

SPHINCS+

PQC

7/3 or 5.

NIST PQC standard.

KEM
(Encryption)

Signature

call for
4th round.

1 lattice

3

2 lattice

1 hash.

PQC : lattice

idea code

hash

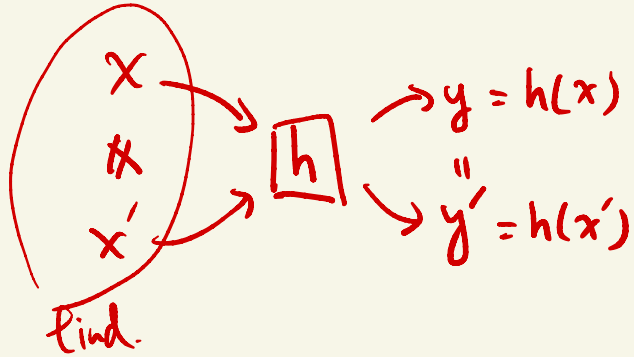
⋮

$\geq n$ \xrightarrow{QC} $\text{poly}(n)$

$\geq n$ $\xrightarrow{\text{Grover}}$ $\sqrt{\geq n}$

hash functions.

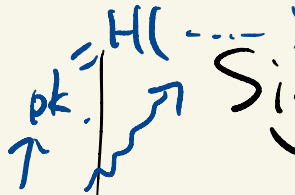
SHA - 256



Winternitz One-time signature

$$H^{256}(sk[0])$$

$$H^{256}(sk[31])$$



KeyGen: sk, pk .

Sign(sk, m) $\rightarrow \sigma$

Verly(pk, m, σ) = $\begin{cases} 0, & \text{reject} \\ 1 & \text{accept} \end{cases}$

$$m_0 = 1$$

$$m_0 \dots$$

8bit \rightarrow

$$m_{31}$$

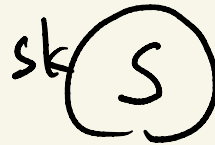
8bit \rightarrow

$$\text{Verly}(pk, m_0=1, H^{256}(sk[0]))$$

$$sk[0] \dots sk[31] \xrightarrow{H(H^{256}(sk[0]))} pk[0]$$

$= ? H^{256}(sk[0])$

$\downarrow sk$



Verly(pk, m, σ)

$$m_1 = 255$$

$$\sigma_1 = H^{256-255}(sk[1])$$

$$= H'(sk[1])$$

$$\text{Vrly: } H^{255}(\sigma_1) \stackrel{?}{=} pk[1] \quad = pk[i]$$

$$m_i = t$$

$$\sigma_i = H^{256-t}(sk[i])$$

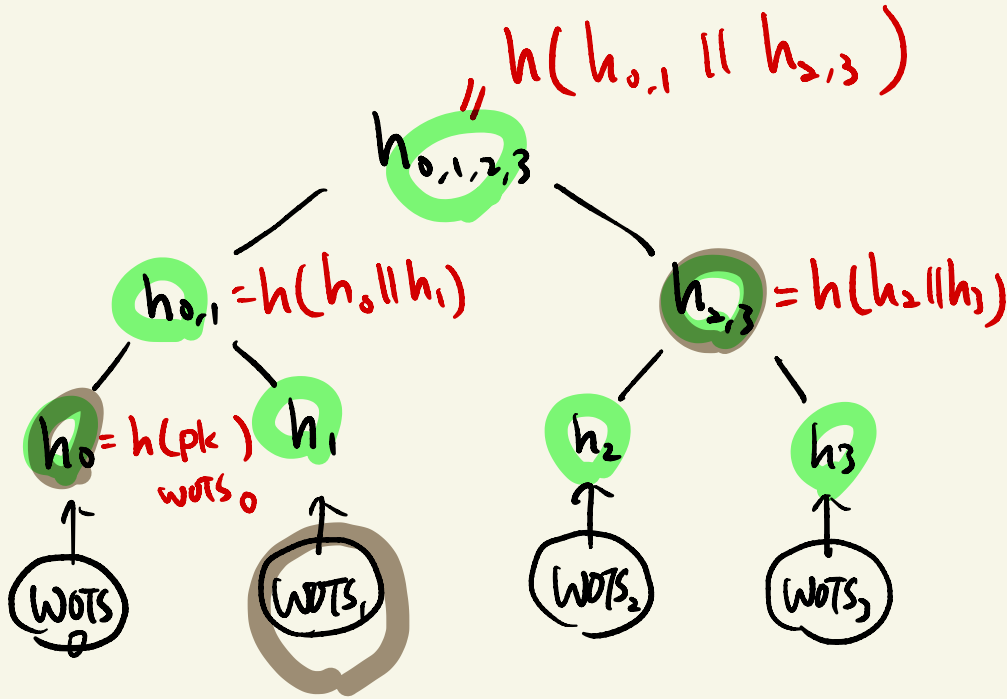
$$\text{Vrly} = H^t(\sigma_i)$$

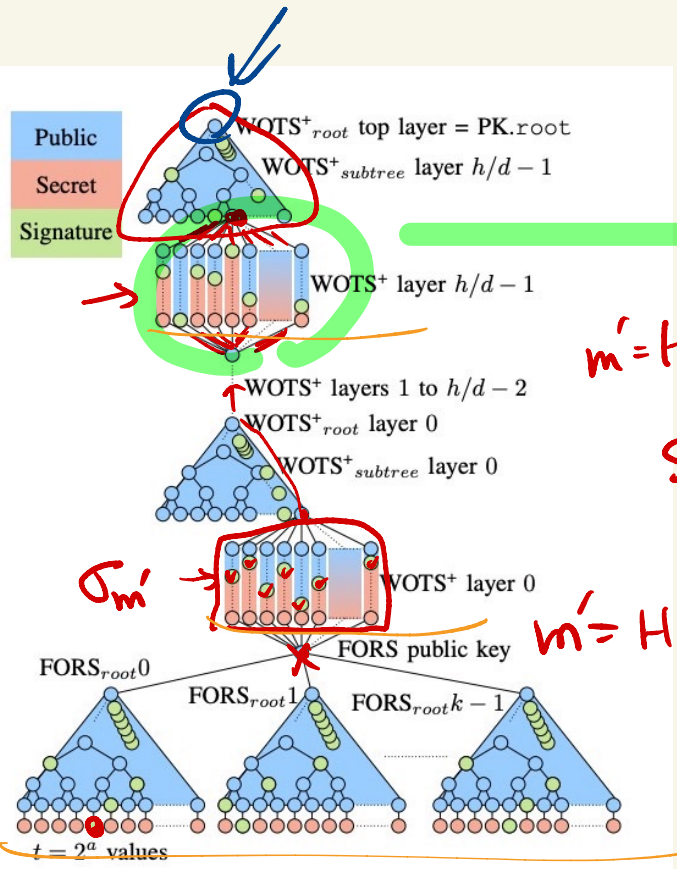
$$= pk[i]$$

254 ... 254 ← σ'
 $m_0 = 255$... 255
 m_{j1}''

$H^2(sk[0])$
↑
 $H'(sk[0])$... $H'(sk[j1]) = \sigma$

Merkle tree.





$m' = H(m || \text{wots+}_{root} \text{ layer 0 pk})$
stateless.

$m' = H(m || \text{FORS public key})$

PRF ()
 r_0
 r_1

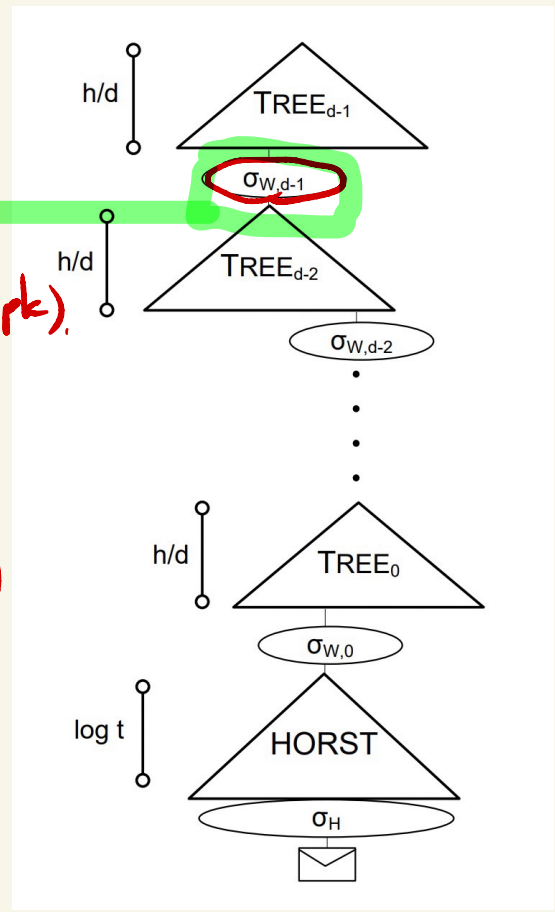
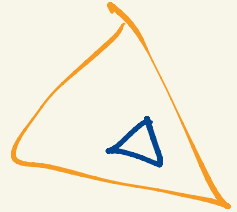
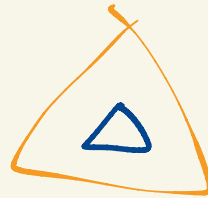
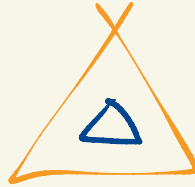
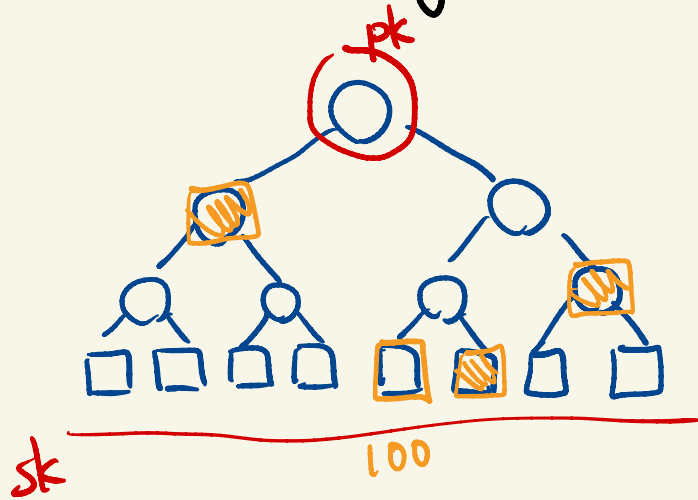


Fig. 2. A SPHINCS+ signature consists of a FORS signature (which signs the message) and several WOTS+ signatures and authentication paths (which sign the FORS public key).

Few-time signature



message = 100 010 011 001