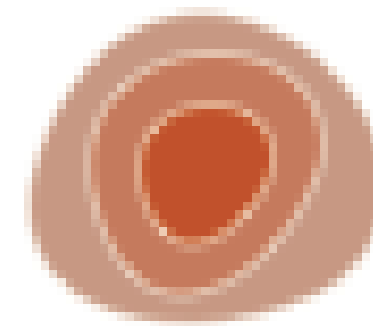
- Geographic
- Other Derived



→ Spatial Fields

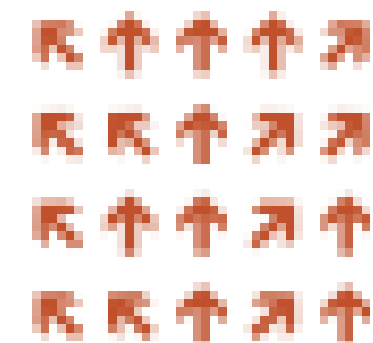
→ Scalar Fields (one value per cell)

- + Isocontours
- + Direct Volume Rendering



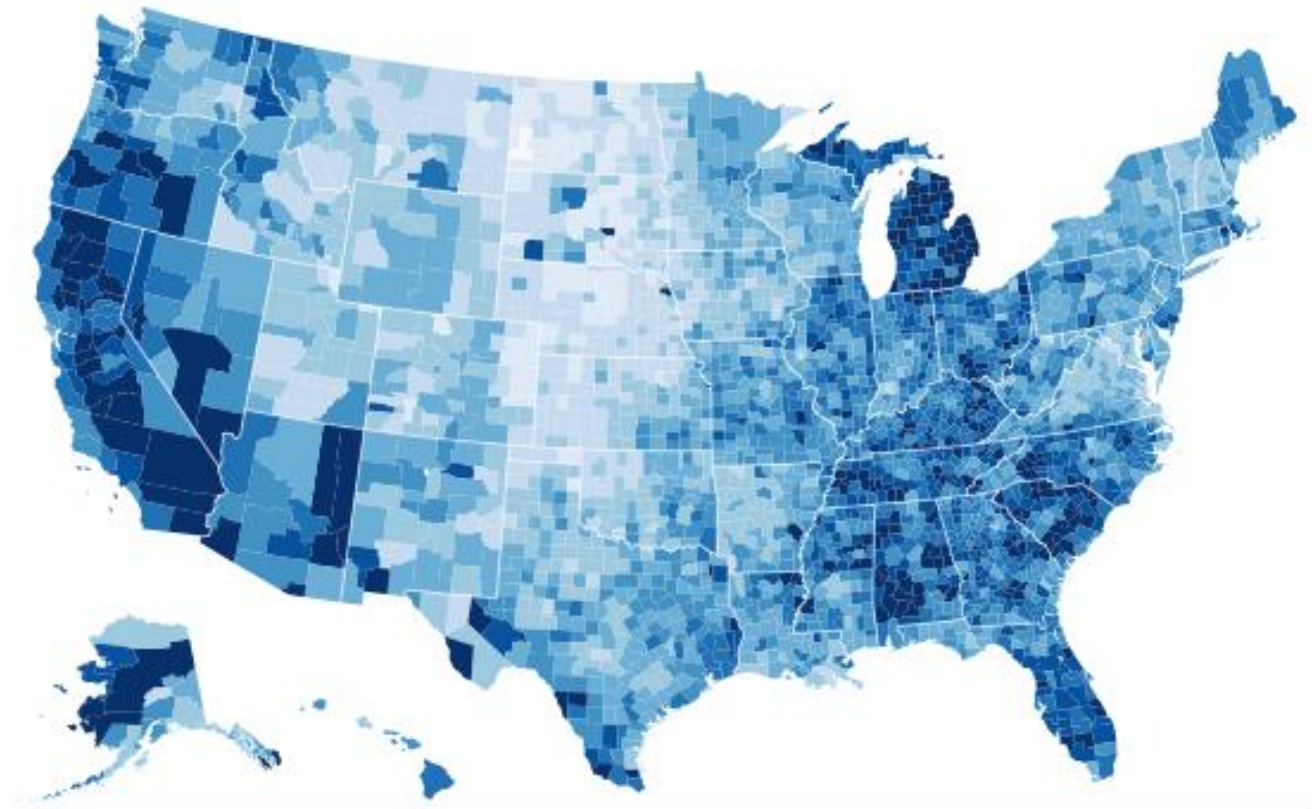
→ Vector and Tensor Fields (many values per cell)

- + Flow Glyphs (local)
- + Geometric (sparse seeds)
- + Textures (dense seeds)
- + Features (globally derived)



Idiom: **choropleth map**

- *use* given spatial data
 - when central task is understanding spatial relationships
- data
 - geographic geometry
 - table with 1 quant attribute per region
- encoding
 - use given geometry for area mark boundaries
 - sequential segmented colormap *[more later]*



<http://bl.ocks.org/mbostock/4060606>

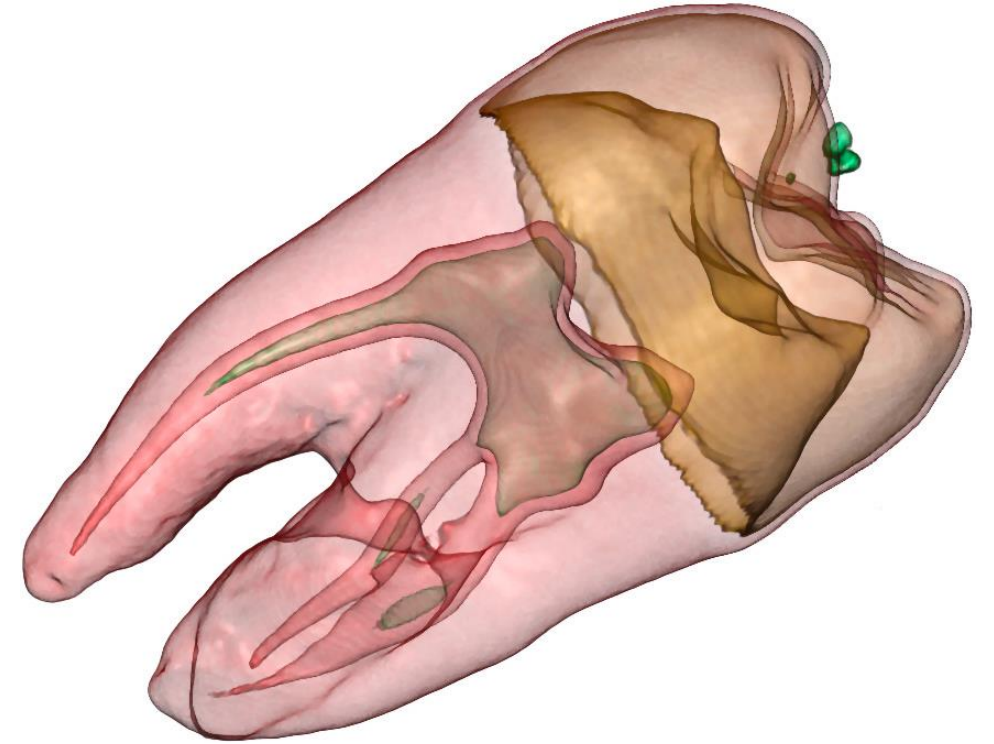
Idiom: **topographic map**

- data
 - geographic geometry
 - scalar spatial field
 - 1 quant attribute per grid cell
- derived data
 - isoline geometry
 - isocontours computed for specific levels of scalar values

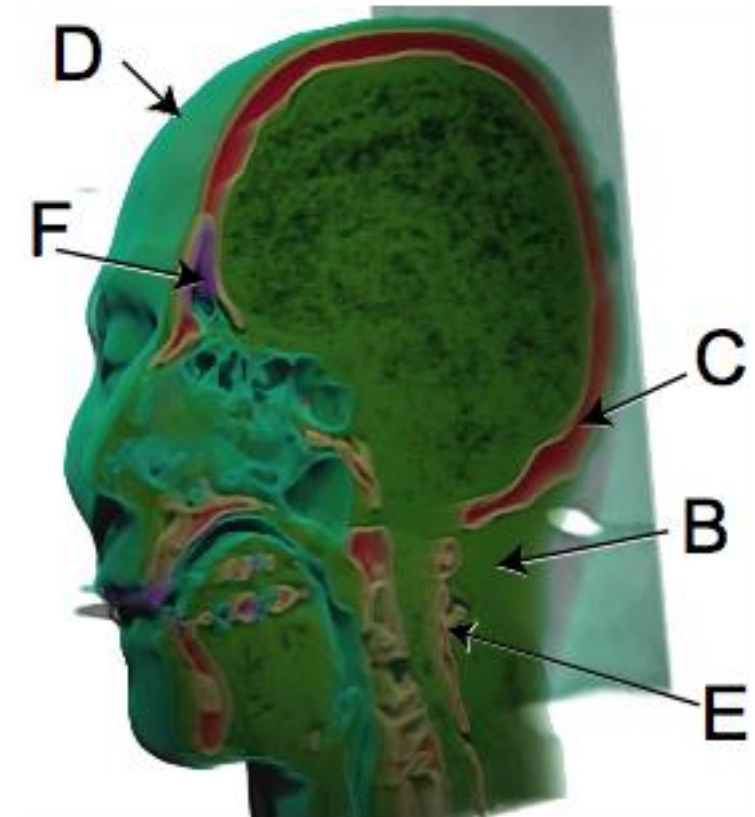


Idioms: **isosurfaces**, **direct volume rendering**

- data
 - scalar spatial field
 - 1 quant attribute per grid cell
- task
 - shape understanding, spatial relationships
- isosurface
 - derived data: isocontours computed for specific levels of scalar values
- direct volume rendering
 - transfer function maps scalar values to color, opacity
 - no derived geometry

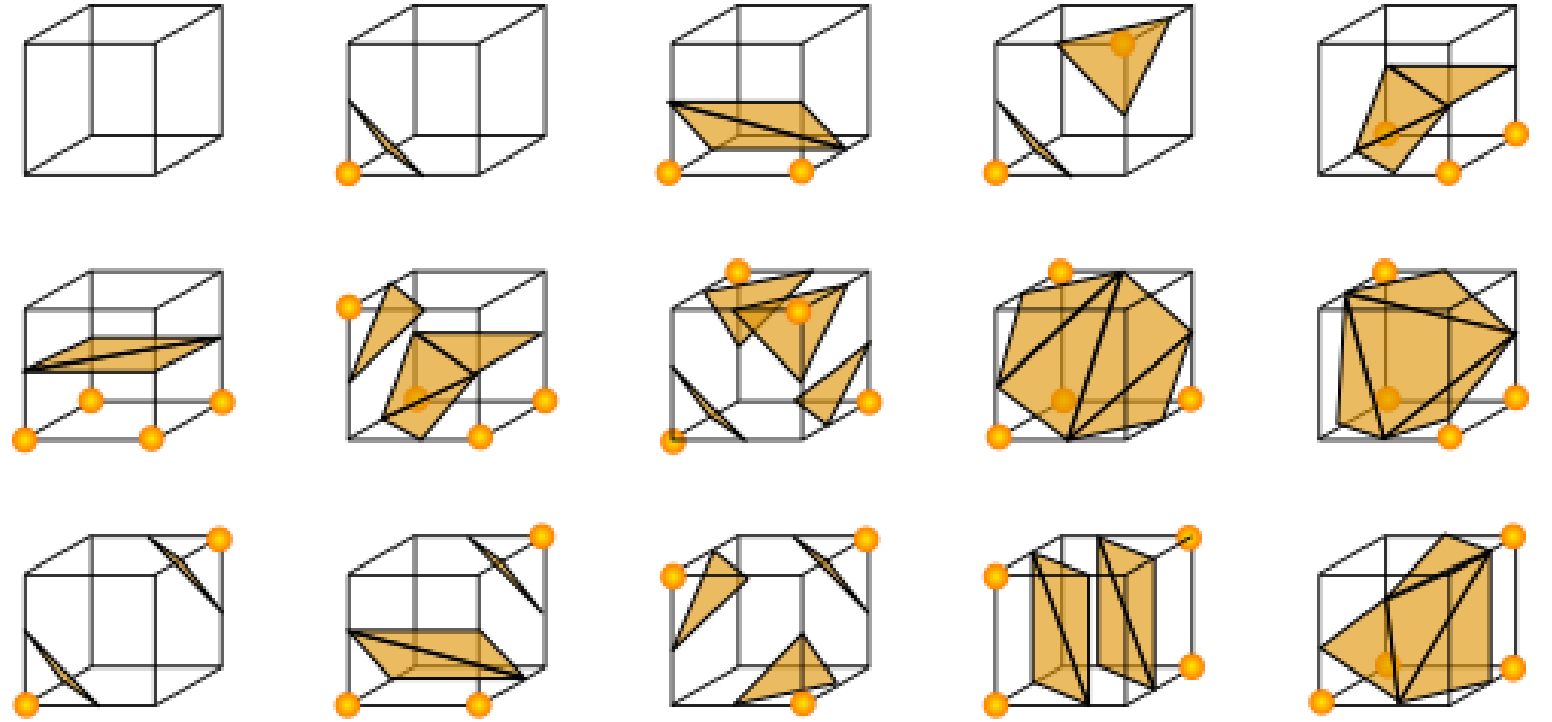


[Interactive Volume Rendering Techniques. Kniss. Master's thesis, University of Utah Computer Science, 2002.]



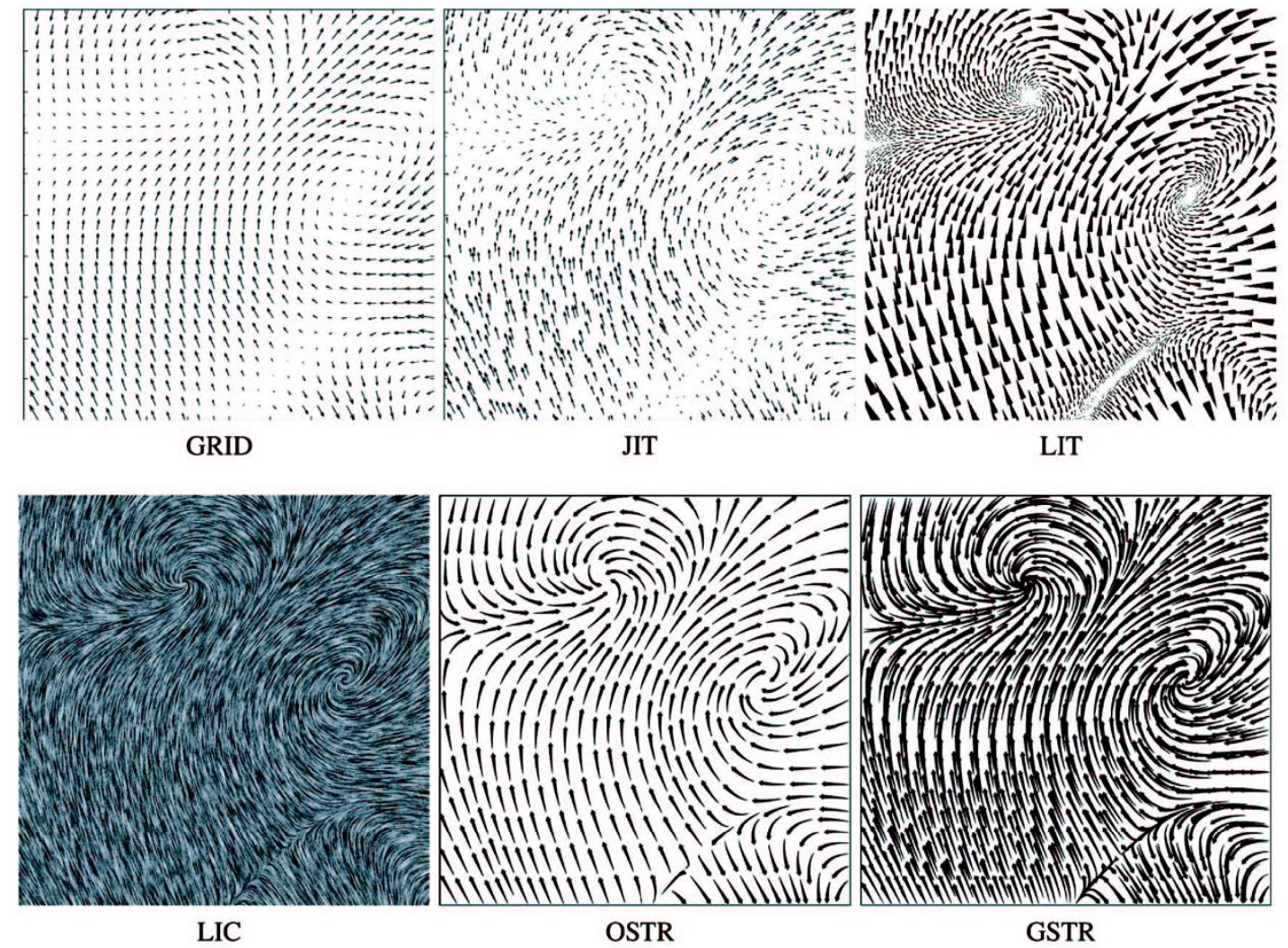
[Multidimensional Transfer Functions for Volume Rendering. Kniss, Kindlmann, and Hansen. In The Visualization Handbook, edited by Charles Hansen and Christopher Johnson, pp. 189 – 210. Elsevier, 2005.]

Marching cubes [1987]

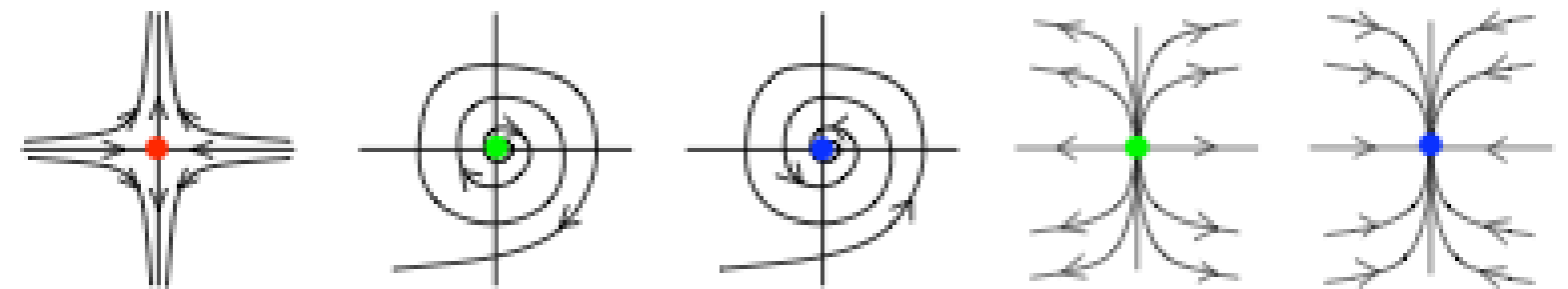


Vector and tensor fields

- data
 - many attribs per cell
- idiom families
 - **flow glyphs**
 - purely local
 - **geometric flow**
 - derived data from tracing particle trajectories
 - sparse set of seed points
 - **texture flow**
 - derived data, dense seeds
 - **feature flow**
 - global computation to detect features
 - encoded with one of methods above



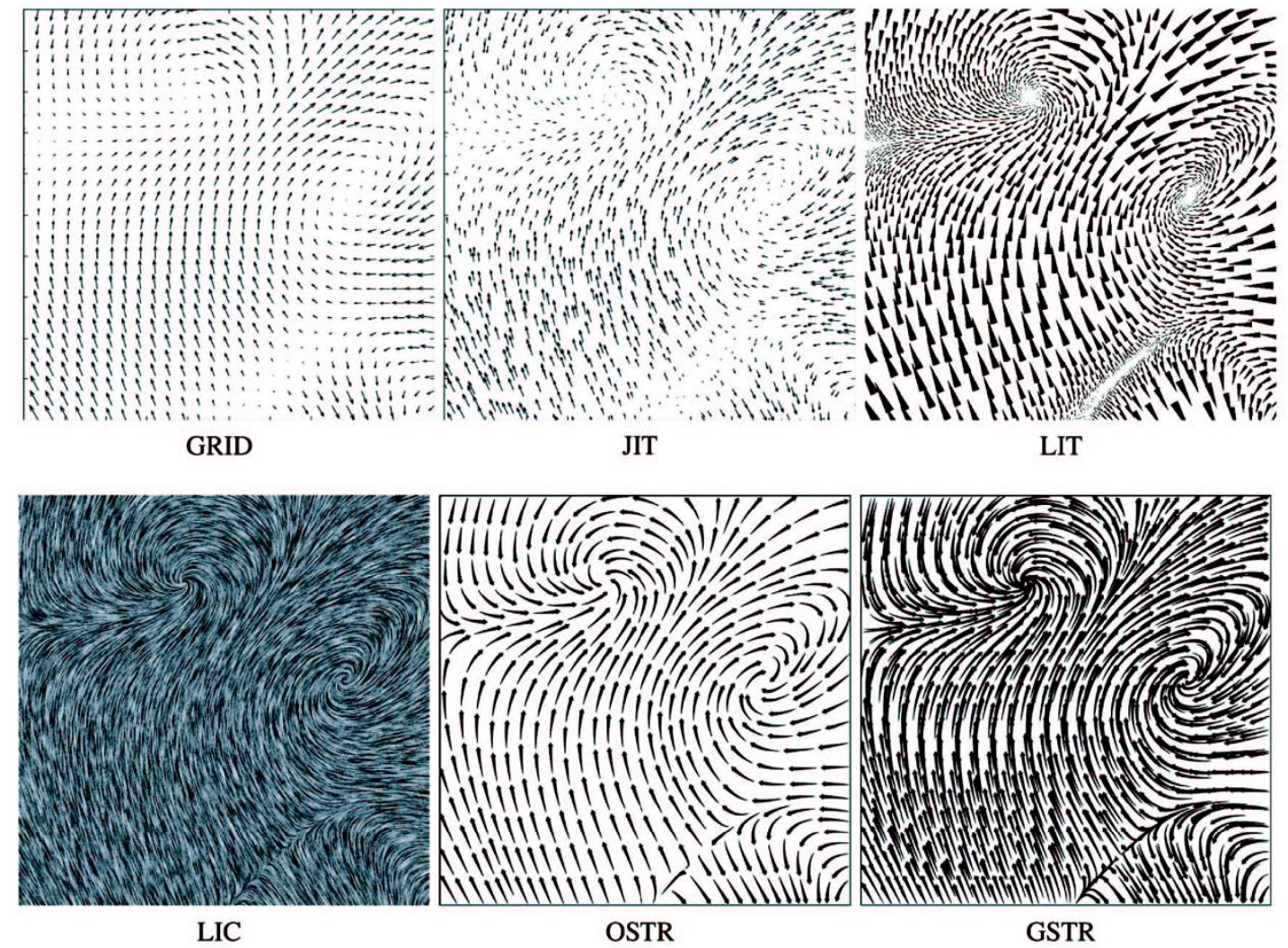
[Comparing 2D vector field visualization methods: A user study. Laidlaw et al. IEEE Trans. Visualization and Computer Graphics (TVCG) 11:1 (2005), 59 – 70.]



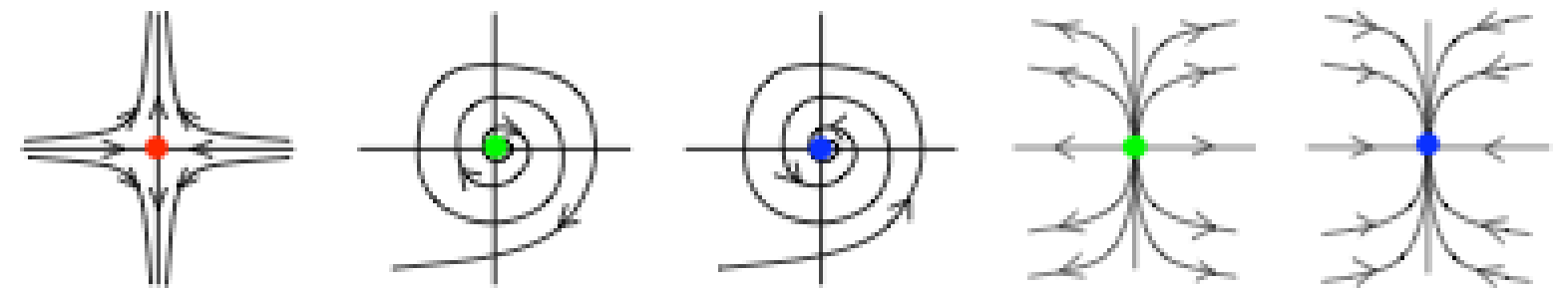
[Topology tracking for the visualization of time-dependent two-dimensional flows. Tricoche, Wischgoll, Scheuermann, and Hagen. Computers & Graphics 26:2 (2002), 249 – 257.]

Vector fields

- empirical study tasks
 - finding critical points, identifying their types
 - identifying what type of critical point is at a specific location
 - predicting where a particle starting at a specified point will end up (advection)

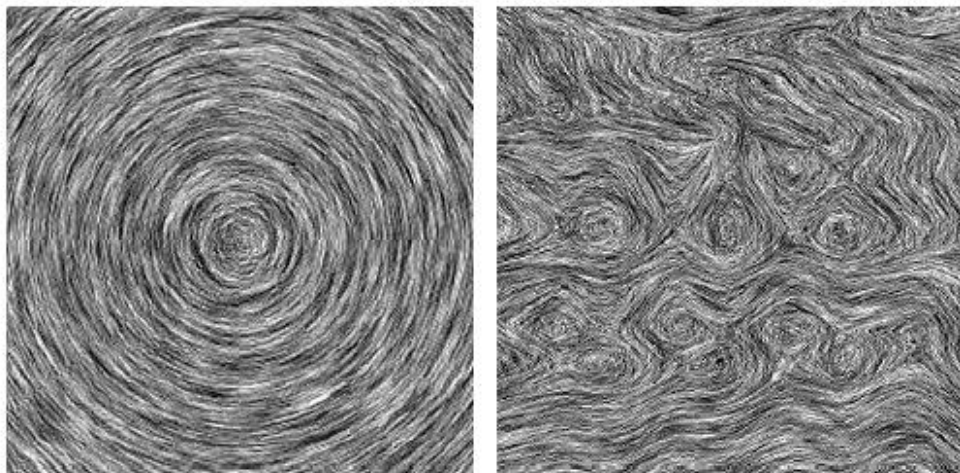
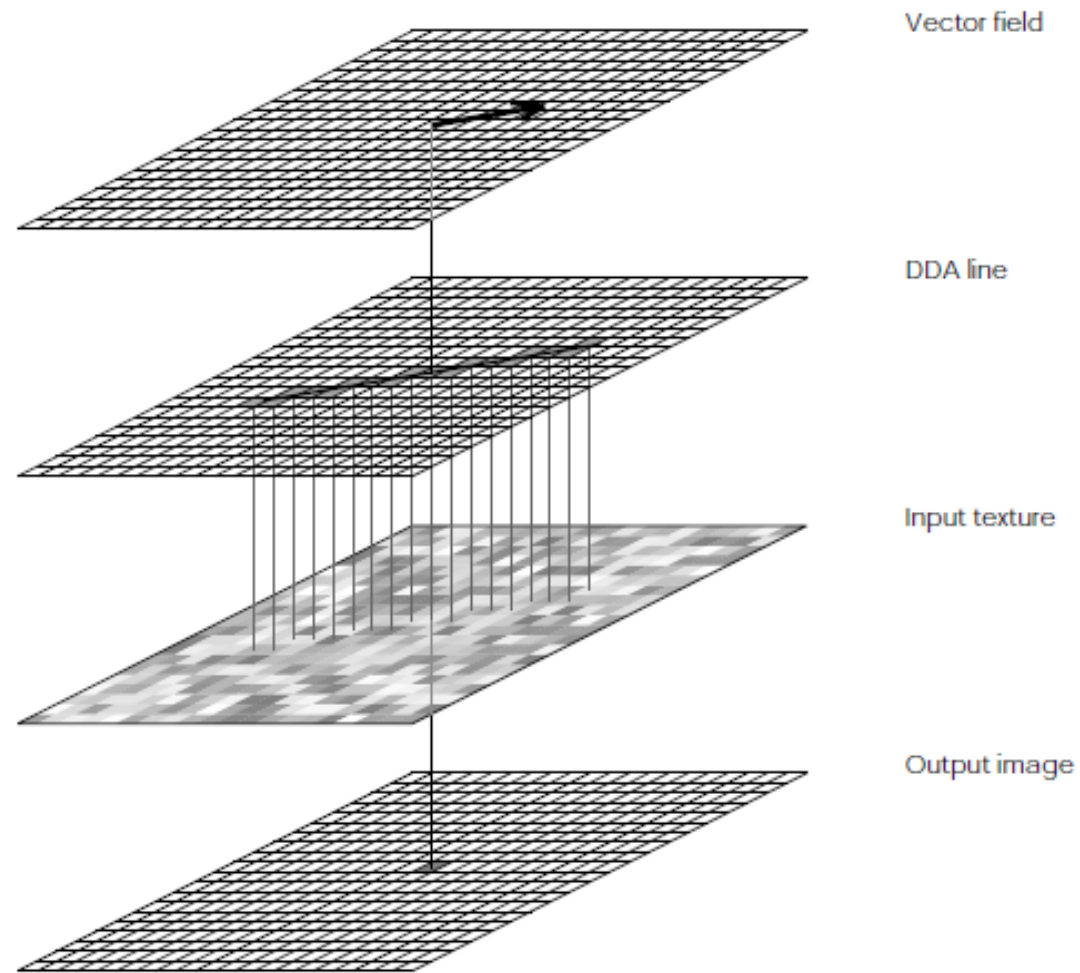


[Comparing 2D vector field visualization methods: A user study. Laidlaw et al. IEEE Trans. Visualization and Computer Graphics (TVCG) 11:1 (2005), 59 – 70.]



[Topology tracking for the visualization of time-dependent two-dimensional flows. Tricoche, Wischgoll, Scheuermann, and Hagen. Computers & Graphics 26:2 (2002), 249 – 257.]

Imaging Vector Fields Using Line Integral Convolution



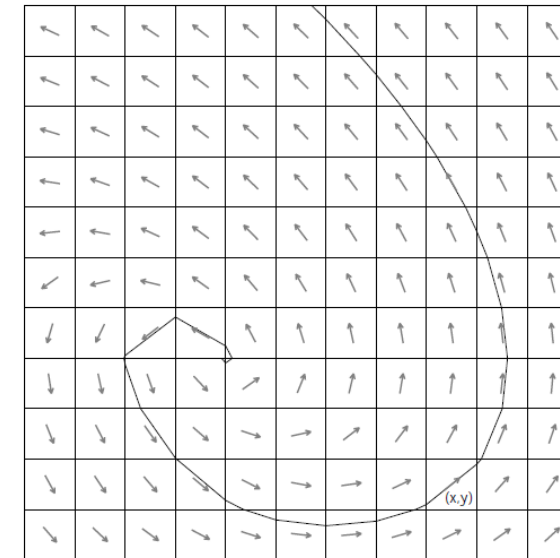
$$P_0 = (x + 0.5, y + 0.5)$$

$$P_i = P_{i-1} + \frac{V(\lfloor P_{i-1} \rfloor)}{\|V(\lfloor P_{i-1} \rfloor)\|} \Delta s_{i-1} \quad (1)$$

$V(\lfloor P \rfloor)$ = the vector from the input vector field at lattice point $(\lfloor P_x \rfloor, \lfloor P_y \rfloor)$

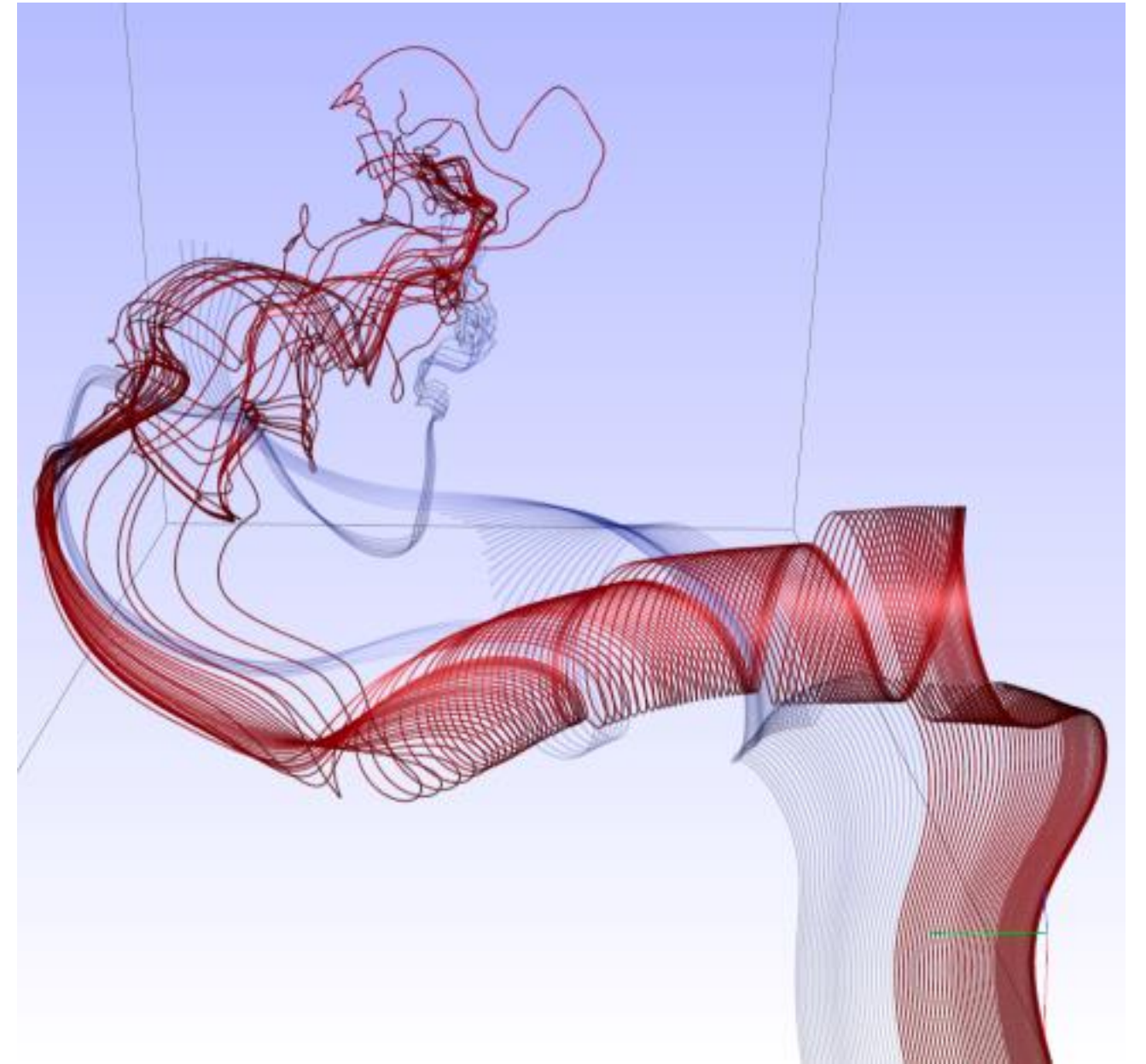
$$s_e = \begin{cases} \infty & \text{if } V \parallel e \\ 0 & \text{if } \frac{\lfloor P_c \rfloor - P_c}{V_c} < 0 \\ \frac{\lfloor P_c \rfloor - P_c}{V_c} & \text{otherwise} \end{cases} \quad \text{for } (e, c) \in \begin{cases} (top, y) \\ (bottom, y) \\ (left, x) \\ (right, x) \end{cases} \quad (2)$$

$$\Delta s_i = \min(s_{top}, s_{bottom}, s_{left}, s_{right})$$



Idiom: **similarity-clustered streamlines**

- data
 - 3D vector field
- derived data (from field)
 - streamlines: trajectory particle will follow
- derived data (per streamline)
 - curvature, torsion, tortuosity
 - signature: complex weighted combination
 - compute cluster hierarchy across all signatures
 - encode: color and opacity by cluster
- tasks
 - find features, query shape
- scalability
 - millions of samples, hundreds of streamlines



*[Similarity Measures for Enhancing Interactive Streamline Seeding.
McLoughlin, Jones, Laramée, Malki, Masters, and Hansen. IEEE Trans.
Visualization and Computer Graphics 19:8 (2013), 1342 – 1353.]*

Further reading

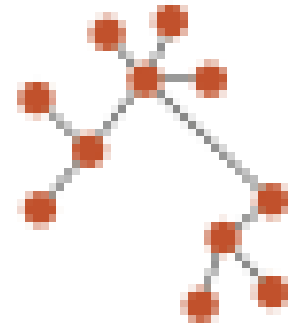
- Visualization Analysis and Design. Munzner. AK Peters Visualization Series, CRC Press, 2014.
 - *Chap 8: Arrange Spatial Data*
- How Maps Work: Representation, Visualization, and Design. MacEachren. Guilford Press, 1995.
- Overview of visualization. Schroeder and. Martin. In The Visualization Handbook, edited by Charles Hansen and Christopher Johnson, pp. 3 – 39. Elsevier, 2005.
- Real-Time Volume Graphics. Engel, Hadwiger, Kniss, Reza-Salama, and Weiskopf. AK Peters, 2006.
- Overview of flow visualization. Weiskopf and Erlebacher. In The Visualization Handbook, edited by Charles Hansen and Christopher Johnson, pp. 261 – 278. Elsevier, 2005.

Arrange Networks and Trees

Arrange networks and trees

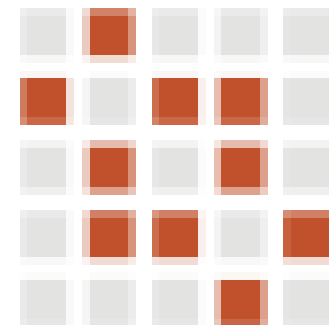
⊕ Node-Link Diagrams Connection Marks

☒ NETWORKS ☒ TREES



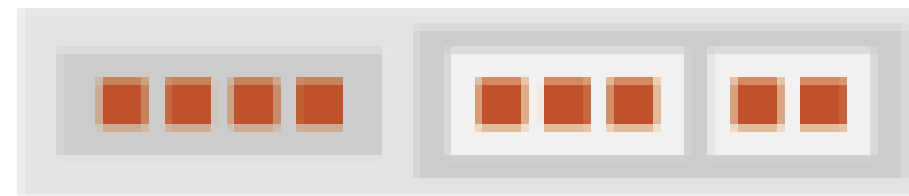
⊕ Adjacency Matrix Derived Table

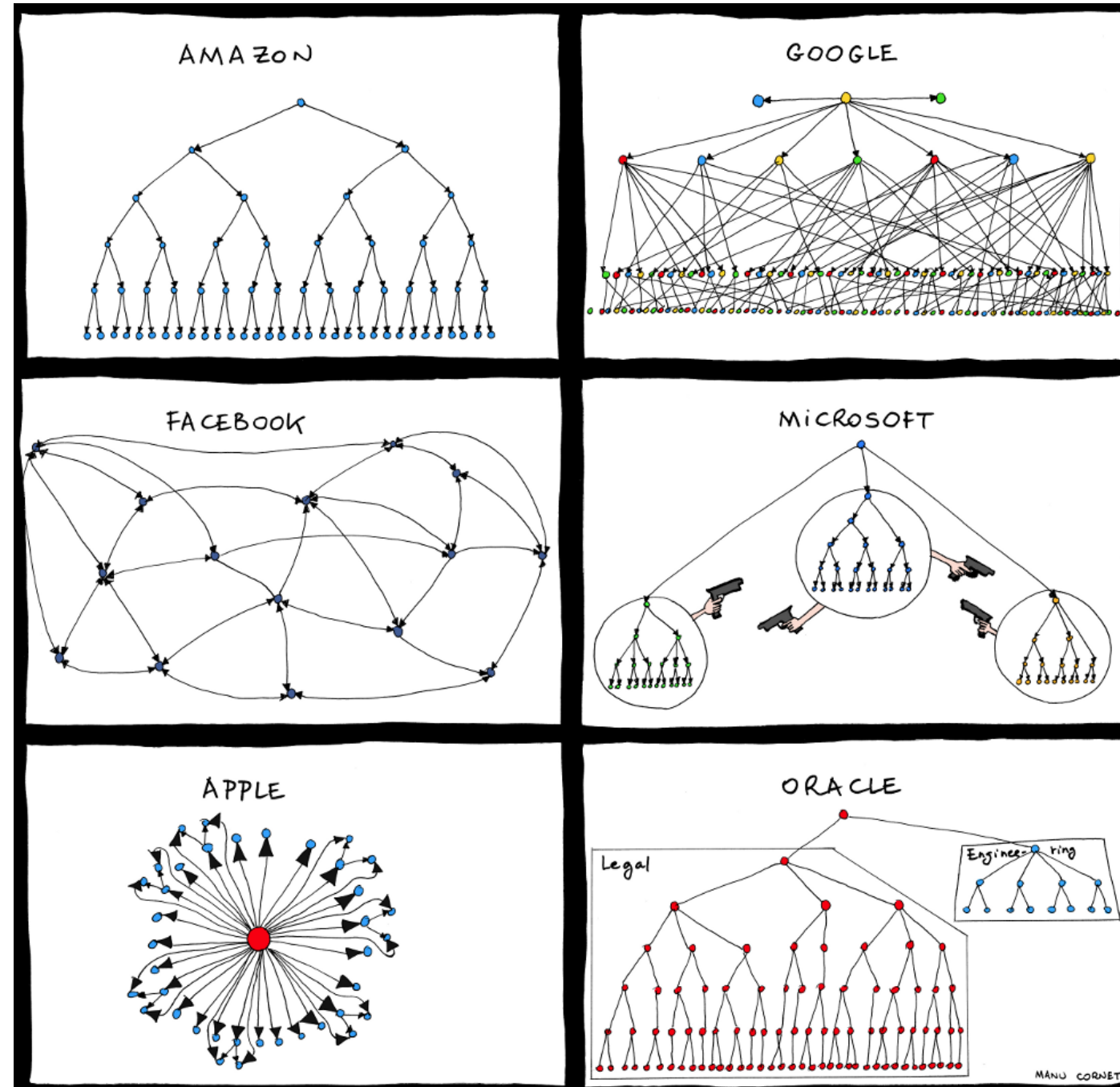
☒ NETWORKS ☒ TREES



⊕ Enclosure Containment Marks

☐ NETWORKS ☒ TREES

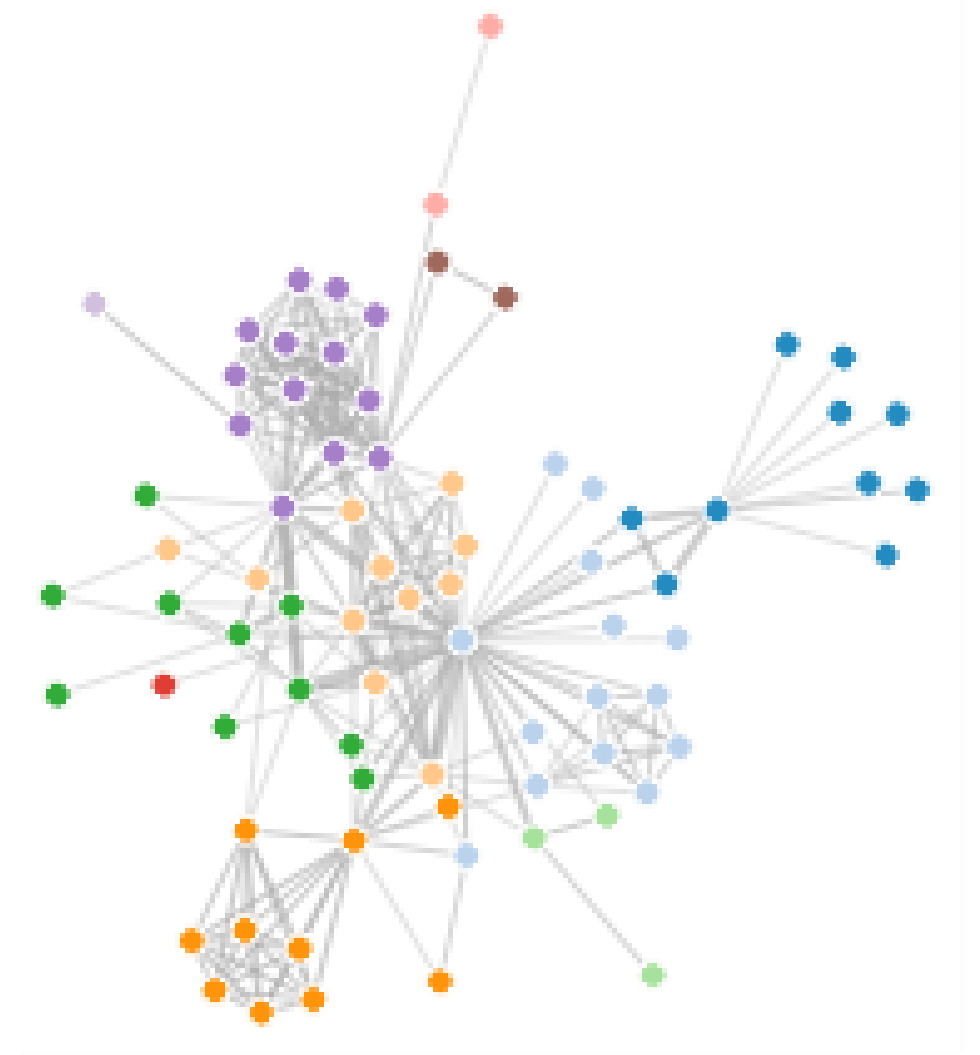




<http://www.bonkersworld.net/organizational-charts/>

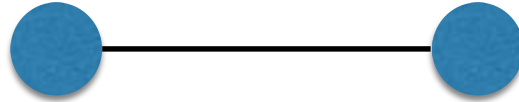
Idiom: **force-directed placement**

- visual encoding
 - link connection marks, node point marks
- considerations
 - spatial position: no meaning directly encoded
 - left free to minimize crossings
 - proximity semantics?
 - sometimes meaningful
 - sometimes arbitrary, artifact of layout algorithm
 - tension with length
 - long edges more visually salient than short
- tasks
 - explore topology; locate paths, clusters
- scalability
 - node/edge density $E < 4N$



- *Spring force*

- $F_{spring} = c_1 \log(\frac{d}{c_2})$



- *force = 0, when $d=c_2$*

- *Repel force for non-adjacent vertex*

- $F_{repeling} = c_3/d^2$

- *Move*

- $c_4 F_{total}$

Spring (G: graph)

Place vertices of G in random locations;

Repeat M times

 calculate the force on each vertex;
 move the vertex;

Draw the graph;

Force-Directed Graph

■ Fruchterman和Reingold[1991]

Even vertex distribution

$$k = \sqrt{\frac{\textit{area}}{\textit{number of vertices}}}$$

$$\Delta = v.pos - u.pos, \text{ for each node } u, v$$

attractive

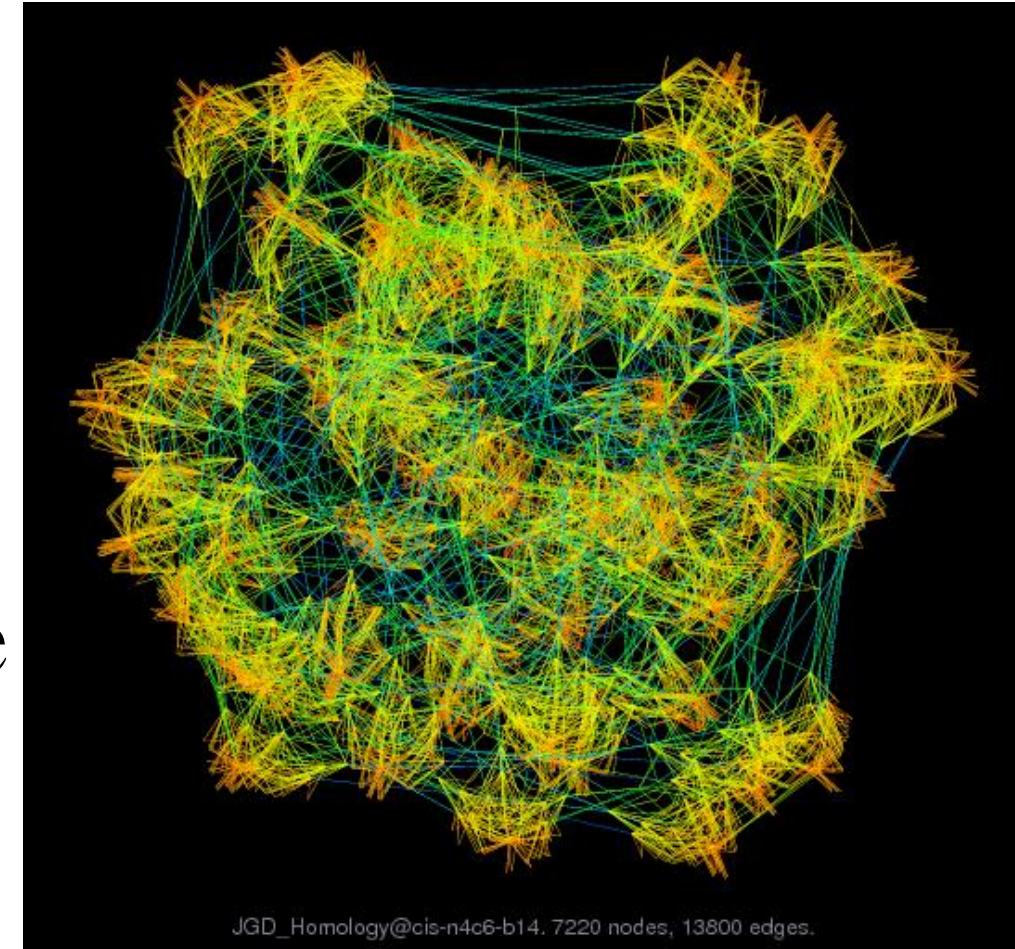
$$f_a(\Delta) = \frac{\Delta^2}{k}$$

repulsive

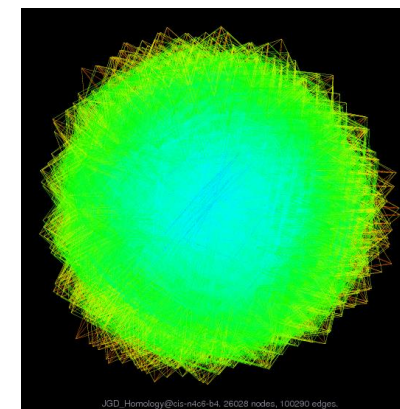
$$f_r(\Delta) = \frac{k^2}{\Delta}$$

Idiom: **sfdp** (multi-level scalable force-directed placement)

- data
 - original: network
 - derived: cluster hierarchy atop it
- considerations
 - better algorithm for same encoding technique
 - same: fundamental use of space
 - hierarchy used for algorithm speed/quality but not shown explicitly
 - (more on algorithm vs encoding in afternoon)
- scalability
 - nodes, edges: 1K-10K
 - hairball problem eventually hits



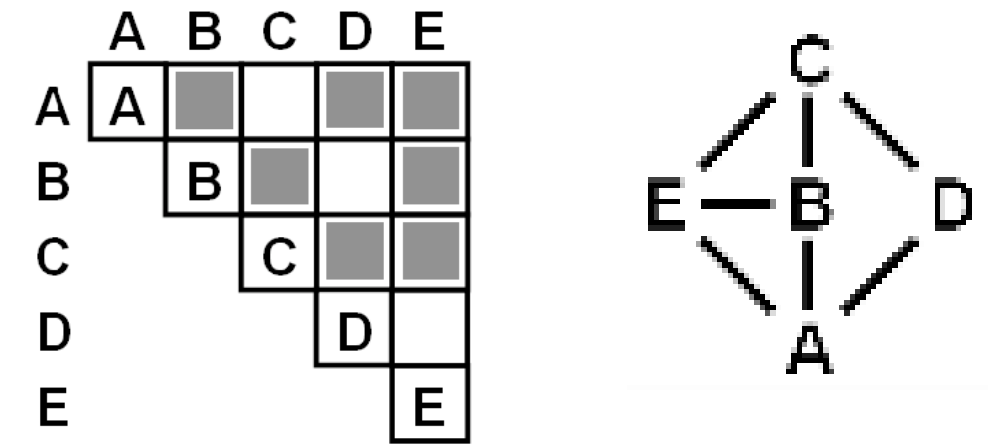
*[Efficient and high quality force-directed graph drawing.
Hu. The Mathematica Journal 10:37 – 71, 2005.]*



26,020 nodes and 100,290 edges

Idiom: **adjacency matrix view**

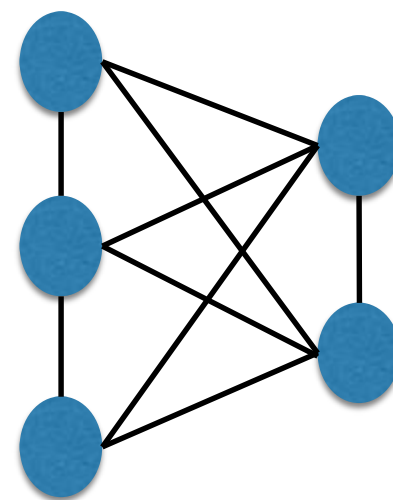
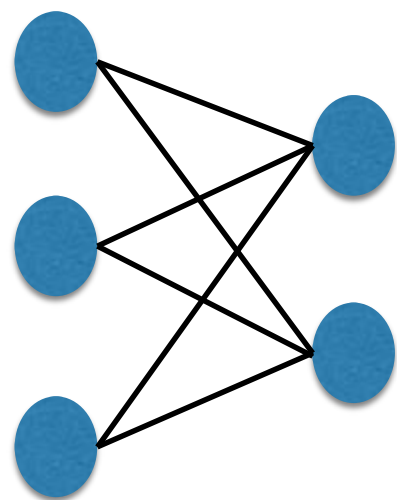
- data: network
 - transform into same data/encoding as heatmap
- derived data: table from network
 - 1 quant attrib
 - weighted edge between nodes
 - 2 categ attribs: node list x 2
- visual encoding
 - cell shows presence/absence of edge
- scalability
 - 1K nodes, 1M edges



[NodeTrix: a Hybrid Visualization of Social Networks. Henry, Fekete, and McGuffin. IEEE TVCG (Proc. InfoVis) 13(6):1302-1309, 2007.]



[Points of view: Networks. Gehlenborg and Wong. Nature Methods 9:115.]



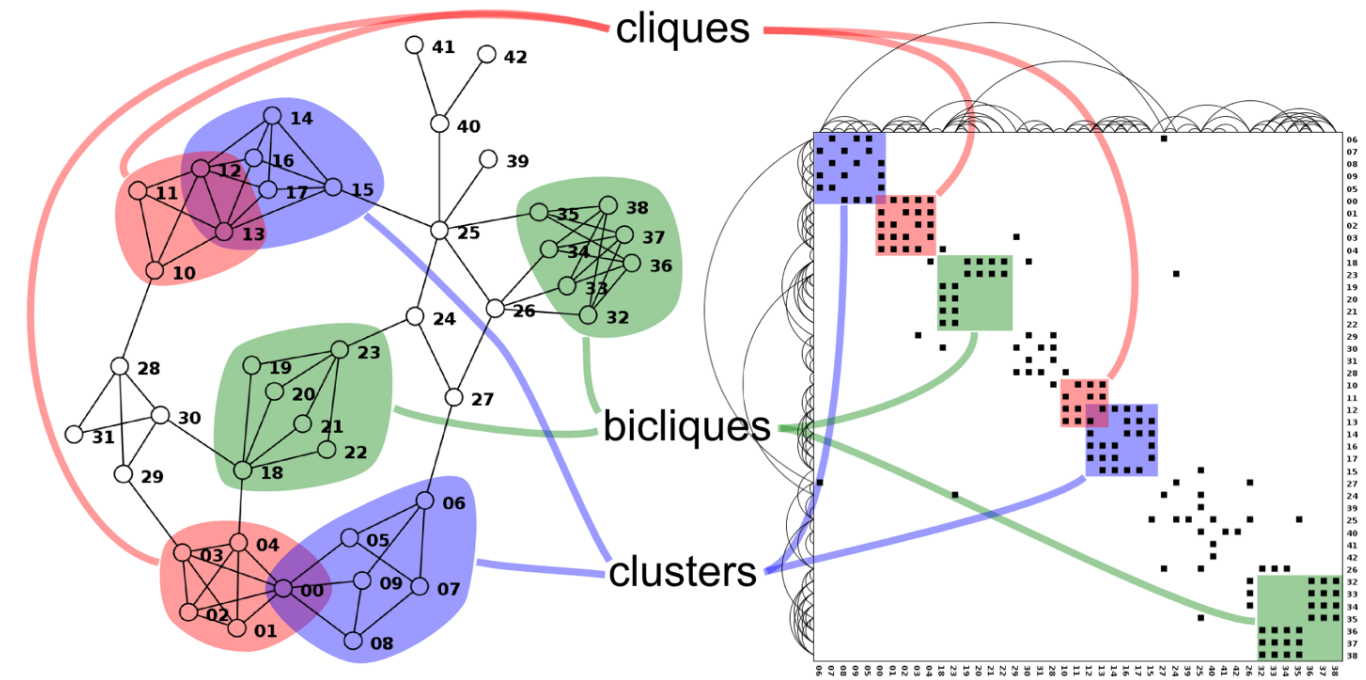
Connection vs. adjacency comparison

- adjacency matrix strengths
 - predictability, scalability, supports reordering
 - some topology tasks trainable
- node-link diagram strengths
 - topology understanding, path tracing
 - intuitive, no training needed
- empirical study
 - node-link best for small networks
 - matrix best for large networks

- if tasks don't involve topological structure!

[On the readability of graphs using node-link and matrix-based representations: a controlled experiment and statistical analysis.

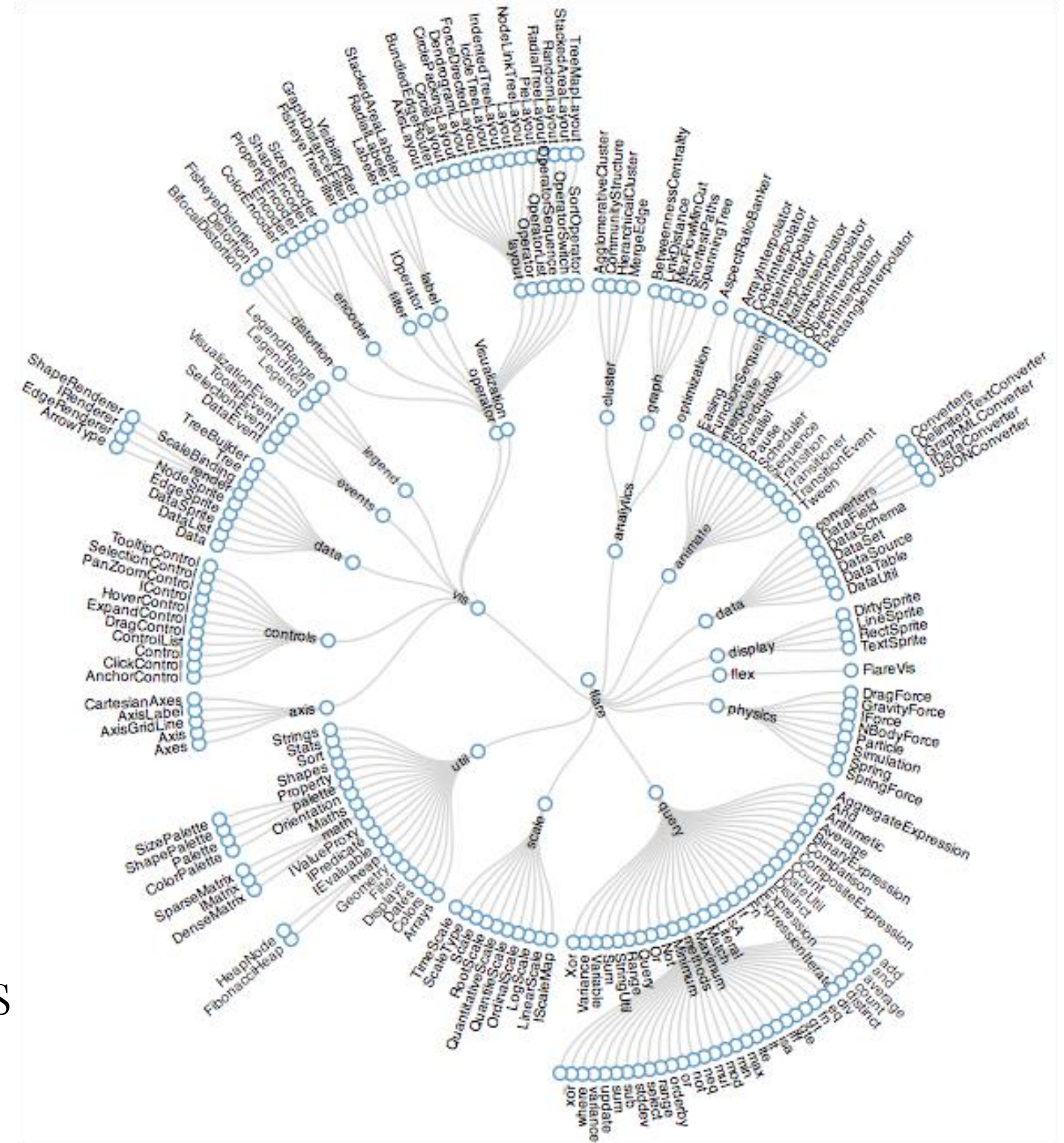
Ghoniem, Fekete, and Castagliola. Information Visualization 4:2 (2005), 114 – 135.]



<http://www.michaelmcguffin.com/courses/vis/patternsInAdjacencyMatrix.pdf>
g

Idiom: **radial node-link tree**

- data
 - tree
- encoding
 - link connection marks
 - point node marks
 - radial axis orientation
 - angular proximity: siblings
 - distance from center: depth in tree
- tasks
 - understanding topology, following paths
- scalability
 - 1K - 10K nodes



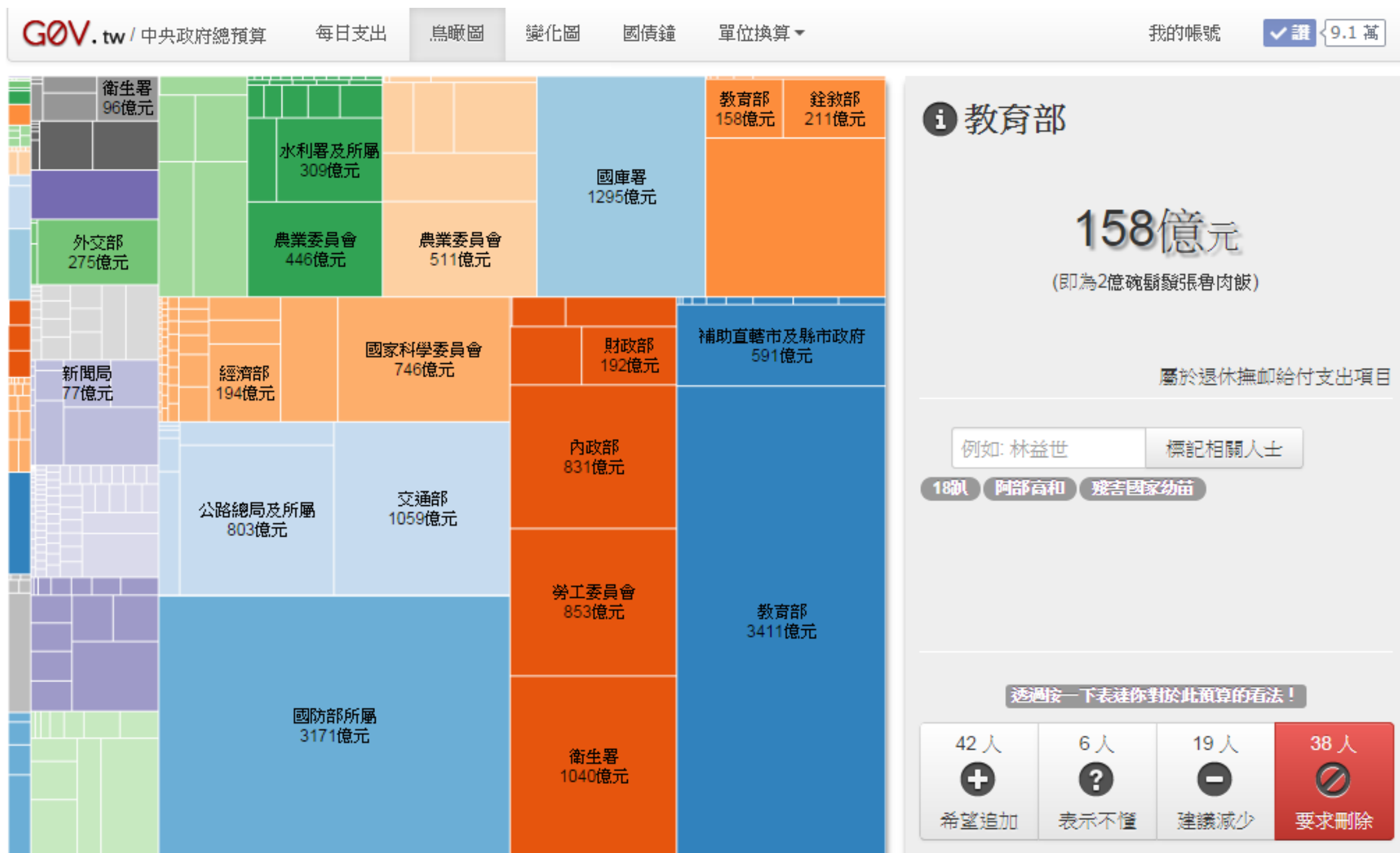
Idiom: **treemap**

- data
 - tree
 - 1 quant attrib at leaf nodes
- encoding
 - area containment marks for hierarchical structure
 - rectilinear orientation
 - size encodes quant attrib
- tasks
 - query attribute at leaf nodes
- scalability
 - 1M leaf nodes



http://tulip.labri.fr/Documentation/3_7/userHandbook/html/ch06.html

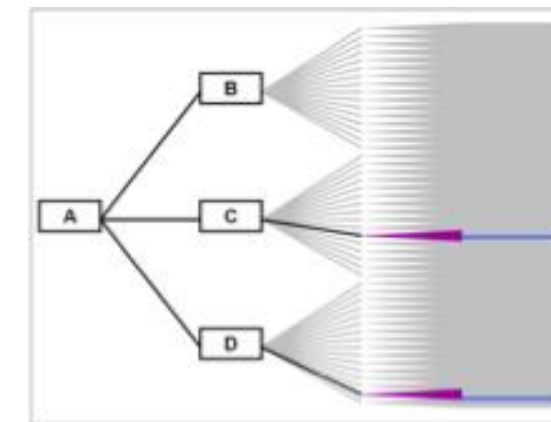
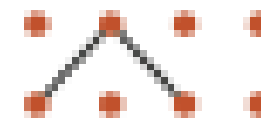
g0v 中央政府總預算



Link marks: Connection and containment

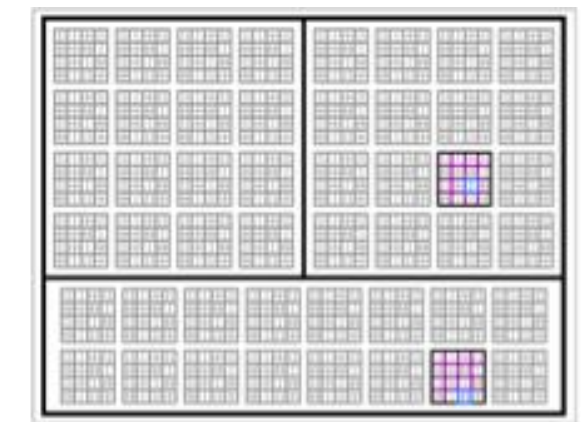
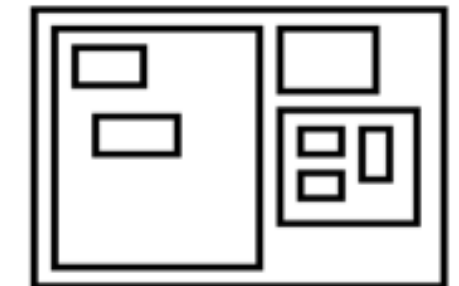
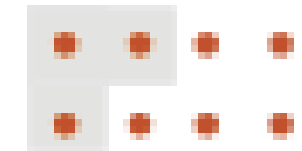
- marks as links (vs. nodes)
 - common case in network drawing
 - 1D case: connection
 - ex: all node-link diagrams
 - emphasizes topology, path tracing
 - networks and trees
 - 2D case: containment
 - ex: all treemap variants
 - emphasizes attribute values at leaves (size coding)
 - only trees

⊕ Connection



Node-Link Diagram

⊕ Containment

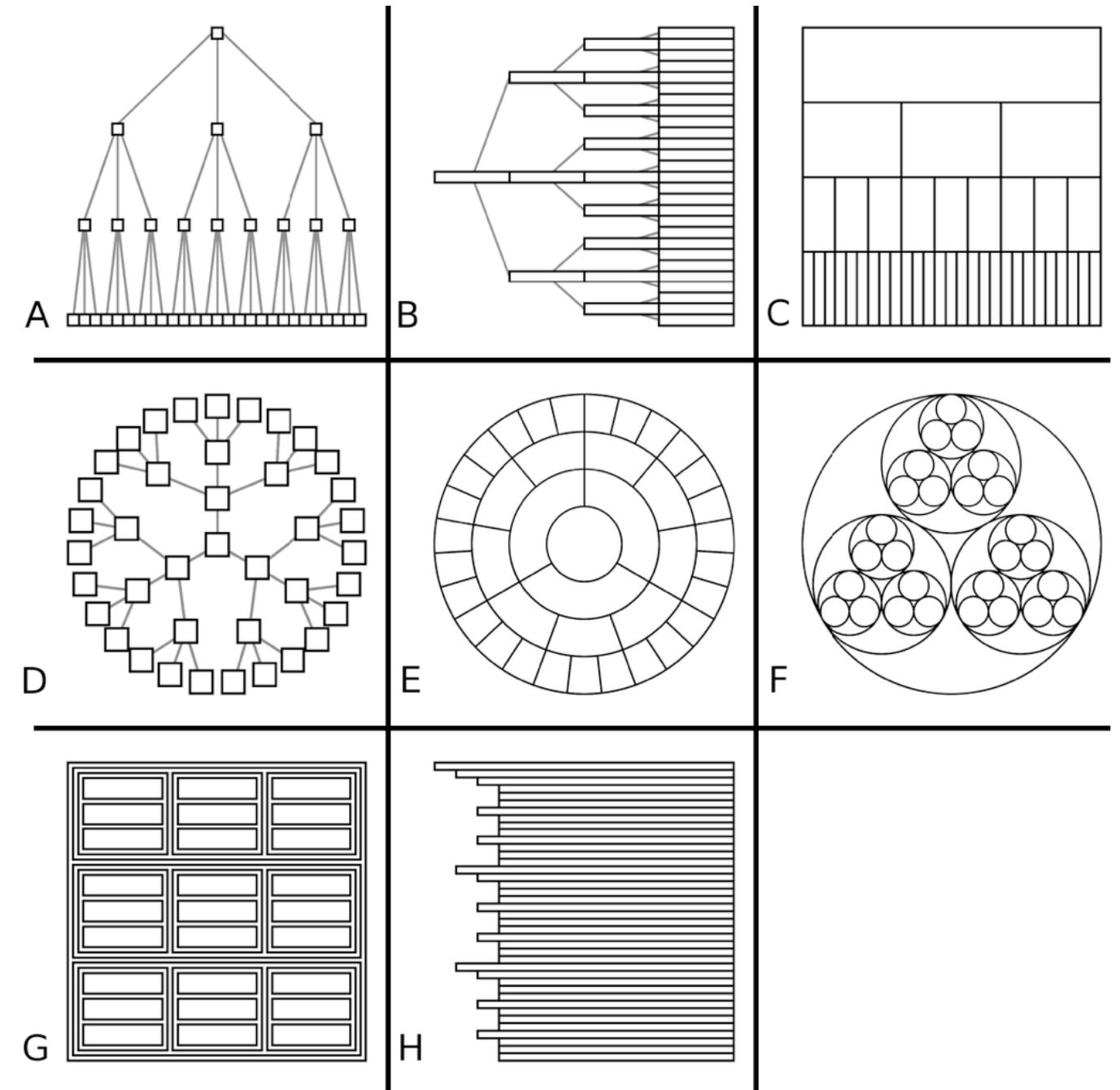


Treemap

[Elastic Hierarchies: Combining Treemaps and Node-Link Diagrams. Dong, McGuffin, and Chignell. Proc. InfoVis 2005, p. 57-64.]

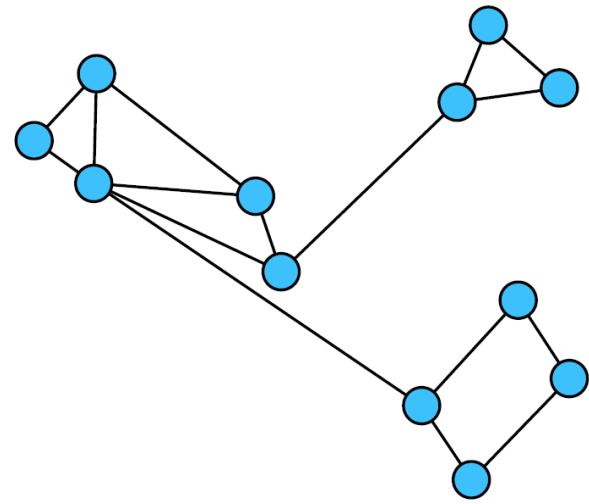
Tree drawing idioms comparison

- data shown
 - link relationships
 - tree depth
 - sibling order
- design choices
 - connection vs containment link marks
 - rectilinear vs radial layout
 - spatial position channels
- considerations
 - redundant? arbitrary?
 - information density?
 - avoid wasting space

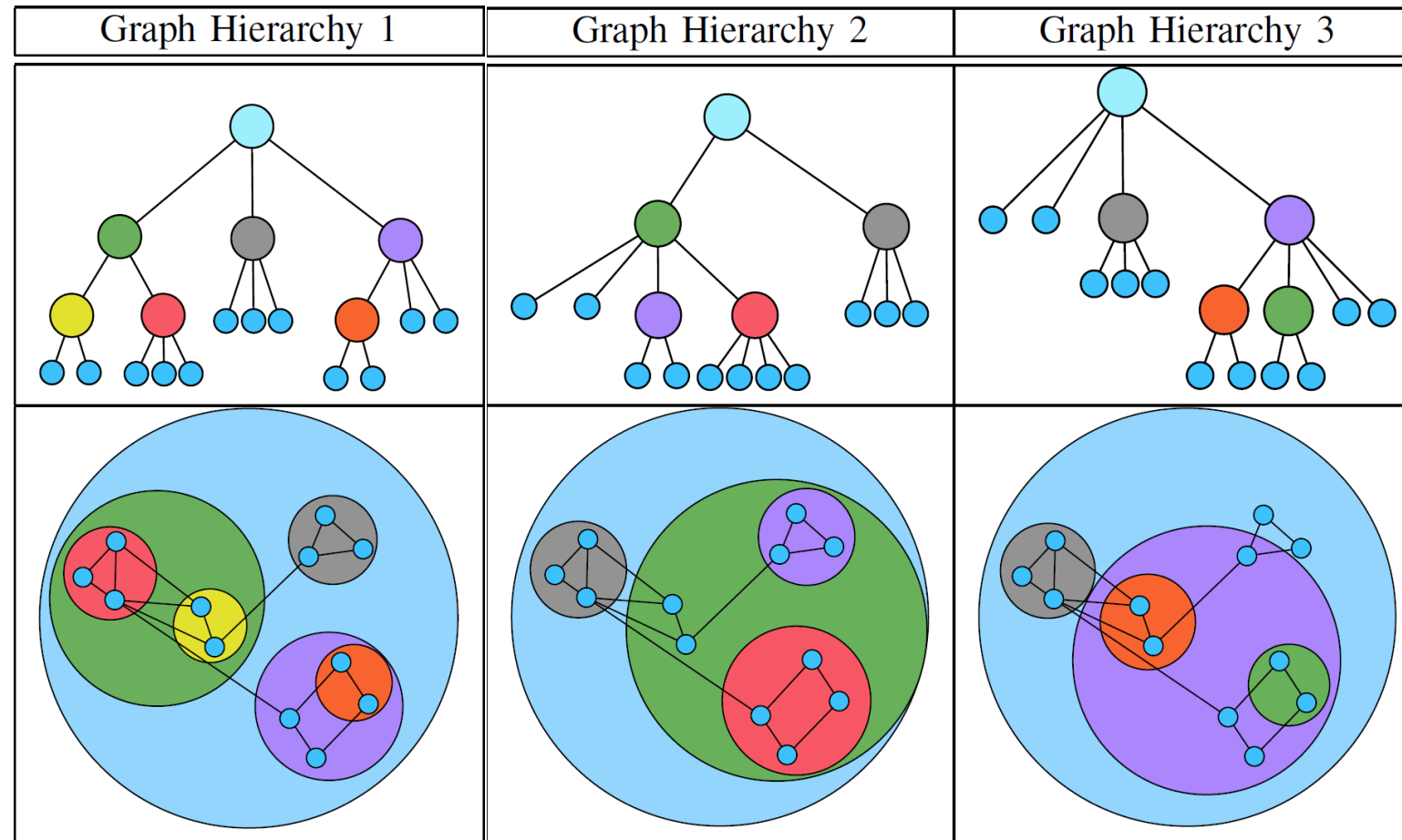


[Quantifying the Space-Efficiency of 2D Graphical Representations of Trees. McGuffin and Robert. Information Visualization 9:2 (2010), 115 – 140.]

GrouseFlocks: Steerable Exploration of Graph Hierarchy Space[2008]



(a) Input Graph



Further reading

- Visualization Analysis and Design. Munzner. AK Peters Visualization Series, CRC Press, 2014.
 - *Chap 9: Arrange Networks and Trees*
- Visual Analysis of Large Graphs: State-of-the-Art and Future Research Challenges. von Landesberger et al. Computer Graphics Forum 30:6 (2011), 1719 – 1749.
- Simple Algorithms for Network Visualization: A Tutorial. McGuffin. Tsinghua Science and Technology (Special Issue on Visualization and Computer Graphics) 17:4 (2012), 383 – 398.
- Drawing on Physical Analogies. Brandes. In Drawing Graphs: Methods and Models, LNCS Tutorial, 2025, edited by M. Kaufmann and D. Wagner, LNCS Tutorial, 2025, pp. 71 – 86. Springer-Verlag, 2001.
- <http://www.treevis.net> Treevis.net: A Tree Visualization Reference. Schulz. IEEE Computer Graphics and Applications 31:6 (2011), 11 – 15.
- Perceptual Guidelines for Creating Rectangular Treemaps. Kong, Heer, and Agrawala. IEEE Trans. Visualization and Computer Graphics (Proc. InfoVis) 16:6 (2010), 990 – 998.