# Multiple Antenna Techniques

- \* In LTE, BS and mobile could both use <u>multiple antennas</u> for radio <u>transmission</u> and <u>reception</u>
- \* In LTE, three main multiple antenna techniques
  - Diversity processing
    - The transmitter, the receiver or both use <u>multiple</u> <u>antennas</u> to
      - \* <u>Increase</u> the <u>received</u> <u>signal</u> <u>power</u>
      - \* <u>Reduce</u> the amount of <u>fading</u>
    - Diversity processing has been used since the <u>early</u> <u>days</u> of mobile communications

- Spatial multiplexing
  - The transmitter and receiver both use multiple antennas to
    - \* <u>Increase</u> the <u>data rate</u>
  - Spatial multiplexing is a relatively new technique that has only <u>recently</u> been introduced into mobile communications
- Beamforming
  - \* Uses multiple antennas at the BS to
    - \* <u>Increase</u> the <u>coverage</u> of the cell

#### Contents

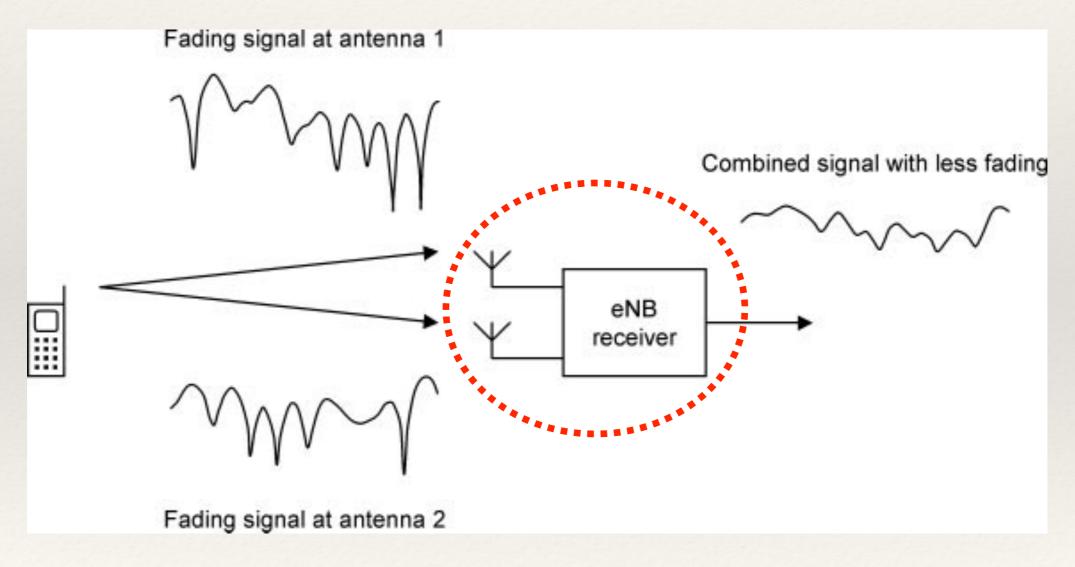
- 5.1 Diversity Processing
- \* 5.2 Spatial Multiplexing
- \* 5.3 Beamforming

# 5.1 Diversity Processing

- 5.1.1 Receive Diversity
- \* 5.1.2 Closed Loop Transmit Diversity
- \* 5.1.3 Open Loop Transmit Diversity

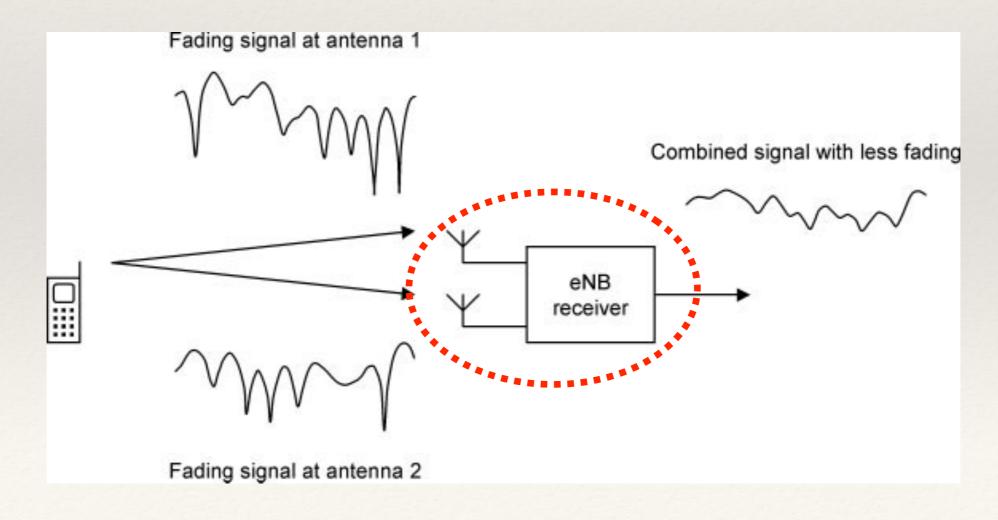
## 5.1.1 Receive Diversity

#### \* <u>Receive diversity</u> is most often used in the <u>uplink</u>



<u>Reduction</u> in <u>fading</u> by the use of a **diversity receiver** 

- BS uses <u>two antennas</u> to pick up <u>two copies</u> of the received signal
- The signals reach the receive antennas with <u>different</u> <u>phase shifts</u>, but these can be <u>removed</u> by antennaspecific <u>channel estimation</u>
- \* BS can then <u>add</u> the signals together in <u>phase</u>



- The signals are both made up from several <u>smaller rays</u>, so they are both <u>subject to fading</u>
  - If the two individual signals undergo <u>fades</u> at the <u>same</u> <u>time</u>, then the <u>power</u> of the <u>combined signal</u> will be <u>low</u>
  - If the antennas are <u>far enough apart</u> (a few wavelengths of the carrier frequency), then the two sets of <u>fading</u> <u>geometries</u> will be very <u>different</u>, so the signals will be far more likely to undergo fades at <u>completely different</u> <u>times</u>

\* BSs

- \* Usually have more than one receive antenna
- \* Mobile
  - In LTE, the mobile's <u>test specifications</u> assume that the mobile is using <u>two receive</u> antennas, so LTE systems are expected to use <u>receive diversity</u> on the <u>downlink</u> as well as the <u>uplink</u>
  - \* A <u>mobile's</u> antennas are <u>closer</u> together than a BS's, which <u>reduces</u> the <u>benefit</u> of <u>receive diversity</u>, but the situation can often be improved using antennas that measure <u>two independent polarizations</u> [極化] of the <u>incoming signal</u>

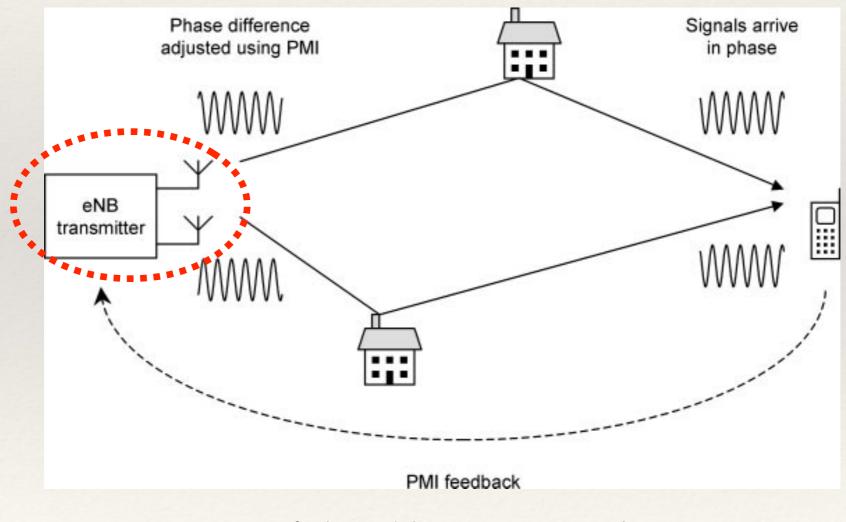
# 5.1 Diversity Processing

- \* 5.1.1 Receive Diversity
- 5.1.2 Closed Loop Transmit Diversity
- \* 5.1.3 Open Loop Transmit Diversity

## 5.1.2 Closed Loop Transmit Diversity

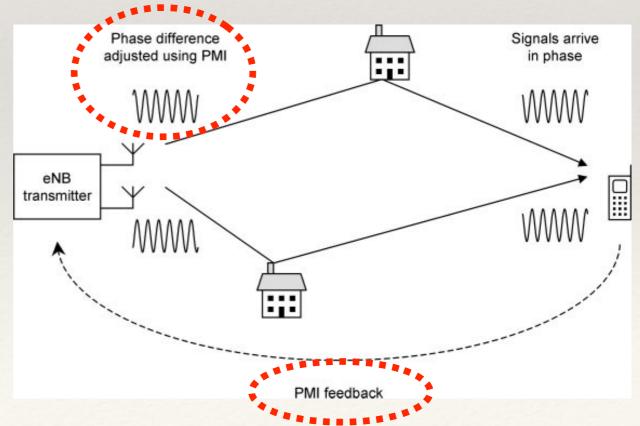
- \* <u>Transmit diversity reduces</u> the amount of <u>fading</u> by using two or more antennas at the <u>transmitter</u>
- It is superficially similar to <u>receive diversity</u>, but with a crucial problem
  - The signals add together at the <u>single receive antenna</u>, which brings a risk of <u>destructive interference</u>

- \* Two ways to solve the problem
  - Closed loop transmit diversity
  - Open loop transmit diversity
- Closed loop transmit diversity

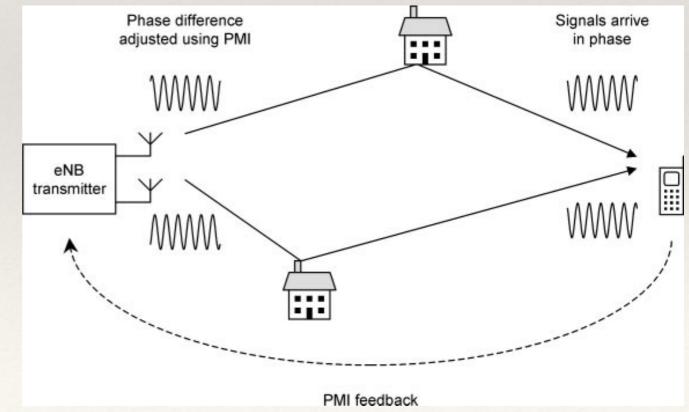


Operation of **closed loop** transmit diversity

- The <u>transmitter</u> sends <u>two copies</u> of the signal in the expected way, but it also applies a <u>phase shift</u> to one or both signals before transmission
  - By doing this, it can ensure that the <u>two signals</u> reach the receiver <u>in phase</u>, without any risk of destructive interference
  - The <u>phase shift</u> is determined by a <u>precoding matrix</u> <u>indicator</u> (PMI), which is calculated by the <u>receiver</u> and fed back to the transmitter



- \* A simple PMI might indicate <u>two options</u>
  - \* Transmit both signals <u>without</u> any <u>phase shifts</u>
  - \* Transmit the second with a <u>phase shift</u> of 180°
  - \* If the first option leads to <u>destructive interference</u>, then the second will automatically work
- \* The <u>amplitude</u> of the combined signal is only <u>low</u> in the unlikely event that the <u>two received signals</u> undergo <u>fades</u> at the same time



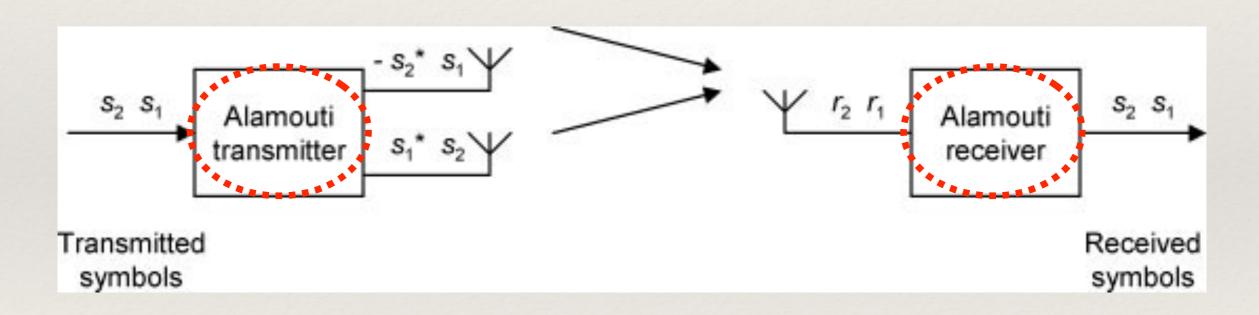
- \* The <u>phase shifts</u> introduced by the radio channel depend on the <u>wavelength</u> of the carrier signal and hence on its <u>frequency</u>
  - \* This implies that the <u>best choice of PMI</u> is a function of <u>frequency</u> as well
    - \* This is easily handled in an OFDMA system, as the <u>receiver</u> can <u>feed back different PMI values</u> for different sets of sub-carriers
  - \* The <u>best choice of PMI</u> also depends on the <u>position</u> of the mobile, so a <u>fast moving mobile</u> will have a PMI that frequently changes
    - Unfortunately the <u>feedback loop</u> introduces <u>time delays</u> into the system, so in the case of <u>fast moving mobiles</u>, the PMI may be <u>out of date</u> by the time it is used
    - \* For this reason, **closed loop transmit diversity** is **only suitable** for mobiles that are moving **sufficiently slowly**
    - \* For <u>fast moving mobiles</u>, it is better to use the **open loop** technique

# 5.1 Diversity Processing

- \* 5.1.1 Receive Diversity
- \* 5.1.2 Closed Loop Transmit Diversity
- 5.1.3 Open Loop Transmit Diversity

# 5.1.3 Open Loop Transmit Diversity

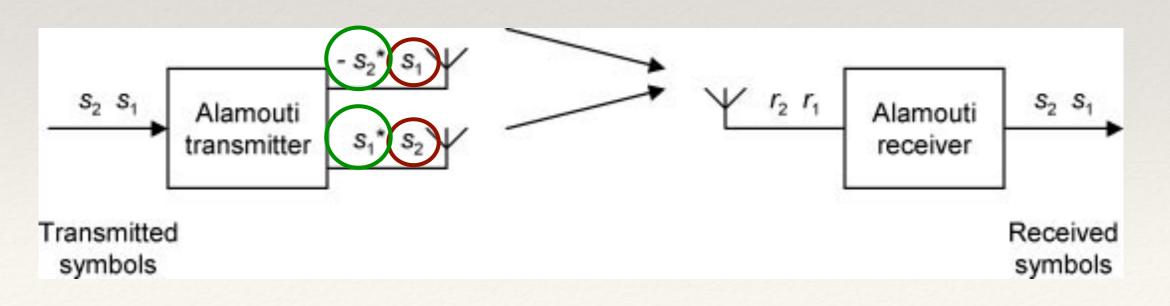
 An implementation of <u>open loop transmit diversity</u> that is known as Alamouti's technique



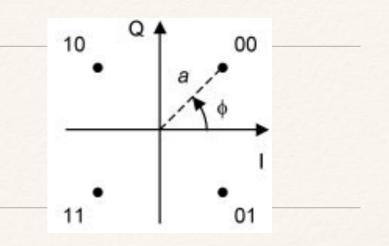
Operation of Alamouti's technique for **open loop** transmit diversity

- \* The <u>transmitter</u> uses two antennas to send two symbols, denoted s<sub>1</sub> and s<sub>2</sub>, in two <u>successive time</u> steps
  - In the first step, the transmitter sends s<sub>1</sub> from the first antenna and s<sub>2</sub> from the second
  - In the second step, it sends -s<sub>2</sub>\* from the first antenna and s<sub>1</sub>\* from the second

(The symbol \* indicates that the transmitter should change the <u>sign</u> of the <u>quadrature</u> <u>component</u>, in a process known as <u>complex conjugation</u>)



# Note: QPSK



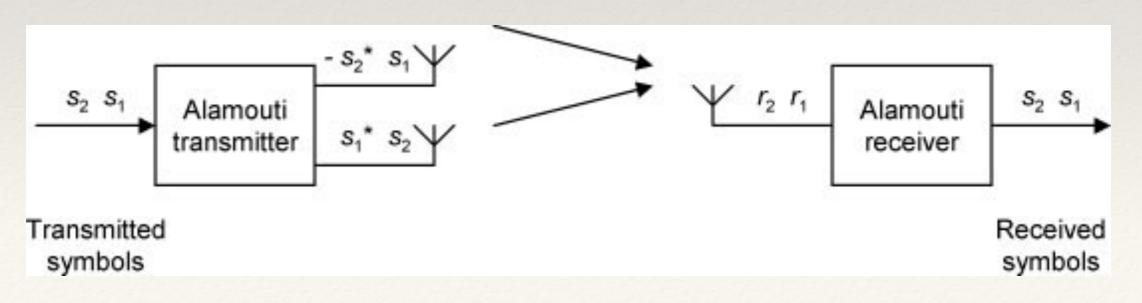
- In the Quadrature Phase Shift Keying (QPSK), it is more convenient to represent each symbol using two numbers, which are known as the in-phase (I) and quadrature (Q) components
- \* These are computed as follows

 $\mathbf{I} = a \cos \phi$ 

 $\mathbf{Q} = a \sin \phi$ 

- where *a* is the <u>amplitude</u> of the transmitted wave and φ is its phase
- \* Mathematicians will recognize the <u>in-phase</u> and <u>quadrature</u> <u>components</u> as the <u>real</u> and <u>imaginary</u> parts of a complex number

- The <u>receiver</u> can now make <u>two successive measurements</u> of the received signal, which correspond to two different combinations of s<sub>1</sub> and s<sub>2</sub>
  - It can then solve the resulting equations, so as to <u>recover</u> the two transmitted symbols
- \* There are only two requirements
  - The <u>fading patterns</u> must stay <u>roughly the same</u> between the first time step and the second
  - \* The two signals must <u>not</u> undergo <u>fades</u> at the <u>same time</u>
  - Both requirements are usually met



 We can <u>combine</u> open and closed loop transmit diversity with the <u>receive diversity techniques</u>, giving a system that carries out diversity processing using <u>multiple antennas</u> at both the transmitter and the receiver

#### Contents

- 5.1 Diversity Processing
- 5.2 Spatial Multiplexing
- \* 5.3 Beamforming

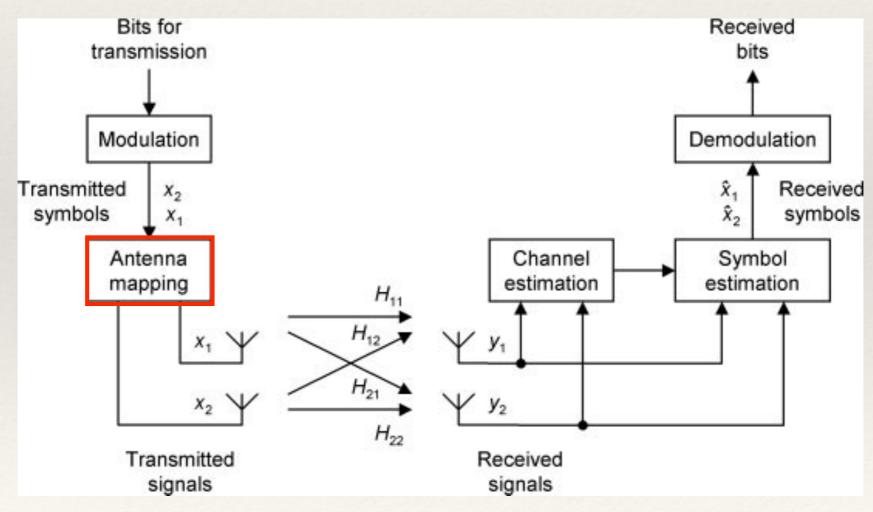
# 5.2 Spatial Multiplexing

- 5.2.1 Principles of Operation
- \* 5.2.2 Open Loop Spatial Multiplexing
- \* 5.2.3 Closed Loop Spatial Multiplexing
- \* 5.2.5 Implementation Issues
- \* 5.2.6 Multiple User MIMO

# 5.2.1 Principles of Operation

- If the transmitter and receiver both have <u>multiple</u> <u>antennas</u>, then we can set up <u>multiple parallel data</u> <u>streams</u> between them, so as to <u>increase</u> the <u>data rate</u>
- \* In a system with  $N_T$  <u>transmit</u> and  $N_R$  <u>receive</u> antennas, often known as an  $N_T \times N_R$  spatial multiplexing system, the <u>peak data rate</u> is proportional to min( $N_T$ ,  $N_R$ )

- A basic spatial multiplexing system, in which the transmitter and receiver both have <u>two</u> antennas
  - \* In the <u>transmitter</u>, the <u>antenna mapper</u> takes symbols from the <u>modulator</u> two at a time, and sends one symbol to each antenna
  - \* The antennas transmit the two symbols <u>simultaneously</u>, so as to <u>double</u> the <u>transmitted data rate</u>



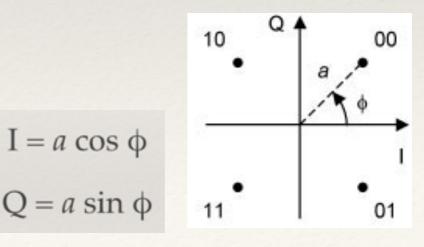
Basic principles of a 2x2 spatial multiplexing system

 The symbols travel to the receive antennas by way of <u>four</u> separate <u>radio paths</u>, so the <u>received signals</u> can be written as follows

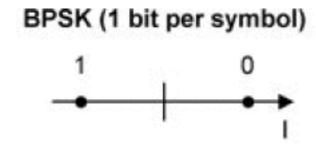
 $y_1 = H_{11} x_1 + H_{12} x_2 + n_1$  $y_2 = H_{21} x_1 + H_{22} x_2 + n_2$ 

- \*  $x_1$  and  $x_2$  are the signals <u>sent</u> from the two <u>transmit</u> antennas
- \* y<sub>1</sub> and y<sub>2</sub> are the signals that <u>arrive</u> at the two <u>receive</u> antennas
- \* n<sub>1</sub> and n<sub>2</sub> represent the <u>received noise</u> and <u>interference</u>
- H<sub>ij</sub> expresses the way in which the transmitted symbols are <u>attenuated</u> and <u>phase-shifted</u>, as they travel to receive antenna *i* from transmit antenna *j*

- In general, all the terms in the equation above are <u>complex</u>
  - In the transmitted and received symbols x<sub>j</sub> and y<sub>j</sub> and the noise terms n<sub>i</sub>, the <u>real</u> and <u>imaginary</u> parts are the <u>amplitudes</u> of the <u>in-phase</u> and <u>quadrature</u> components
  - \* In each of the channel elements H<sub>ij</sub>
    - \* The <u>magnitude</u> represents the <u>attenuation</u> of the radio signal
    - \* The <u>phase</u> represents the <u>phase shift</u>



- \* We will simplify the examples by using <u>real numbers</u> alone
  - We assume that the <u>transmitter</u> is modulating the bits using <u>binary phase shift keying</u>
    - ✤ The <u>in-phase</u> components are +1 and −1
    - \* The <u>quadrature</u> components are zero



 We will also assume that the radio channel can <u>attenuate</u> or <u>invert</u> the signal, but does <u>not</u> introduce any other phase shifts Consistent with these assumptions, let us consider the following example

 $H_{11} = 0.8 \quad H_{12} = 0.6 \quad x_1 = +1 \quad n_1 = +0.02$ 

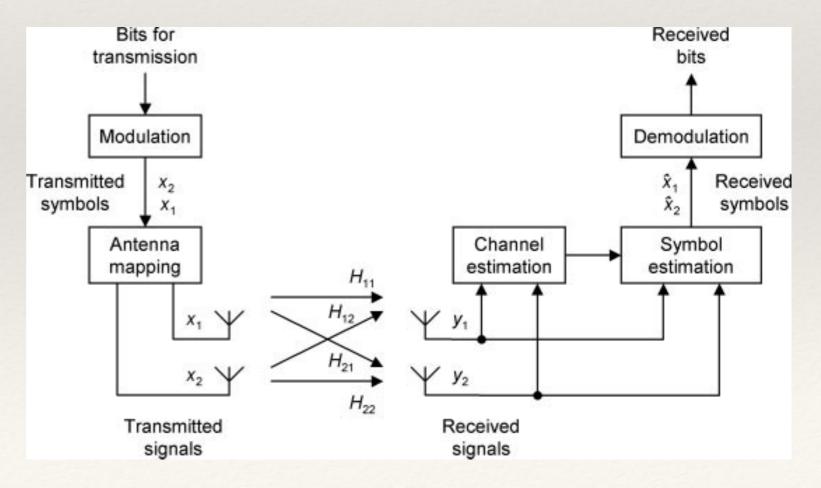
 $H_{21}=0.2 \quad H_{22}=0.4 \quad x_2=-1 \quad n_2=-0.02$ 

 Substituting these numbers into the previous equation shows that the received signals are as follows

> $y_1 = +0.22$  $y_2 = -0.22$

- The <u>receiver's</u> first task is to <u>estimate</u> the <u>four</u> channel elements H<sub>ij</sub>
  - The <u>transmitter</u> broadcasts <u>reference symbols</u> with one extra feature
    - When one antenna transmits a reference symbol, the other antenna keeps <u>quiet</u> and <u>sends nothing</u> at all

- The <u>receiver</u> can then <u>estimate</u> the channel elements H<sub>11</sub> and H<sub>21</sub>, by measuring the two received signals at the times when <u>transmit antenna 1</u> is sending a reference symbol
- It can then wait until <u>transmit antenna 2</u> sends a reference symbol, before estimating the channel elements H<sub>12</sub> and H<sub>22</sub>



 $y_1 = H_{11}x_1 + H_{12}x_2 + n_1$  $y_2 = H_{21}x_1 + H_{22}x_2 + n_2$ 

- The <u>receiver</u> now has enough information to <u>estimate</u> the <u>transmitted symbols</u> x<sub>1</sub> and x<sub>2</sub>
  - The simplest way is a <u>zero-forcing detector</u>, which operates as follows
    - If we ignore the noise and interference, then the equation (5.1) is a pair of <u>simultaneous equations</u> for two unknown quantities, x<sub>1</sub> and x<sub>2</sub>

$$\hat{x}_{1} = \frac{\hat{H}_{22}y_{1} - \hat{H}_{12}y_{2}}{\hat{H}_{11}\hat{H}_{22} - \hat{H}_{21}\hat{H}_{12}}$$
$$\hat{x}_{2} = \frac{\hat{H}_{11}y_{2} - \hat{H}_{21}y_{1}}{\hat{H}_{11}\hat{H}_{22} - \hat{H}_{21}\hat{H}_{12}}$$

(5.1)

$$\hat{x}_{1} = \frac{\hat{H}_{22}y_{1} - \hat{H}_{12}y_{2}}{\hat{H}_{11}\hat{H}_{22} - \hat{H}_{21}\hat{H}_{12}}$$
$$\hat{x}_{2} = \frac{\hat{H}_{11}y_{2} - \hat{H}_{21}y_{1}}{\hat{H}_{11}\hat{H}_{22} - \hat{H}_{21}\hat{H}_{12}}$$

- <sup>\*</sup> <sup>^</sup>H<sub>ij</sub> is the <u>receiver's estimate</u> of the <u>channel element</u> H<sub>ij</sub> (This quantity may be different from H<sub>ij</sub>, because of noise and other errors in the channel estimation process)
- ^x<sub>1</sub> and ^x<sub>2</sub> are the receiver's <u>estimates</u> of the <u>transmitted symbols</u> x<sub>1</sub> and x<sub>2</sub>

$$\begin{array}{ll} H_{11} = 0.8 & H_{12} = 0.6 & x_1 = +1 & n_1 = +0.02 \\ H_{21} = 0.2 & H_{22} = 0.4 & x_2 = -1 & n_2 = -0.02 \end{array}$$
(5.2)  
 
$$\begin{array}{l} y_1 = +0.22 \\ y_2 = -0.22 \end{array}$$
(5.3)

Substituting the numbers from Equations (5.2) and (5.3) gives the following result

$$\hat{x}_1 = +1.1$$

$$\hat{x}_2 = -1.1$$

- This is consistent with transmitted symbols of +1 and-1
- We have therefore <u>transferred two symbols</u> at the same time using the <u>same sub-carriers</u>, and have <u>doubled the</u> <u>data rate</u>

# 5.2 Spatial Multiplexing

- \* 5.2.1 Principles of Operation
- 5.2.2 Open Loop Spatial Multiplexing
- \* 5.2.3 Closed Loop Spatial Multiplexing
- \* 5.2.5 Implementation Issues
- \* 5.2.6 Multiple User MIMO

#### 5.2.2 Open Loop Spatial Multiplexing

- \* There is a problem with the technique described above
  - \* Let us change one of the channel elements, H<sub>11</sub>, to give the following example

 $H_{11} = 0.3$   $H_{12} = 0.6$ 

 $H_{21}=0.2 \quad H_{22}=0.4$ 

$$\hat{x}_{1} = \frac{\hat{H}_{22}y_{1} - \hat{H}_{12}y_{2}}{\hat{H}_{11}\hat{H}_{22} - \hat{H}_{21}\hat{H}_{12}}$$

$$\hat{x}_{2} = \frac{\hat{H}_{11}y_{2} - \hat{H}_{21}y_{1}}{\hat{H}_{11}\hat{H}_{22} - \hat{H}_{21}\hat{H}_{12}}$$
(5.4)

- If we try to estimate the transmitted symbols using Equation (5.4), we find that H<sub>11</sub>H<sub>22</sub> – H<sub>21</sub>H<sub>12</sub> is zero
  - \* We therefore end up dividing by zero, which is nonsense
  - \* So, for this choice of channel elements, the technique has failed

 $y_1 = H_{11}x_1 + H_{12}x_2 + n_1$  $y_2 = H_{21}x_1 + H_{22}x_2 + n_2$ (5.1)

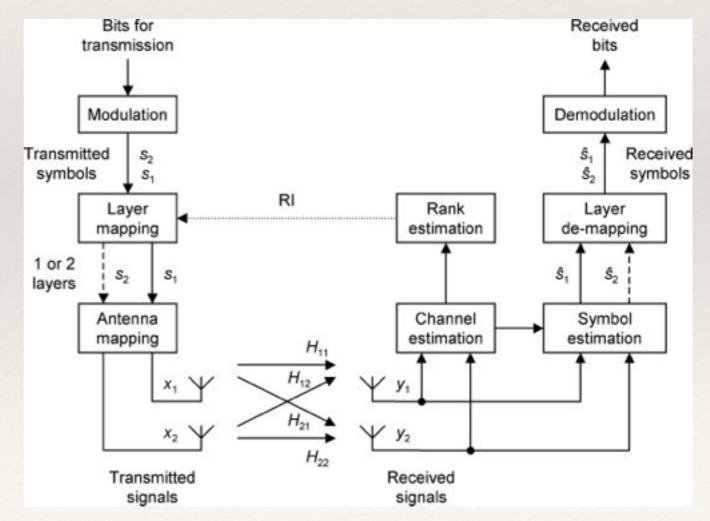
 We can see what has gone wrong by substituting the channel elements into Equation (5.1), and writing the received signals as follows

 $y_1 = 0.3(x_1 + 2x_2) + n_1$  $y_2 = 0.2(x_1 + 2x_2) + n_2$ 

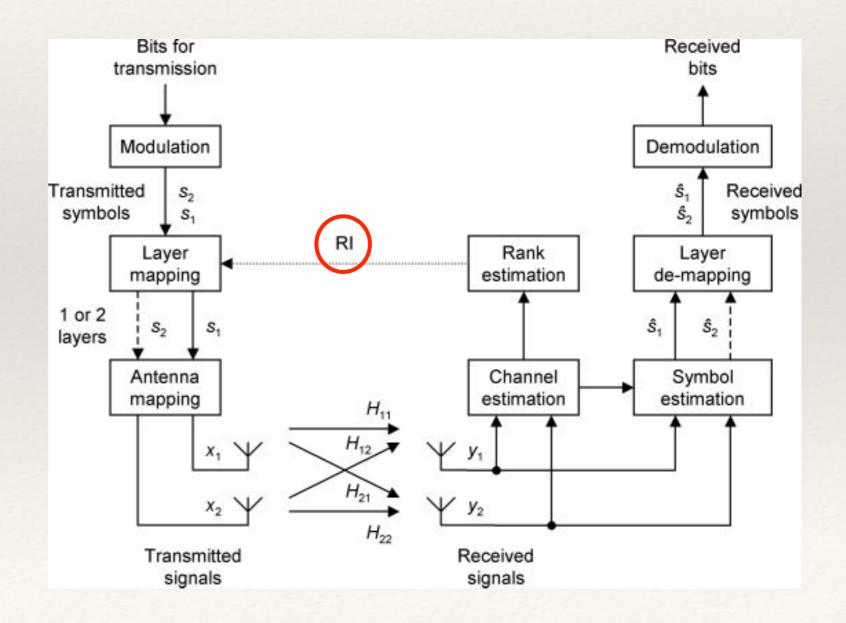
 $y_1 = 0.3(x_1 + 2x_2) + n_1$  $y_2 = 0.2(x_1 + 2x_2) + n_2$ 

- By measuring the received signals y<sub>1</sub> and y<sub>2</sub>, we were expecting to measure two different pieces of information, from which we could <u>recover</u> the transmitted data
  - This time, we have measured the same piece of information, namely x<sub>1</sub> + 2x<sub>2</sub>, twice
  - As a result, we do not have enough information to recover x<sub>1</sub> and x<sub>2</sub> independently
- \* Furthermore, this is not just an isolated special case
  - If H<sub>11</sub>H<sub>22</sub> H<sub>21</sub>H<sub>12</sub> is <u>small</u> but <u>non-zero</u>, then our estimates of x<sub>1</sub> and x<sub>2</sub> turn out to be <u>badly corrupted</u> by noise and are completely unusable

- \* The solution comes from the knowledge that we can still send <u>one symbol</u> at a time, by the use of <u>diversity processing</u>
- \* We therefore require an <u>adaptive</u> system
  - \* Use <u>spatial multiplexing</u> to send <u>two symbols</u> at a time if the channel elements are <u>well behaved</u>
  - \* Can fall back to <u>diversity processing</u> otherwise



- Here, the <u>receiver</u> measures the channel elements and works out a <u>rank indication (RI)</u>, which indicates the <u>number of symbols</u> that it can successfully receive
- \* It then feeds the rank indication back to the <u>transmitter</u>

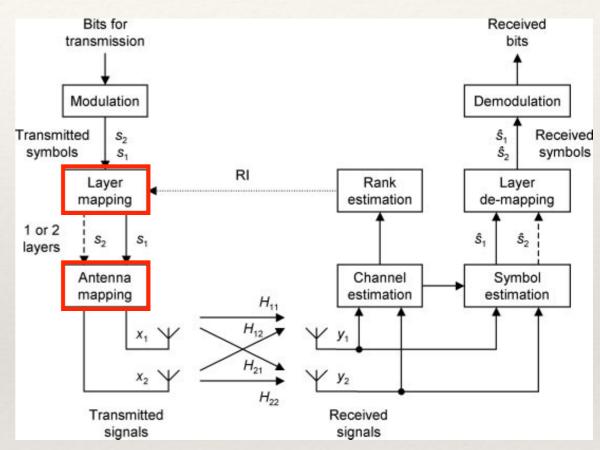


- \* If the rank indication is <u>two</u>
  - The <u>transmitter's layer mapper</u> grabs <u>two symbols</u>, s<sub>1</sub> and s<sub>2</sub>, from the transmit buffer, so as to create <u>two</u> independent <u>data streams</u> that are known as <u>layers</u>
  - The <u>antenna mapper</u> then sends one symbol to each antenna, by a straightforward mapping operation

$$x_1 = s_1$$

$$\mathbf{x}_2 = \mathbf{s}_2$$

 The <u>receiver</u> measures the incoming signals and <u>recovers</u> the transmitted symbols as before



$$y_1 = 0.3(x_1 + 2x_2) + n_1$$
  
$$y_2 = 0.2(x_1 + 2x_2) + n_2$$

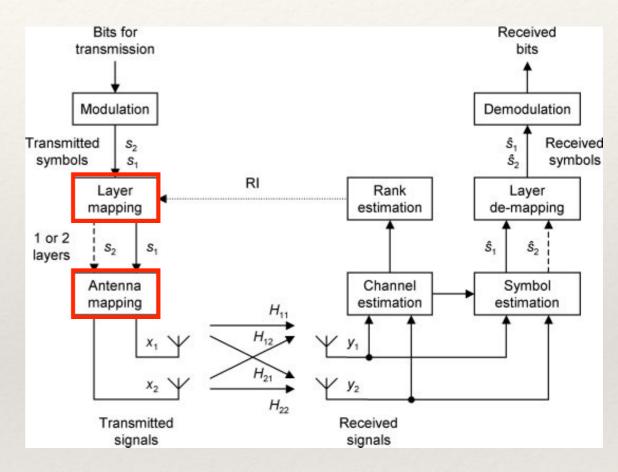
- \* If the rank indication is <u>one</u>
  - The <u>layer mapper</u> only grabs <u>one</u> symbol, s<sub>1</sub>
  - The <u>antenna mapper</u> sends to both <u>transmit antennas</u> as follows

 $\mathbf{x}_1 = \mathbf{s}_1$ 

$$\mathbf{x}_2 = \mathbf{s}_1$$

 Under these assumptions, Equation (5.7) becomes the following

$$y_1 = 0.9s_1 + n_1$$
  
 $y_2 = 0.6s_1 + n_2$ 



(5.7

- The <u>receiver</u> now has <u>two measurements</u> of the transmitted symbol s<sub>1</sub>, and can combine these in a <u>diversity receiver</u> so as to <u>recover</u> the transmitted data
- This technique is implemented in LTE and is known as <u>open loop</u> spatial multiplexing

# 5.2 Spatial Multiplexing

- \* 5.2.1 Principles of Operation
- \* 5.2.2 Open Loop Spatial Multiplexing
- 5.2.3 Closed Loop Spatial Multiplexing
- \* 5.2.5 Implementation Issues
- \* 5.2.6 Multiple User MIMO

### 5.2.3 Closed Loop Spatial Multiplexing

- \* There is one remaining problem
- \* Let us change two more of the channel elements, so that

 $H_{11} = 0.3$   $H_{12} = -0.3$  $H_{21} = 0.2$   $H_{22} = -0.2$ 

- \* These channel elements are <u>badly behaved</u>, in that  $H_{11}H_{22} H_{21}H_{12}$  is <u>zero</u>
- But if we try to handle the situation in the manner described above, by sending the same symbol from <u>both</u> <u>transmit antennas</u>, then the <u>received</u> signals are as follows

 $y_1 = 0.3s_1 - 0.3s_1 + n_1$ 

 $y_2 = 0.2s_1 - 0.2s_1 + n_2$ 

- \* So the <u>transmitted</u> signals cancel out at both <u>receive</u> antennas and we are left with measurements of the <u>incoming noise</u> and <u>interference</u>
- We therefore have <u>insufficient information</u> even to <u>recover</u>
   <u>S1</u>
- To see the way out, consider what happens if we send <u>one</u> symbol at a time as before, but <u>invert the signal</u> that is sent from the <u>second</u> antenna

$$\mathbf{x}_1 = \mathbf{s}_1$$

$$x_2 = -s_1$$

\* The <u>received</u> signal can now be written as follows

 $y_1 = 0.3s_1 + 0.3s_1 + n_1$ 

$$y_2 = 0.2s_1 + 0.2s_1 + n_2$$

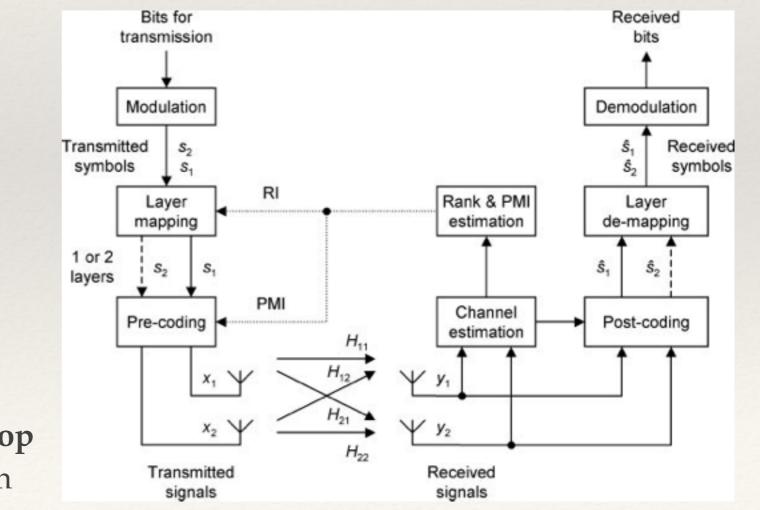
- \* This time, we can <u>recover</u> the transmitted symbol s<sub>1</sub>
- \* So we now require <u>two levels</u> of <u>adaptation</u>
  - If the rank indication is <u>two</u>, then the transmitter sends <u>two</u> symbols at a time using the antenna mapping of Equation (5.8)

$$\begin{aligned}
 x_1 &= s_1 \\
 x_2 &= s_2
 \end{aligned}
 \tag{5.8}$$

 If the rank indication is <u>one</u>, then the transmitter falls back to <u>diversity processing</u> and sends <u>one</u> symbol at a time In doing so, it chooses an antenna mapping such as Equation (5.9) or (5/13), which depends on the exact nature of the <u>channel elements</u> and which guarantees a <u>strong signal</u> at the receiver

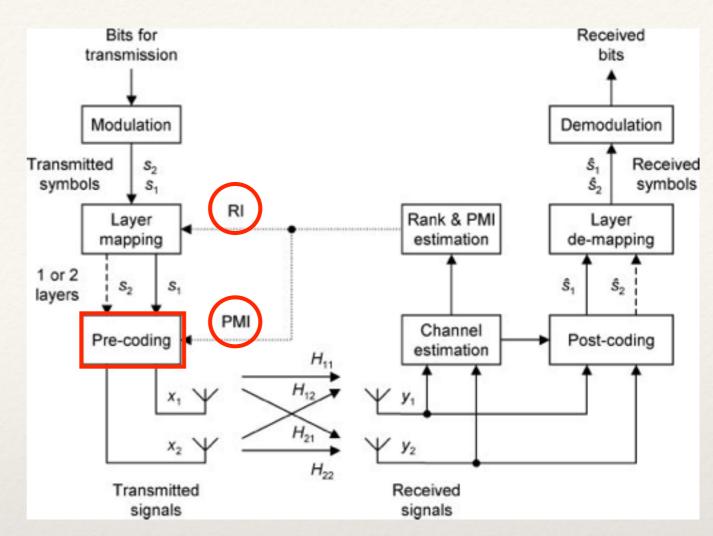
$$\begin{array}{l} x_1 = s_1 \\ x_2 = s_1 \end{array} \tag{5.9} \quad \begin{array}{l} x_1 = s_1 \\ x_2 = -s_1 \end{array} \tag{5.13}$$

\* Such a system is shown s follows:



Operation of a 2x2 **closed loop** spatial multiplexing system

- The receiver measures the channel elements as before and uses them to <u>feed back two quantities</u>
  - \* Rank Indication (RI)
  - \* Precoding Matrix Indicator (PMI)
- \* PMI
  - \* Controls a **precoding** step in the transmitter
  - It implements an <u>adaptive antenna</u> <u>mapping</u> using (for example) Equations (5.8), (5.9) and (5.13), to ensure that the signals reach the receiver without <u>cancellation</u> (In fact the PMI has exactly the <u>same role</u> that we saw earlier when discussing <u>closed loop transmit</u> <u>diversity</u>, which is why its name is the same)



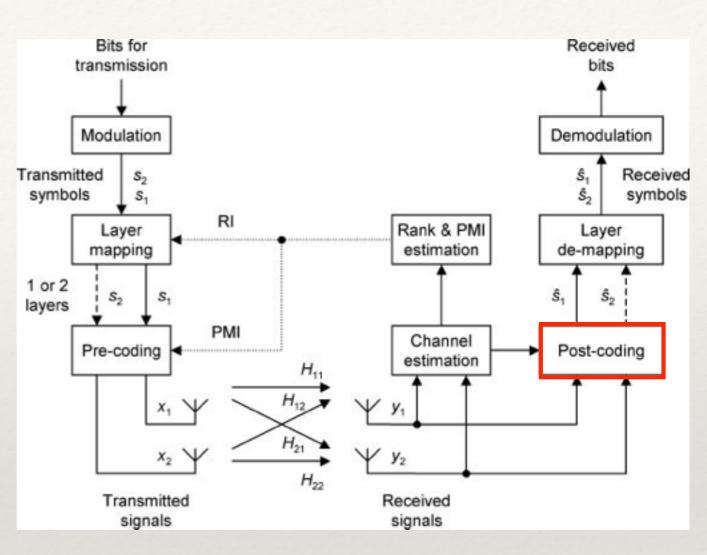
$$x_{1} = s_{1}$$

$$x_{2} = s_{2}$$
(5.8)
$$x_{1} = s_{1}$$

$$x_{2} = s_{1}$$
(5.9)
$$x_{1} = s_{1}$$

$$x_{2} = -s_{1}$$
(5.13)

- In the <u>receiver</u>, the <u>post-</u>
   <u>coding</u> step <u>reverses</u> the
   effect of <u>precoding</u> and also
   includes the <u>soft decision</u>
   <u>estimation</u> step from earlier
- This technique is also implemented in LTE, and is known as <u>closed loop</u> <u>spatial multiplexing</u>
- In this expression, the term
   'closed loop' refers
   specifically to the loop that
   is created by feeding back
   the PMI



# 5.2 Spatial Multiplexing

- \* 5.2.1 Principles of Operation
- \* 5.2.2 Open Loop Spatial Multiplexing
- \* 5.2.3 Closed Loop Spatial Multiplexing
- 5.2.5 Implementation Issues
- \* 5.2.6 Multiple User MIMO

# 5.2.5 Implementation Issues

- <u>Spatial multiplexing</u> is implemented in the <u>downlink</u> of LTE <u>Release</u>
   <u>8</u>, using a maximum of <u>four</u> transmit antennas on the <u>BS</u> and <u>four</u>
   receive antennas on the <u>mobile</u>
- \* There are <u>similar implementation</u> issues to <u>diversity processing</u>
  - Firstly, the antennas at the BS and mobile should be reasonably <u>far</u> <u>apart</u>, ideally a few wavelengths of the carrier frequency, or should handle different <u>polarizations</u>
  - \* If the antennas are <u>too close</u> together, then the channel elements H<sub>ij</sub> will be very <u>similar</u>
  - \* This can easily take us into the situation where spatial multiplexing was <u>unusable</u> and we had to fall back to <u>diversity processing</u>

- A similar situation can easily arise in the case of <u>line-of-sight</u> transmission and reception. This leads us to an <u>unexpected</u> conclusion
  - Spatial multiplexing actually works best in conditions with <u>no direct line-of-sight</u> and <u>significant multipath</u>, because, in these conditions, the channel elements H<sub>ij</sub> are <u>uncorrelated</u> with each other
- In <u>line-of-sight</u> conditions, we often have to fall back to <u>diversity processing</u>

- As in the case of <u>closed loop transmit diversity</u>, the <u>PMI</u> depends on the carrier <u>frequency</u> and the <u>position</u> of the mobile
- For <u>fast moving</u> mobiles, <u>delays</u> in the feedback loop can make the PMI <u>unreliable</u> by the time the transmitter comes to use it, so <u>open loop spatial multiplexing</u> is often <u>preferred</u>

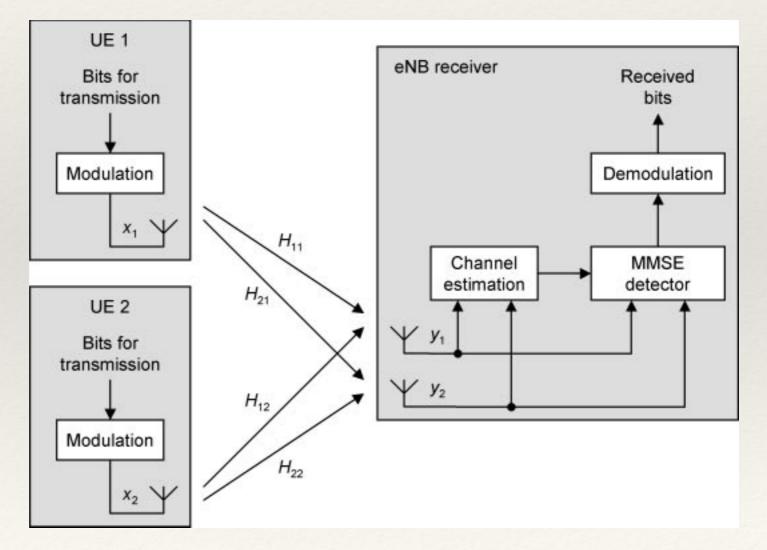
# 5.2 Spatial Multiplexing

- \* 5.2.1 Principles of Operation
- \* 5.2.2 Open Loop Spatial Multiplexing
- \* 5.2.3 Closed Loop Spatial Multiplexing
- \* 5.2.5 Implementation Issues
- 5.2.6 Multiple User MIMO

# 5.2.6 Multiple User MIMO

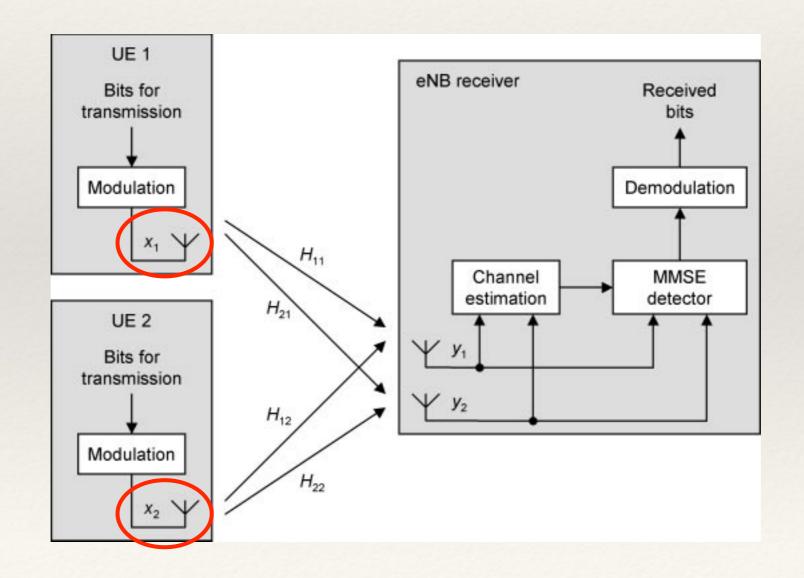
\* Two transmit and two receive antennas are sharing the <u>same transmission times</u> and <u>frequencies</u>, in the same

way as before



Uplink multiple user MIMO

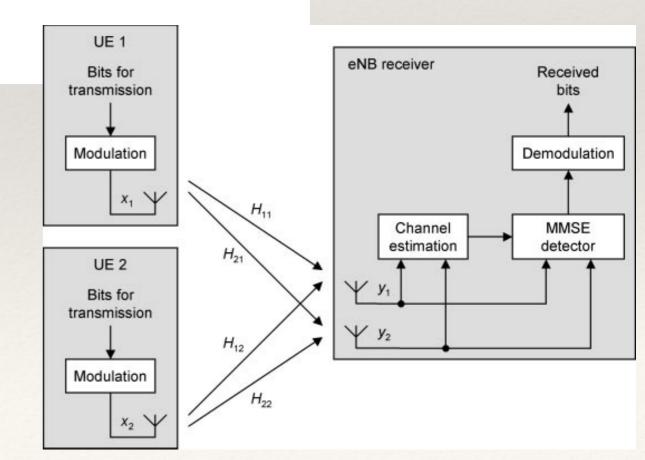
- The mobile antennas are on <u>two different mobiles</u> instead of one
- This technique is known as <u>multiple user MIMO</u> (MU-MIMO), in contrast with the earlier spatial multiplexing techniques, which are sometimes known as single user MIMO (SU-MIMO)



- \* This figure specifically shows the implementation of multiple user MIMO on the <u>uplink</u>, which is the <u>more common</u> situation
- The mobiles transmit at the <u>same time</u> and on the <u>same carrier</u> <u>frequency</u>, but without using any precoding and without even knowing that they are part of a spatial multiplexing system
- \* The BS receives their transmissions and <u>separates</u> them using (for example) the <u>minimum mean square error detector</u>

If  $\hat{Y}$  is a vector of n predictions, and Y is the vector of the true values, then the (estimated) MSE of the predictor is:

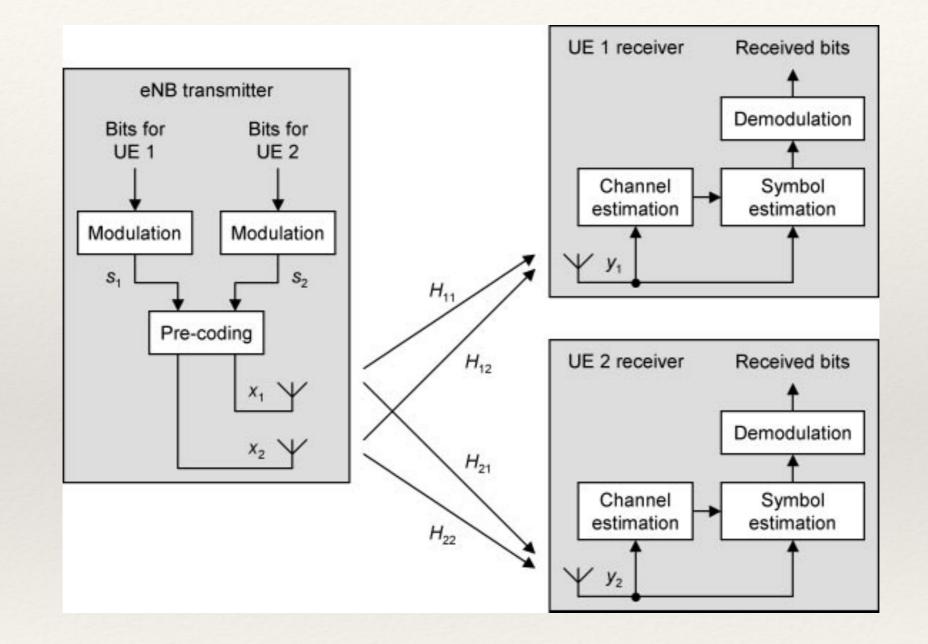
 $MSE = \frac{1}{n} \sum_{i=1}^{n} (\hat{Y}_i - Y_i)^2.$ 



- This technique <u>only works</u> if the channel matrix is <u>well</u> <u>behaved</u>, but we can usually <u>guarantee</u> this for two reasons
  - Firstly, the mobiles are likely to be <u>far apart</u>, so their <u>ray paths</u> are likely to be very <u>different</u>
  - Secondly, the BS can freely choose the mobiles that are <u>taking part</u>, so it can freely choose mobiles that lead to a <u>well-behaved</u> channel matrix

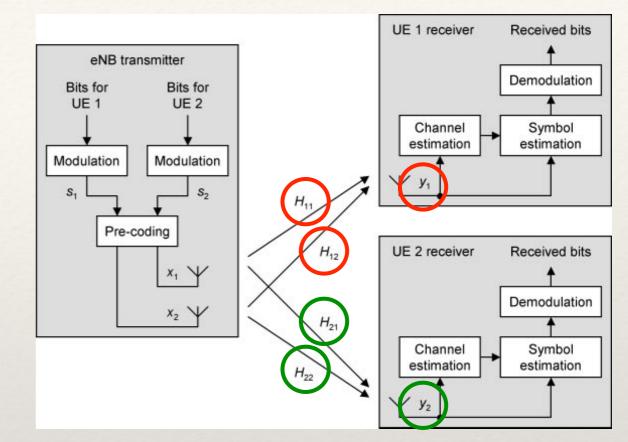
- <u>Uplink</u> multiple user MIMO does <u>not</u> increase the <u>peak</u> <u>data rate</u> of an individual mobile, but it is still beneficial because of the <u>increase</u> in <u>cell throughput</u>
- It can also be implemented using <u>inexpensive mobiles</u> that just have <u>one power amplifier</u> and <u>one transmit</u> <u>antenna</u>, not two
- For these reasons, <u>multiple user MIMO</u> is the <u>standard</u> technique in the uplink of LTE <u>Release 8</u>: <u>single user</u> <u>MIMO</u> is not introduced into the uplink until <u>Release 10</u>

\* We can also apply <u>multiple user MIMO</u> to the <u>downlink</u>, as shown in the following figure:

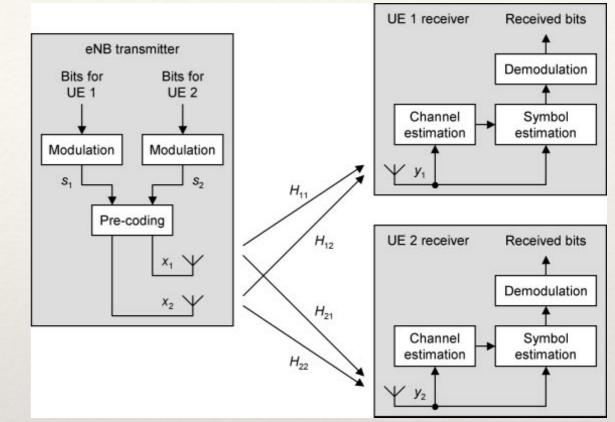


Downlink multiple user MIMO

- \* This time, there is a <u>problem</u>
- Mobile 1 can measure its received signal y<sub>1</sub> and the channel elements H<sub>11</sub> and H<sub>12</sub>, in the same way as before
  - However, it has no
     knowledge of the other
     received signal y<sub>2</sub>, or of the
     other channel elements H<sub>21</sub>
     and H<sub>22</sub>
- The <u>opposite situation</u> applies for mobile 2



- Neither mobile has complete knowledge of the channel elements or of the received signals, which <u>invalidates</u> the techniques we have been using
- The solution is to implement <u>downlink</u> multiple user
   MIMO by <u>adapting</u> another multiple antenna technique, known as <u>beamforming</u>



#### Contents

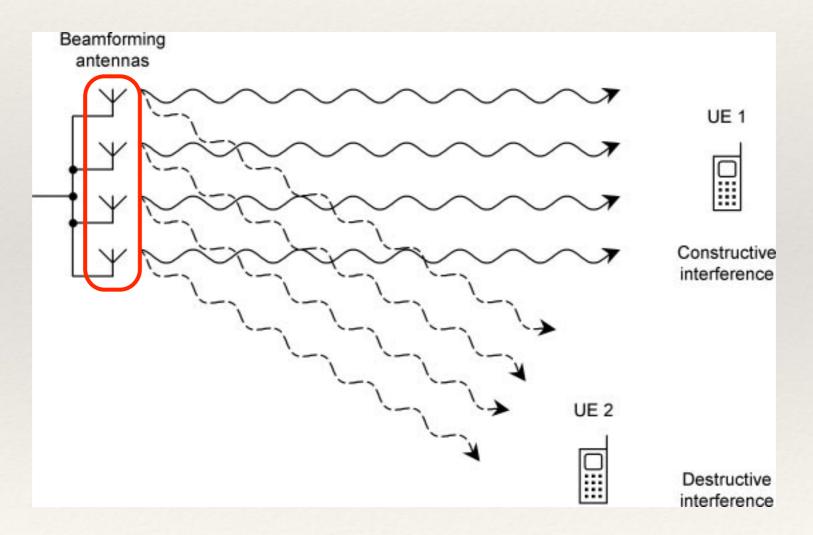
- 5.1 Diversity Processing
- \* 5.2 Spatial Multiplexing
- 5.3 Beamforming

# 5.3 Beamforming

- \* 5.3.1 Principles of Operation
- \* 5.3.2 Beam Steering
- \* 5.3.3 Dual Layer Beamforming
- \* 5.3.4 Downlink Multiple User MIMO Revisited

### 5.3.1 Principles of Operation

\* In beamforming, a BS uses multiple antennas in a completely different way, to **increase its coverage** 



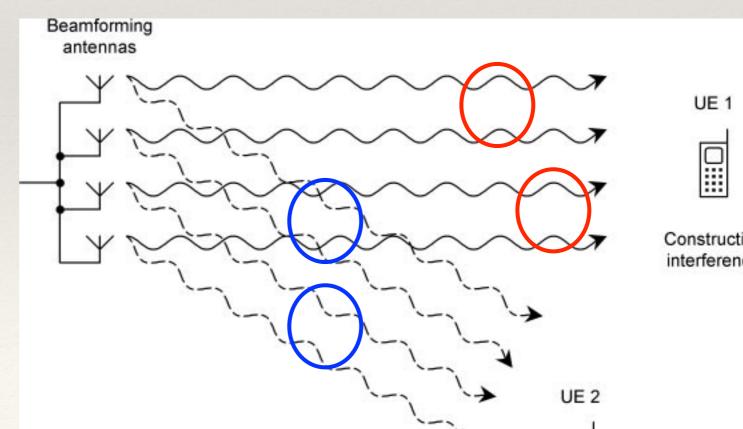
Basic principles of beamforming

\* UE 1

- \* Long way from the BS, on a line of sight that is at <u>right angles</u> to the antenna array
- The signals from each antenna reach UE 1 in phase, so they interfere \* constructively, and the received signal power is high

\* UE 2

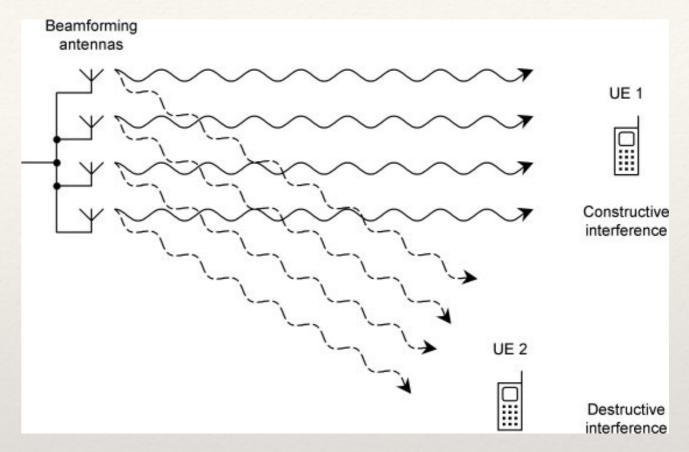
- \* At an <u>oblique</u> [斜的] <u>angle</u>, and receives signals from <u>alternate antennas</u> that are 180° out of phase
- \* These signals <u>interfere destructively</u>, so the received signal power is <u>low</u>
- \* We have therefore created a synthetic antenna beam, which has a main beam pointing towards UE 1 and a <u>null pointing</u> towards UE 2



UE 1

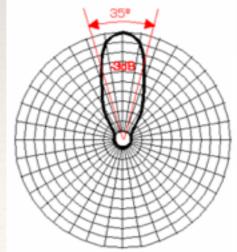
Beam steering using a set of phase shifts

\* The <u>beamwidth</u> is <u>narrower</u> than one from a single antenna, so the transmitted power is <u>focussed</u> towards mobile 1

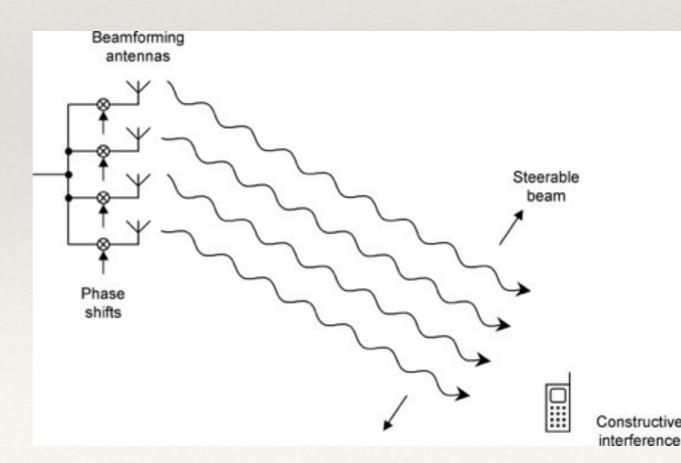


**Beamwidth**: In a radio antenna pattern, the <u>half power beam width</u> is the **angle** between the <u>half-power (-3 dB) points</u> of the main lobe [波瓣], when referenced to the <u>peak</u> effective radiated power of the main lobe

 $10 \log_{10}(1/2) = -3 dB$ 



- \* By applying a <u>phase ramp</u> [斜坡] to the transmitted signals, we can change the <u>direction</u> at which <u>constructive</u> <u>interference</u> arises, so we can <u>direct</u> the beam towards <u>any</u> <u>direction</u> we choose
- More generally, we can <u>adjust</u> the <u>amplitudes</u> and <u>phases</u> of the transmitted signals, by applying a suitable set of <u>antenna weights</u>



- \* We can use the same technique to construct a <u>synthetic</u> <u>reception beam</u> for the <u>uplink</u>
- By applying a suitable set of <u>antenna weights</u> at the BS receiver, we can ensure that the received signals add together <u>in phase</u> and <u>interfere constructively</u>
- In OFDMA, we can process <u>different sub-carriers</u> using different sets of <u>antenna weights</u>, so as to create <u>synthetic antenna beams</u> that point in different directions
- We can therefore use <u>beamforming</u> to communicate with <u>several different mobiles</u> at once using <u>different sub-</u> <u>carriers</u>, even if those mobiles are in completely <u>different</u> <u>locations</u>

- Beamforming works <u>best</u> if the <u>antennas</u> are <u>close</u> <u>together</u>, with a <u>separation</u> comparable with the <u>wavelength</u> of the radio waves
  - This ensures that the signals sent or received by those antennas are <u>highly correlated</u>
  - This is a <u>different</u> situation from diversity processing or spatial multiplexing, which work best if the antennas are <u>far apart</u>, with <u>uncorrelated</u> signals
- \* A BS is therefore likely to use <u>two sets of antennas</u>
  - \* A <u>closely spaced</u> set for beamforming
  - A <u>widely spaced</u> set for diversity and spatial multiplexing

# 5.3.2 Beam Steering

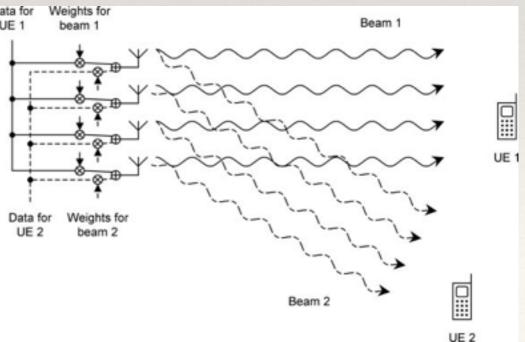
- \* How to calculate the <u>antenna weights</u> and <u>steer</u> [引導] the beam?
- \* For the <u>reception beams</u> on the <u>uplink</u>, there are two main techniques
  - Using the <u>reference signal</u> technique
    - The BS <u>adjusts</u> the <u>antenna weights</u> so as to <u>reconstruct</u> the mobile's <u>reference symbols</u> with the <u>correct signal phase</u> and the <u>greatest possible</u> signal to interference plus noise ratio (<u>SINR</u>)
  - \* An alternative is the **<u>direction of arrival technique</u>** 
    - \* The BS <u>measures</u> the <u>signals</u> that are received by each antenna and <u>estimates</u> the <u>direction</u> of the <u>target mobile</u>
  - From this quantity, it can estimate the <u>antenna weights</u> that are needed for satisfactory reception

- For the <u>transmission beams</u> on the <u>downlink</u>, how to calculate the antenna weights and steer the beam depends on the BS's <u>mode</u> of operation
  - \* In TDD mode
    - The uplink and the downlink use the <u>same carrier</u> <u>frequency</u>, so the BS can use the <u>same antenna weights</u> on the downlink that it calculated for the uplink
  - \* In FDD mode
    - \* The <u>carrier frequencies</u> are <u>different</u>, so the downlink antenna weights are different and are <u>harder</u> to estimate
  - For this reason, <u>beamforming is more common</u> in systems that are using <u>TDD</u> rather than FDD

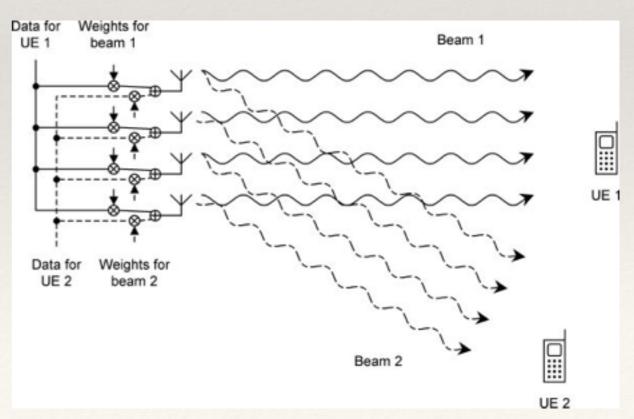
# 5.3.3 Dual Layer Beamforming

- In this technique, the BS sends <u>two different data streams</u> into its <u>antenna array</u>, instead of just one
- \* It then processes the data using <u>two different sets of antenna</u> weights and <u>adds</u> the results together before transmission
- In doing so, it has created <u>two separate antenna beams</u>, which share the <u>same sub-carriers</u> but carry <u>two different</u> <u>sets of information</u>

Dual layer beamforming using two parallel sets of <u>antenna weights</u>



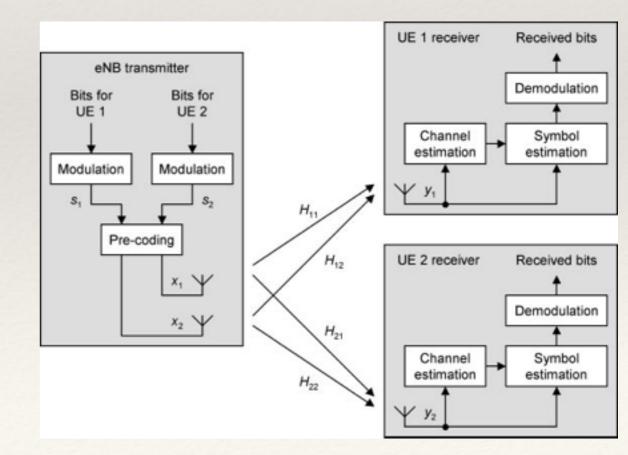
- \* The BS can then adjust the <u>antenna weights</u> so as to steer the beams to <u>two different mobiles</u>, so that the <u>first</u> mobile receives <u>constructive</u> interference from <u>beam 1</u> and <u>destructive</u> interference from <u>beam 2</u> and vice-versa
  - \* By doing this, the BS can <u>double</u> the <u>capacity</u> of the cell
- Alternatively, the BS can steer the beams to <u>two different</u> antennas on a <u>single mobile</u>, so as to <u>double</u> that mobile's <u>instantaneous data rate</u>



- In ideal conditions, the <u>maximum</u> number of <u>independent data streams</u> is equal to the number of <u>antennas</u> in the <u>array</u>
- LTE first supports the technique in Release 9 of the 3GPP specifications
  - In that release, the maximum number of data streams is limited to <u>two</u>, leading to the name of <u>dual layer</u> <u>beamforming</u>

#### 5.3.4 Downlink Multiple User MIMO Revisited

- Referring back to Figure 5.9, the only reliable solution is to precode the transmitted symbols s<sub>1</sub> and s<sub>2</sub>, so that s<sub>1</sub> is subject to <u>constructive</u> interference at UE 1 and <u>destructive</u> interference at UE 2, with the <u>opposite</u> situation applying for s<sub>2</sub>
- This implies that <u>downlink MU-MIMO</u> is best treated as a <u>variety</u> of beamforming, using BS antennas that are <u>close</u> together rather than far apart



- The <u>difference</u> between **downlink multiple user MIMO** and **dual layer beamforming** lies in the <u>calculation</u> of the <u>antenna weights</u>
  - \* In multiple user MIMO
    - \* Each <u>mobile</u> feeds back a <u>precoding matrix</u> from which the BS determines the <u>antenna weights</u> that it requires
  - \* There is <u>no such feedback</u> in **dual layer beamforming** 
    - Instead, the BS calculates the <u>downlink antenna</u> weights from its <u>measurements</u> of the mobile's <u>uplink</u> transmissions

- LTE first supports this <u>implementation</u> of <u>downlink</u> multiple user MIMO in Release 10 of the 3GPP specifications
- There is, however, <u>limited support</u> for downlink multiple user MIMO in Release 8
  - The Release 8 implementation uses the same algorithms that single user MIMO does, so the <u>performance</u> of downlink multiple user MIMO in <u>Release 8</u> is comparatively <u>poor</u>